# Homework7

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## **STAT4205**

## dce2108

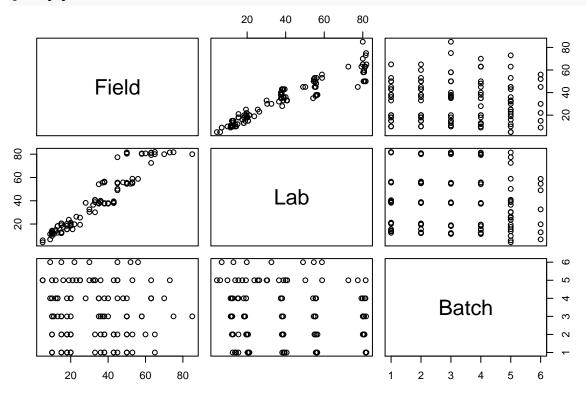
```
library(alr4)
library(ggplot2)
library(tidyverse)
```

# Problem 9.3

## head(pipeline)

```
##
     Field Lab Batch
## 1
        18 20.2
## 2
        38 56.0
                     1
        15 12.5
## 3
                     1
## 4
        20 21.2
                     1
## 5
        18 15.5
                    1
## 6
        36 39.0
```

## plot(pipeline)



```
labfield <- lm(Lab ~ Field, data=pipeline)</pre>
lab.line <- labfield$coefficients</pre>
lab.line
## (Intercept)
                       Field
     -1.967500
                   1.222968
##
plot(pipeline[1:2])
abline(lab.line[1], lab.line[2])
      80
                                                                                      0
                                                  0
      9
Lab
      40
```

m1.res <- labfield\$residuals

fieldlab <- lm(Field ~ Lab, data=pipeline)
field.line <- fieldlab\$coefficients

#field.line
plot(pipeline[2:1])
abline(field.line[1], field.line[2])</pre>

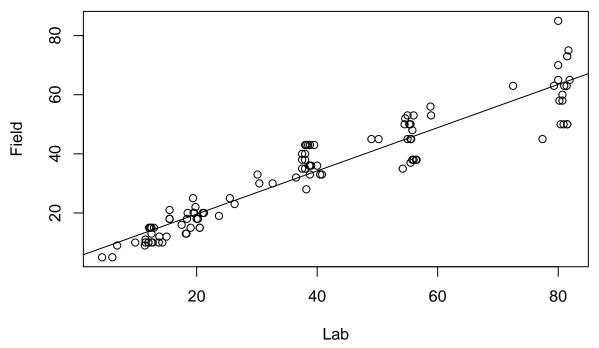
Field

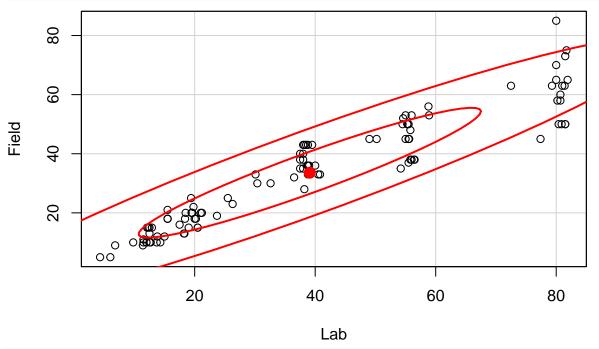
40

60

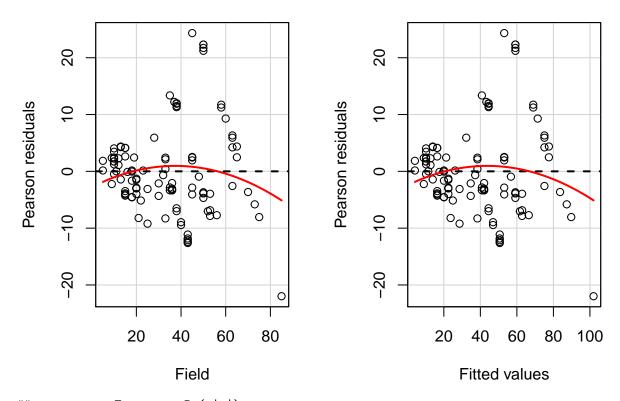
80

20





residualPlots(labfield)



```
## Test stat Pr(>|t|)
## Field -1.303 0.196
## Tukey test -1.303 0.193
```

The plot suggests non-constant variance since the curvature of the fitted values versus the residuals is quadratic.

