

# HW 1

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Instructions:

- Work on your own.
- You may write code to do some of the work. Do not submit your code.

## Transposition Cipher

- Columnar Transposition
- Write the message in a rectangle
- Example:

Key: 4312567

	4	3	1	2	5	6	7
Plaintext:	a	t	t	a	c	k	p
	o	s	t	p	o	n	e
	d	u	n	t	i	l	t
	w	o	a	m	x	y	z

Ciphertext: TTNAAPTMTSUOAODWCOIXKNLYPETZ

## Substitution Ciphers

- Change characters in plaintext to produce ciphertext
- Example (Caesar cipher)
  - Uses a left shift of  $k$  to protect messages
  - Plaintext is HELLO WORLD
  - $K=3$ : Change each letter to the third letter following it (X goes to A, Y to B, Z to C)
  - PT: A B C D E F G H I J K L M N O P Q R S T U V W X Y Z
  - CT: D E F G H I J K L M N O P Q R S T U V W X Y Z A B C
  - Ciphertext is KHOOR ZRUOG

We talked in class briefly about transposition and substitution operations used by symmetric key encryption algorithms. A transposition cipher is one that uses the

transposition operation only. A substitution cipher is one that uses the substitution operation only. A product cipher is one that uses both.

### Q1 (6pts) Transposition Ciphers

a) (2pt) Encrypt the following plaintext using the Columnar transposition cipher. Use the key: 10243 (key size is 5):

theshadowofthemoonsweptacrosstheglobe fromhongkongtothetexaspanhandleasareannu  
larsolareclipsebeganmondaymorninginasiaandtraversedthepacificthesunappearedasathinri  
ngbehindthemoontopeoplein anarrowpathalongthecenterofthetrackwhichbeganinsouthern  
hinaheavycloudsobscuredtheviewinhongkongbutresidentsoftokyoandothercitieswereablet  
ogetaspectacularviewforaboutfourminutesaroundseventhirtytwoammondaysixthirtytwo  
pmetSundayevents wereheldatschoolsandmuseumsinJapanwhilemanymorepeopletookintheu  
nusualastronomical eventathomeoronstreetcornersafterwhizzingacrossthepacifictheshado  
wemergedovernorthernCaliforniaandsouthernoregonwherethousandsofpeopleattendedparti  
estowatchtheeventthefirsttoappearintheunitedstatessincenineteenninetyfour expertswarned  
thathopefulviewersshouldnotpeerupattheskywithoutspecialviewingequipmentsince lookin  
g atthesunwiththenakedeyecancauseblindnessderekralstonaprofessionalphotographersaidh  
eusedaweldingfiltertocaptureadirectviewofeclipseinthefoothillsaboveorovillecaliforniahes  
haredthephotooncnnreportnotingtheratherslimswathoftheglobewhocouldseetheimpactoft  
heeclipsealstonsaidhewantedtoenabletherestoftheworldtoseehowclearitlookedtothoseofus  
whowerefortunateenoughtoseeittheliverofsunshinethentraveledsoutheastacrosscentralnev  
adasouthernutahandnorthernarizonaandthennewmexicoitpassedoveralbuquerque newmexi  
coaboutseventhirtyfourpmninethirtyfourpm beforepeteringouteastoflubbocktexas accordi  
ngtonasa

ciphertext:

