

Diagnostic questions 8-13

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9. Simplify and state the restrictions for $\frac{3x^2-5x-2}{3x^2+13x+4} \div \frac{x^2-x-2}{x^2+3x-4}$

$$\begin{aligned} &= \frac{(x-2)(3x+1)}{(3x+1)(x+4)} \div \frac{(x-2)(x+1)}{(x+4)(x-1)} \\ &= \frac{x-2}{x+4} \div \frac{(x-2)(x+1)}{(x+4)(x-1)} \\ &= \frac{(x-2)(x+4)(x-1)}{(x+4)(x-2)(x+1)} \\ &= \frac{x-1}{x+1} \end{aligned}$$

10. Determine the equivalent to $\frac{x}{3x-6} - \frac{3}{2x-4}$

$$\begin{aligned} &= \frac{x(2x-4)}{(3x-6)(2x-4)} - \frac{3(3x-6)}{(2x-4)(3x-6)} \\ &= \frac{2x^2-4x}{(3x-6)(2x-4)} - \frac{9x-18}{(2x-4)(3x-6)} \\ &= \frac{2x^2-13x-18}{(3x-6)(2x-4)} \end{aligned}$$

11. Simplify $(2x^4 - 2x^2 - 7) - (3x^4 - x^3 + x^2 - 4) + (x^4 - x^3 + 2x^2 - 1)$

$$\begin{aligned} &= 2x^4 - 2x^2 - 7 - 3x^4 + x^3 - x^2 + 4 + x^4 - x^3 + 2x^2 - 1 \\ &= -x^2 - 4 \end{aligned}$$

12. Simplify $(x^2 - 2x - 1) + (3x^2 + x + 2)$

$$= 4x^2 - x + 1$$

13. Simplify $-2x(x+1)^2 + 3x(x-4)$

$$\begin{aligned} &= -2x^3 - 4x^2 - 2x + 3x^2 - 12x \\ &= -2x^3 - x^2 - 14x \end{aligned}$$