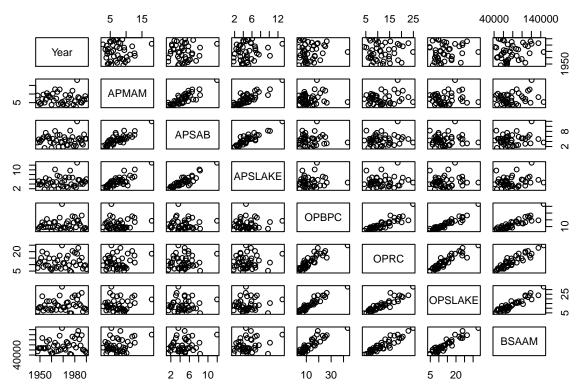
## ncvTest(labfield)

There is a lot p-value This means that the model is non-constant

## Problem 9.8

## head(water)

```
Year APMAM APSAB APSLAKE OPBPC
                                      OPRC OPSLAKE
                                                     BSAAM
## 1 1948
           9.13
                 3.58
                          3.91
                                4.10
                                      7.43
                                              6.47
                                                     54235
           5.28
                                              10.26
## 2 1949
                 4.82
                          5.20
                               7.55 11.11
                                                     67567
## 3 1950
           4.20
                 3.77
                          3.67
                                9.52 12.20
                                              11.35
                                                     66161
           4.60
## 4 1951
                          3.93 11.14 15.15
                                              11.13
                                                     68094
                 4.46
           7.15
## 5 1952
                 4.99
                          4.88 16.34 20.05
                                              22.81 107080
## 6 1953
          9.70
                 5.65
                          4.91
                               8.88 8.15
                                              7.41
                                                    67594
plot(water)
```



The problem asks:

#### Q: What is the model?

```
\log(\mathrm{BSAMM}) \sim \log(\mathrm{APMAM}) + \log(\mathrm{APSAB}) + \log(\mathrm{APSLAKE}) + \log(\mathrm{OPBPC}) + \log(\mathrm{OPRC}) + \log(\mathrm{OPSLAKE})
```

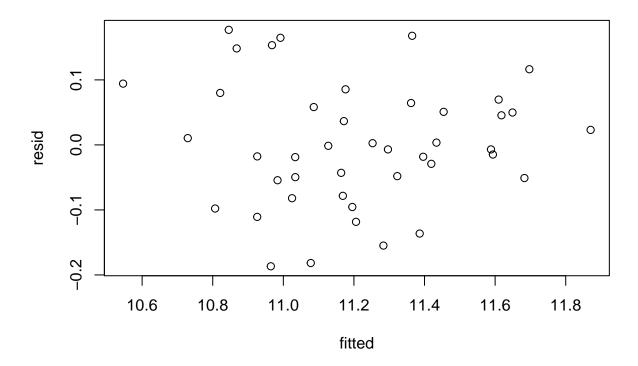
```
prob9.3 <- lm(log(BSAAM) ~ log(APMAM) + log(APSAB) + log(APSLAKE) + log(OPBPC) + log(OPRC) + log(OPSLAK summary(prob9.3)
```

```
##
## Call:
## lm(formula = log(BSAAM) \sim log(APMAM) + log(APSAB) + log(APSLAKE) +
##
       log(OPBPC) + log(OPRC) + log(OPSLAKE), data = water)
##
## Residuals:
##
        Min
                       Median
                  1Q
                                     3Q
                                             Max
##
  -0.18671 -0.05264 -0.00693 0.06130 0.17698
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                 9.46675
                            0.12354
                                     76.626
                                              < 2e-16 ***
## (Intercept)
                                     -0.308
## log(APMAM)
                -0.02033
                            0.06596
                                             0.75975
## log(APSAB)
                -0.10303
                            0.08939
                                     -1.153
                                             0.25667
## log(APSLAKE) 0.22060
                                      2.463
                                             0.01868
                            0.08955
## log(OPBPC)
                 0.11135
                            0.08169
                                      1.363
                                             0.18134
## log(OPRC)
                                      3.310 0.00213 **
                 0.36165
                            0.10926
## log(OPSLAKE) 0.18613
                            0.13141
                                      1.416 0.16524
```

<sup>&</sup>quot;Draw residual plots for the mean function described in Problem 8.3.4 for the California water data, and comment on your results."

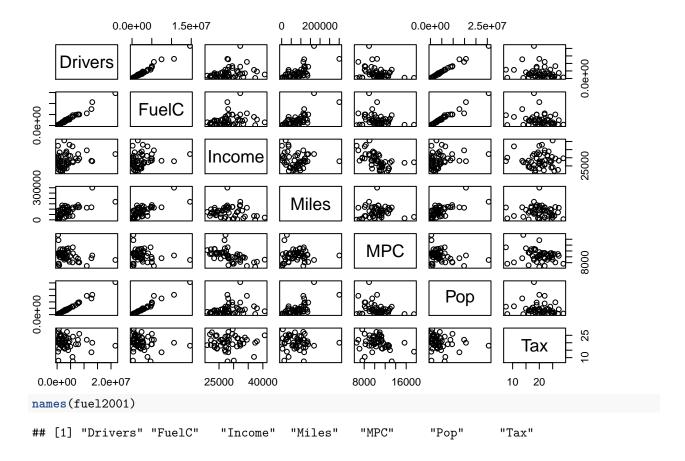
<sup>&</sup>quot;Test for curvature as a function of fitted values"