hdtopoeehotxnlrnrpgnogitrihararetoeiraoeehccaornvusdihotdoyocsaosarfouurstymatym  
nweslmmaharpohssoltmnenfhniofeorvrnfaorgeodeadrtcetrareetnnntrrrhpvrutuhwucigpsl  
nhwhēcuisespsatpauwntrrieshtseiareepoirieemheeoieplseentshleciktoheueheeeunneoar  
eldtuntanteipdaueeastypetrberutbtadotafoerhbmkoadaaaaieomnsdetctnasnbdopeaplhttaig  
seiaobevnkuiskdreetatawb nadntadxtpueshtodujwmoooutuananoerawirhihdeo oriiseehnp  
enastetioahtaiieueatoleoortyo evniteitntkealerlaenoaseailouivfptolvvcohreonothhihbcsec  
hianhteetrswroewrtegehvsievseccaaunarnodnxterqumotntrnrutresuksrtaeohntsgfonhah  
eansesadriarsefepetihhnnonrtncrkhnnunaydcteonrefotiwb gpcvourtoehtmyhtedeelcsuspinel  
keutmeaestetigspiswgetcoaunorusotetohvhs piudecenyetnaeislppeitieemiogeiedasnsktrslo  
hisegeaeceehaollnsdhnrtnrsgwuemoessawdahtedeltehfofnntisrnetlusonnahtdhrahwca  
olnxbefhmtypetitobecin homwctoogttnpselllbyianvdacueaignmolnwatnfrhenhheloreig  
bstoneiretcleafisneronirosyteaonennemetnnlochrrosrztctamdnelndhrwtaflepeahnf tetitsn  
enopwdhuwhnetkhpliunctuhaycbneanfohrrhddittdtoinolooefaahtnpottlatoodhatlrod nolrf  
oooatssertustifhhdhasrvorhorznneiseuqwcueruiioeotgalcaogsswesaslrngesaaruocenann  
aaepisdpdhnietpaohgeotwbitchcsuhwngentahteleuirtmeuviwosiwtanrdhasialypeiuarivtotcr  
ezasacheerharntonesoptdiwteetpnnssetifxsetfesdeastsawqenoastneneddrooipgedelfrpacwli

fibrliihtocengaswflhltpfcetiatbeowtheldouwoaootlostrettsteseaneiaemosvbreiovionhfmfen  
efoxcna

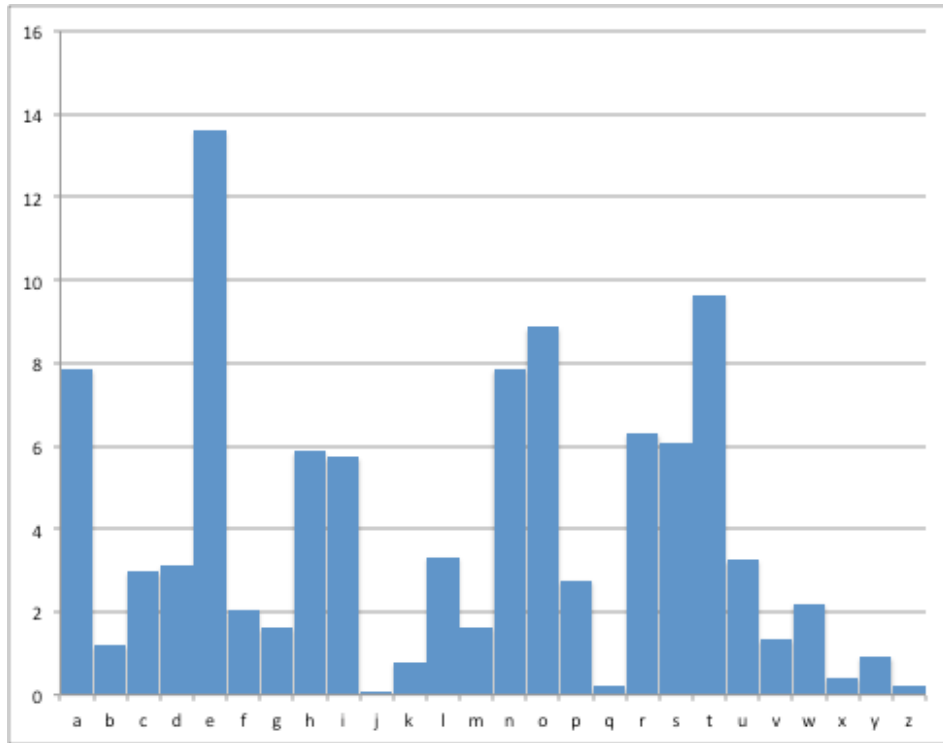
b) (2pt) How many possible keys can you use to encrypt this message using this cipher?  
What does that say about the susceptibility of the message to brute force attacks?

Since there are 10 (0-9) unique digits with 10 distinct possibilities at each position, we have  $10^{10}$  possible keys.