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1017 on 36 degrees of freedom
## Multiple R-squared: 0.9098, Adjusted R-squared: 0.8948
## F-statistic: 60.54 on 6 and 36 DF, p-value: < 2.2e-16
residualPlots(prob9.3)
Pearson residuals
                                      Pearson residuals
                                                                            Pearson residuals
                                                                                            0 000
                                                  0.0
                                          0.0
                                                                                0.0
                                          -0.2
    -0.2
                                                                                -0.2
              1.5
                    2.0
                         2.5
                                                          1.5
                                                               2.0
                                                                    2.5
                                                                                   0.5
                                                                                         1.0
        1.0
                                               0.5
                                                     1.0
                                                                                              1.5
                                                                                                    2.0
                                                                                                         2.5
               log(APMAM)
                                                     log(APSAB)
                                                                                          log(APSLAKE)
Pearson residuals
                                      Pearson residuals
                                                                            Pearson residuals
                                                     800
                                                         °°
                     0000
    0.0
                                                                                0.0
                                          0.0
                                                              8
    -0.2
         1.5 2.0 2.5 3.0 3.5
                                               1.5
                                                     2.0
                                                           2.5
                                                                 3.0
                                                                                    1.5
                                                                                         2.0
                                                                                               2.5
                                                                                                     3.0
                                                                                                          3.5
               log(OPBPC)
                                                      log(OPRC)
                                                                                          log(OPSLAKE)
Pearson residuals
    0.0
         10.6
               11.0
                      11.4
                            11.8
               Fitted values
##
                    Test stat Pr(>|t|)
## log(APMAM)
                         0.450
                                     0.656
                                     0.645
## log(APSAB)
                        -0.465
## log(APSLAKE)
                        -0.852
                                     0.400
## log(OPBPC)
                         1.385
                                     0.175
## log(OPRC)
                         0.839
                                     0.407
## log(OPSLAKE)
                         1.630
                                     0.112
## Tukey test
                                     0.066
                         1.839
resid <- prob9.3$residuals</pre>
fitted <- prob9.3$fitted.values</pre>
plot(fitted, resid)
```



# Problem 9.11

```
head(fuel2001)
                  FuelC Income Miles
##
       Drivers
                                           MPC
                                                    Pop Tax
     3559897
                2382507
                         23471
                                94440 12737.00
                                                3451586 18.0
## AL
                 235400
                         30064
                                                 457728
## AK
        472211
                                13628
                                      7639.16
                                                         8.0
## AZ
       3550367
                2428430
                         25578
                                55245
                                       9411.55
                                                3907526 18.0
                         22257
                                98132 11268.40
     1961883
                1358174
                                                2072622 21.7
## CA 21623793 14691753
                         32275 168771
                                       8923.89 25599275 18.0
## CO 3287922
                                85854
                2048664
                         32949
                                       9722.73 3322455 22.0
plot(fuel2001)
```



#### Linear Model

$$E(fuel|X) = B_0 + B_1 Tax + B_2 Dlic + B_3 Income + B_4 log(miles)$$

# Transform data

```
fuel2001 <- transform(fuel2001,</pre>
Dlic=1000 * Drivers/Pop,
Fuel=1000 * FuelC/Pop)
model9.11 <- lm( Fuel ~ Tax + Dlic + Income + log(Miles), data=fuel2001)</pre>
summary(model9.11)
##
## Call:
## lm(formula = Fuel ~ Tax + Dlic + Income + log(Miles), data = fuel2001)
## Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
                         5.895
                                         183.499
## -163.145 -33.039
                                 31.989
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                                        0.791 0.432938
## (Intercept) 154.192845 194.906161
```

```
## Tax
                                 2.030121
                                            -2.083 0.042873 *
                   -4.227983
                                              3.672 0.000626 ***
## Dlic
                    0.471871
                                 0.128513
## Income
                   -0.006135
                                 0.002194
                                             -2.797 0.007508 **
## log(Miles)
                   26.755176
                                 9.337374
                                              2.865 0.006259 **
## Signif. codes:
                      0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 64.89 on 46 degrees of freedom
## Multiple R-squared: 0.5105, Adjusted R-squared: 0.4679
## F-statistic: 11.99 on 4 and 46 DF, p-value: 9.331e-07
residualPlots(model9.11)
Pearson residuals
                                                     Pearson residuals
    20
                                                         50
    -150
                                                         -150
                     15
             10
                              20
                                      25
                                                             700
                                                                       800
                                                                                900
                                                                                          1000
                          Tax
                                                                               Dlic
                                                     Pearson residuals
Pearson residuals
                            8° 0
    50
                                                         50
    -150
                                                         -150
                                                                  8
              25000
                        30000
                                           40000
                                                                         9
                                                                                10
                                                                                              12
                                 35000
                                                                                       11
                                                                             log(Miles)
                         Income
Pearson residuals
    50
    -150
                        0
           400
                      500
                                600
                                          700
                       Fitted values
##
                Test stat Pr(>|t|)
## Tax
                    -1.077
                                0.287
## Dlic
                    -1.922
                                0.061
## Income
                    -0.084
                                0.933
                    -1.347
## log(Miles)
                                0.185
## Tukey test
                    -1.446
hat 9.11 <- hatvalues(model9.11)
hat_9.11
                                                                 CA
                                                                              CO
##
             AL
                          AK
                                       ΑZ
                                                    AR
   0.09767199\ 0.25609617\ 0.03339132\ 0.06348242\ 0.08668537\ 0.09825485
             CT
                          DE
                                       DC
                                                    FL
                                                                 GA
   0.26953288 0.12350939 0.41491327 0.10088750 0.18246091 0.20572692
##
                          IL
                                       IN
                                                    IA
## 0.06429223 0.08496379 0.05534860 0.03644005 0.03632232 0.06000338
##
             LA
                         ME
                                      MD
```

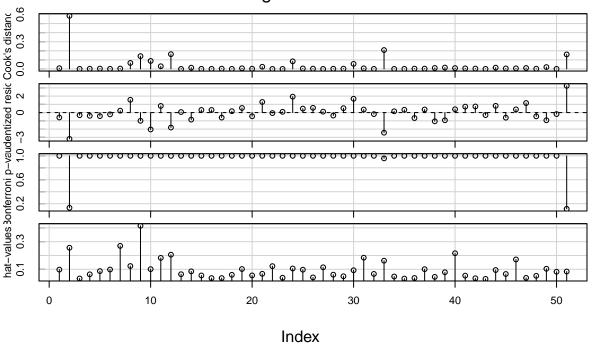
```
## 0.10182252 0.05552660 0.06745367 0.12277212 0.03872358 0.10573833
##
                       MΩ
           MS
                                  MT
                                              NF.
                                                          NV
## 0.09716522 0.04125576 0.11430006 0.06085993 0.04945254 0.09306405
                                              NC
                       NM
                                  NY
                                                         ND
## 0.18395399 0.06650900 0.16237155 0.04755207 0.03267468 0.03689858
           ΠK
                       \mathsf{OR}
                                              RΙ
                                                          SC
                                  PA
## 0.10086971 0.04489247 0.07853836 0.21620511 0.05408396 0.03504750
##
           TN
                       ΤX
                                  UT
                                              VT
                                                          VΑ
## 0.03062388 0.09460381 0.06589521 0.17117439 0.03779511 0.05252210
           WV
                       WI
                                  WY
## 0.10375252 0.08213607 0.08378222
states <- c("AK", "NY", "HI", "WY", "DC")
hat_fivestates <- hat_9.11[states]</pre>
hat_fivestates
##
           AK
                       NY
                                  ΗI
                                              WY
                                                          DC
## 0.25609617 0.16237155 0.20572692 0.08378222 0.41491327
fuel <- c(514.279, 374.164, 426.349, 842.792, 317.492)
ehat_fuel <- c(-163.145, -137.599, -102.409, 183.499, -49.452)
hat_fuel \leftarrow c(0.256, 0.162, 0.206, 0.084, 0.415)
states_resid <- model9.11$residuals[states]</pre>
r_hat <- ehat_fuel / ( states_resid * sqrt(1 - hat_fuel))
r_hat
         ΑK
                            ΗI
## 1.159347 1.092395 1.122253 1.044847 1.307444
n <- 51
p_prime <- 5
t \leftarrow r_hat * ((n - p_prime - 1) / (n - p_prime - r_hat^2))^(1/2)
##
         AK
                  NY
                            ΗI
                                     WY
## 1.163805 1.094749 1.125502 1.045914 1.317873
D i <- (1/p prime) * r hat^2 * (hat fuel /(1 - hat fuel))
names(D_i) <- states</pre>
D_i
##
           ΑK
                       NY
                                  ΗТ
                                              WY
                                                          DC:
## 0.09249625 0.04613814 0.06535186 0.02002255 0.24253174
dl <- cooks.distance(model9.11)</pre>
dl
##
                                         AZ
                                                                    CA
             AT.
                           ΑK
                                                      AR.
## 7.800459e-03 5.850260e-01 7.188822e-04 2.111673e-03 3.540623e-03
             CO
                           CT
                                         DE
                                                      DC
## 1.019614e-03 4.054545e-03 6.568633e-02 1.407798e-01 8.807427e-02
             GA
                           HI
                                         ID
                                                      TT.
## 2.932058e-02 1.624367e-01 6.391753e-05 1.358427e-02 1.203642e-03
##
             ΙA
                           KS
                                         ΚY
                                                      LA
```

```
## 7.891835e-04 2.797952e-03 3.743808e-04 7.223696e-03 2.392345e-03
         MD MA MI MN
## 2.368748e-02 1.073745e-04 6.916698e-05 8.353715e-02 5.043638e-03
                     MT
                               NE
                                           NV
## 2.912985e-03 3.408831e-04 1.727086e-03 3.028305e-03 5.546151e-02
         NJ
                    NM NY NC
## 6.298652e-03 4.988883e-04 2.081099e-01 2.620893e-04 8.025976e-04
          OH OK OR
                                    PA
## 3.407617e-03 3.214596e-03 1.050371e-02 1.479644e-02 9.046794e-03
      SC SD TN TX
## 6.004272e-03 4.029751e-03 5.884541e-04 1.415694e-02 5.442837e-03
          VT VA WA
                                      VW
## 6.294248e-03 1.042558e-02 2.349349e-03 2.014122e-02 5.942758e-04
##
## 1.596169e-01
r <- rstudent(model9.11)
                    ΑK
                             ΑZ
                                        AR
## -0.59604249 -3.19302217 -0.31940486 -0.39101498 -0.42802758 -0.21405044
         CT
                  DE DC FL
                                                 GA
   0.23197297 \quad 1.54976004 \quad -0.99621024 \quad -2.04875497 \quad 0.80740453 \quad -1.81436531
##
          ID
             IL
                        IN
                                  IA
                                            KS
   0.06745827 - 0.85273394 \ 0.31734297 \ 0.31984853 - 0.60502152 \ 0.16942711
##
               ME
                              MD
                                       MA
                                                  MΤ
   0.56022239 \; \hbox{--}0.44712723 \quad 1.28876755 \; \hbox{--}0.06126147 \quad 0.09165130 \quad 1.93472315
##
                             MT
                   MO
##
                                       NE
                                                   NV
   0.48000082 0.57755619 0.11368351 -0.36157527 0.53528241 1.67591799
##
         NJ
                   NM
                             NY
                                       NC
                                                  ND
##
   0.37025366 -0.18513742 -2.43822460 0.16028647 0.34135279 -0.66279376
##
                    \mathsf{OR}
                        PA
                                  RI
                                            SC
   0.37495905 \ -1.05843156 \ -0.93030491 \ \ 0.40123926 \ \ 0.72082107 \ \ 0.74115757
         TN
             TX
                         UT
                                       VT
                                                  VA
WV
                    WΙ
## -0.93135606 -0.18029570 3.24608995
r.newModel <- r[states]</pre>
dl.newModel <- dl[states]</pre>
n <- 51
p_prime <- 5
t <-r.newModel * ((n - p_prime - 1) / (n - p_prime - r.newModel^2))^(1/2)
                  NY
                           ΗI
## -3.5796348 -2.5843496 -1.8624129 3.6566188 -0.9961265
r.newModel
                 NY
                           _{
m HI}
                                     WY
## -3.1930222 -2.4382246 -1.8143653 3.2460899 -0.9962102
```

```
dl.newModel
##
## 0.5850260 0.2081099 0.1624367 0.1596169 0.1407798
p.new \leftarrow 2*pt(-abs(t),df=n-1)
p.adjust(p.new, method = "bonferroni")
##
                                      ΗI
            AK
                         NY
## 0.003883200 0.063615878 0.342129610 0.003069248 1.000000000
outlierTest(model9.11)
##
## No Studentized residuals with Bonferonni p < 0.05
## Largest |rstudent|:
      rstudent unadjusted p-value Bonferonni p
## WY 3.24609
                          0.002212
                                         0.11281
Wyoming has the largest influence on the regression
```

influenceIndexPlot(model9.11)

# Diagnostic Plots



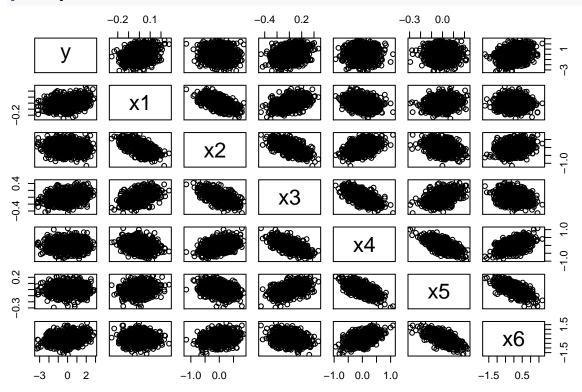
# #Extra Practice Problems

# Problem 9.1

head(Rpdata)								
##	У	<b>x1</b>	x2	х3	x4	х5	x6	

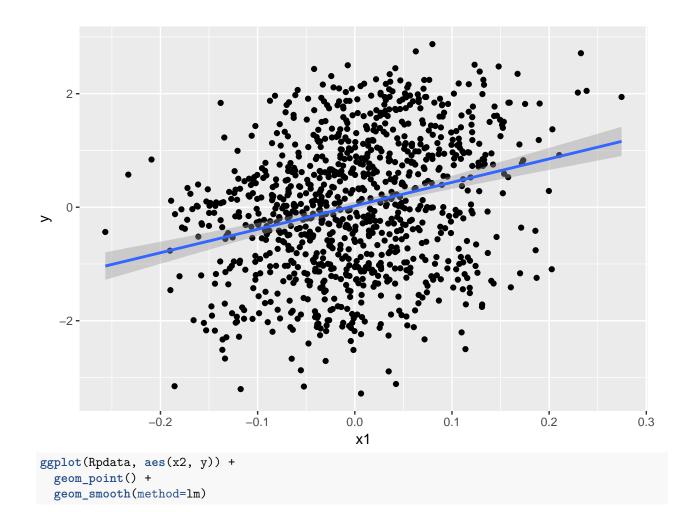
```
## 1 0.31680 -0.034611 -0.0635220 0.0437570 -0.030642 0.1303200 -0.56870  
## 2 -0.58091 -0.028196 0.2368700 -0.1884600 0.190510 -0.0818980 0.29123  
## 3 -0.38789 0.059727 0.0884460 -0.0946590 0.022736 0.0073608 0.40923  
## 4 -0.31245 0.052236 0.0032441 -0.1222200 0.127780 0.0471430 -0.64441  
## 5 0.96025 -0.057986 0.0659260 -0.0070171 0.107700 0.1265700 -0.71757  
## 6 1.18400 0.189340 -0.4765500 0.1547300 -0.321130 0.0726280 -0.13887
```

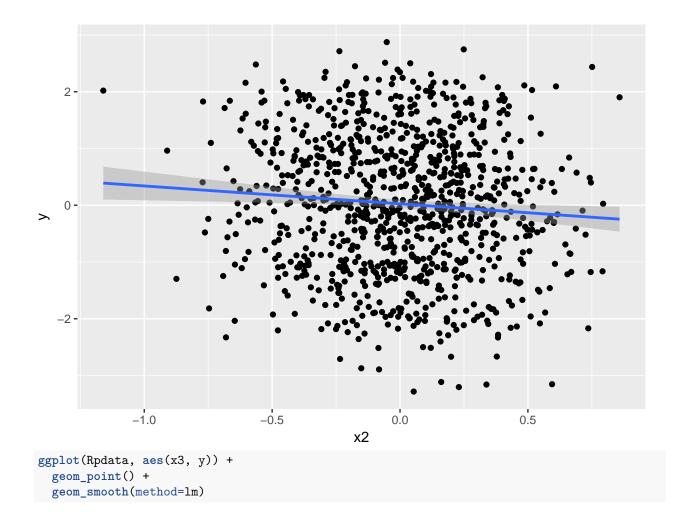
## pairs(Rpdata)

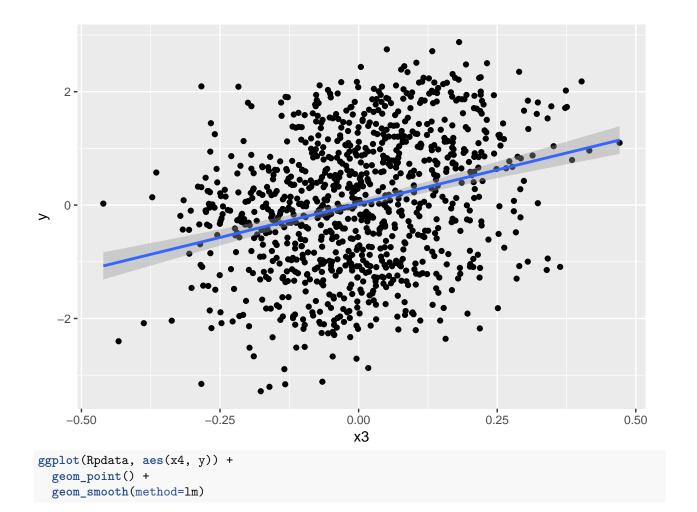


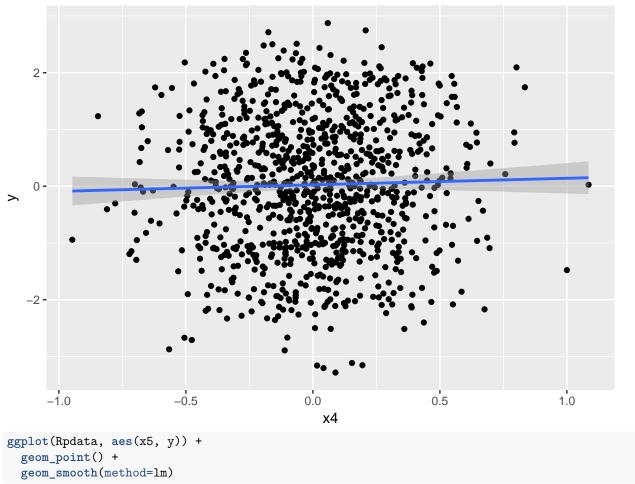
The variables next to each other seem strongly correlated, except with x1 and y. x1 neighbors is x2.

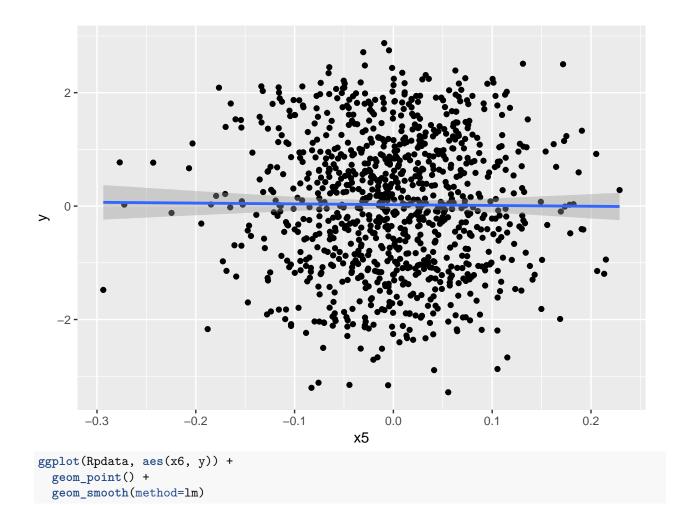
```
ggplot(Rpdata, aes(x1, y)) +
  geom_point() +
  geom_smooth(method=lm)
```

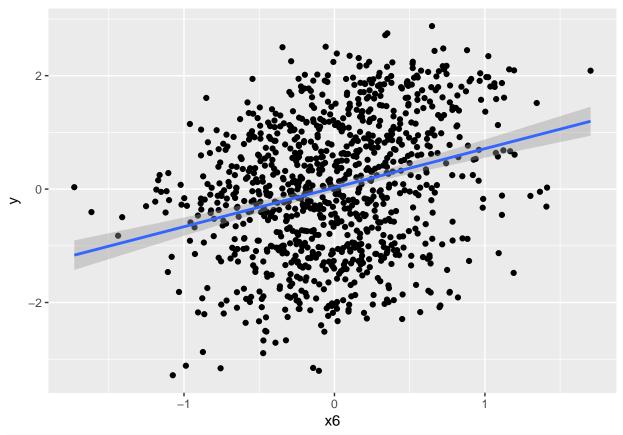










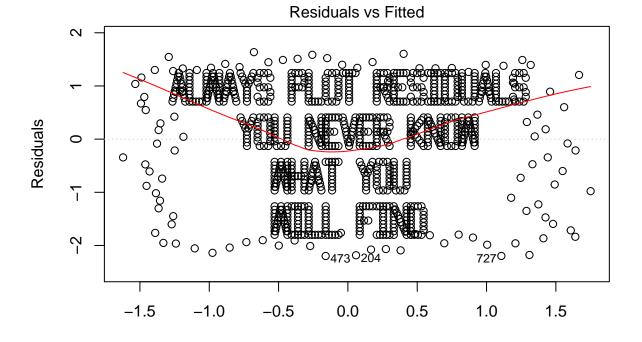


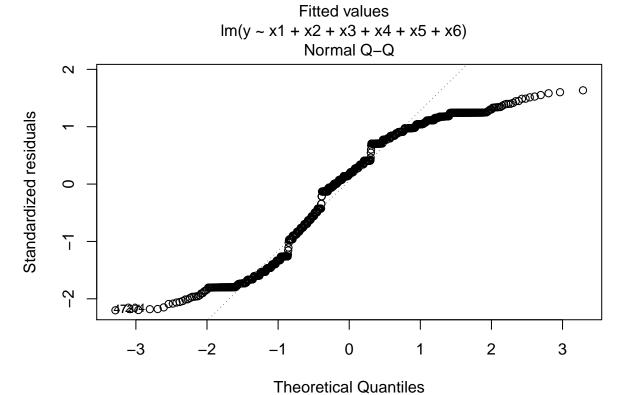
 $pr9.1 \leftarrow lm(y \sim x1 + x2 + x3 + x4 + x5 + x6, data = Rpdata)$ summary(pr9.1)

```
##
## Call:
## lm(formula = y \sim x1 + x2 + x3 + x4 + x5 + x6, data = Rpdata)
##
## Residuals:
       Min
                1Q Median
                                3Q
                                       Max
## -2.1977 -0.7631 0.1729
                           0.8851
                                   1.6359
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.02481
                          0.03188
                                    0.778
                                              0.437
## x1
               4.14061
                           0.50954
                                     8.126 1.32e-15 ***
               1.01233
                           0.15522
                                    6.522 1.11e-10 ***
## x2
## x3
               3.99614
                           0.32663 12.234 < 2e-16 ***
                                    5.766 1.09e-08 ***
## x4
               0.96045
                           0.16657
               3.75122
                           0.64726
                                    5.796 9.17e-09 ***
## x5
## x6
               0.95390
                           0.08561 11.142 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.003 on 983 degrees of freedom
## Multiple R-squared: 0.3112, Adjusted R-squared: 0.307
## F-statistic: 74.03 on 6 and 983 DF, p-value: < 2.2e-16
```

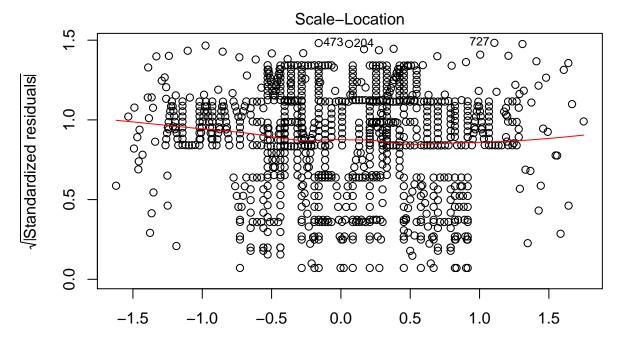
All the p-values are signficant. This might mean that the model is wrong.

```
pr9.1.1 \leftarrow lm(x1 \sim x2, data = Rpdata)
summary(pr9.1)
##
## Call:
## lm(formula = y ~ x1 + x2 + x3 + x4 + x5 + x6, data = Rpdata)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -2.1977 -0.7631 0.1729 0.8851 1.6359
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.02481
                          0.03188
                                   0.778
                                              0.437
## x1
                           0.50954
                                    8.126 1.32e-15 ***
               4.14061
## x2
               1.01233
                           0.15522
                                    6.522 1.11e-10 ***
## x3
               3.99614
                           0.32663 12.234 < 2e-16 ***
               0.96045
                           0.16657
                                     5.766 1.09e-08 ***
## x4
## x5
               3.75122
                           0.64726
                                     5.796 9.17e-09 ***
               0.95390
                           0.08561 11.142 < 2e-16 ***
## x6
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.003 on 983 degrees of freedom
## Multiple R-squared: 0.3112, Adjusted R-squared: 0.307
## F-statistic: 74.03 on 6 and 983 DF, p-value: < 2.2e-16
pr9.1.2 \leftarrow lm(x2 \sim x1, data = Rpdata)
summary(pr9.1.2)
##
## Call:
## lm(formula = x2 ~ x1, data = Rpdata)
##
## Residuals:
##
        Min
                  1Q
                     Median
                                    3Q
                                            Max
## -0.73758 -0.16832 -0.00125 0.17387 0.86465
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.036e-07 7.813e-03
                                        0.00
## x1
              -2.384e+00 9.724e-02 -24.51
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2458 on 988 degrees of freedom
## Multiple R-squared: 0.3782, Adjusted R-squared: 0.3776
## F-statistic: 600.9 on 1 and 988 DF, p-value: < 2.2e-16
plot(pr9.1)
```

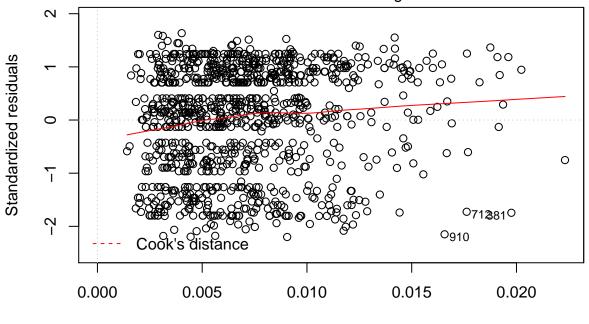




 $Im(y \sim x1 + x2 + x3 + x4 + x5 + x6)$ 



Fitted values  $Im(y \sim x1 + x2 + x3 + x4 + x5 + x6)$  Residuals vs Leverage



Leverage  $Im(y \sim x1 + x2 + x3 + x4 + x5 + x6)$ 

resid <- pr9.1\$residuals
fitted <- pr9.1\$fitted.values
plot(fitted, resid)</pre>