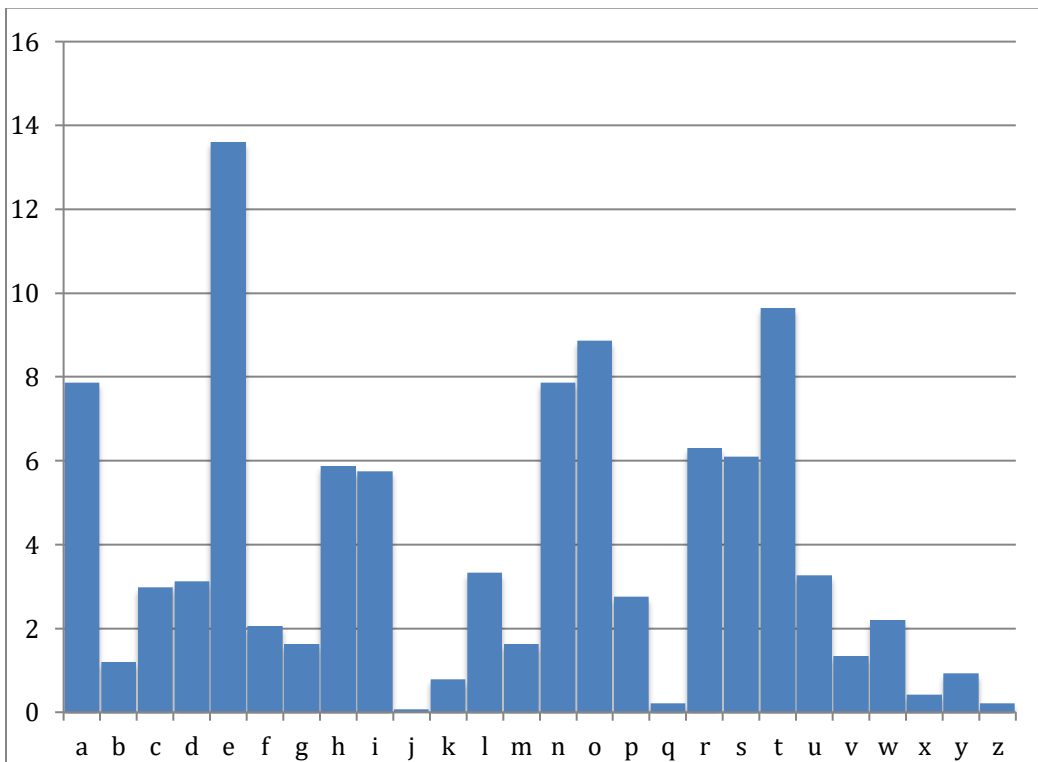
Key Size	Cipher	Number of Alternative Keys	Time Required at $10^9$ decryptions/s	Time Required at $10^{13}$ decryptions/s
56	DES	$2^{56} \approx 7.2 \times 10^{16}$	$2^{55}$ ns = 1.125 years	1 hour
128	AES	$2^{128} \approx 3.4 \cdot 10^{38}$	$2^{127}$ ns = $5.3 \cdot 10^{21}$ years	$5.3 \times 10^{17}$ years
168	3DES	$2^{168} \approx 3.7 \cdot 10^{50}$	$2^{167}$ ns = $5.8 \cdot 10^{33}$ years	$5.8 \cdot 10^{29}$ years
192	AES	$2^{192} \approx 6.3 \times 10^{57}$	$2^{191}$ ns = $9.8 \times 10^{40}$ years	$9.8 \cdot 10^{36}$ years
256	AES	$2^{256} \approx 1.2 \times 10^{77}$	$2^{255}$ ns = $1.8 \times 10^{60}$ years	$1.8 \cdot 10^{56}$ years
10	OURS	$10^{10}$	$5^{10}$ ns = 9.77 milliseconds	0.977 microseconds

It very suspectable to brute force attacks that can be completed in mere seconds (as seen by trying  $\frac{1}{2}$  the key space to find solution).

c) (2pt) Calculate and plot the letter frequencies of the ciphertext (use the spreadsheet provided) and compare it to that of the English letters shown below. What is the relationship between both?



Source: [https://en.wikipedia.org/wiki/Letter\\_frequency](https://en.wikipedia.org/wiki/Letter_frequency)



Transposition cipher was used and so the letter frequencies are the same (as they were not substituted or altered just moved/transposed).

## Q2 (6pts) Substitution Ciphers

a) (2pt) Encrypt the following plaintext using the Caesar substitution cipher. Use the key 10:

theshadowofthemoonsweptacrosstheglobe fromhongkongtothetexaspanhandleasareannu  
larsolareclipsebeganmondaymorninginasiaandtraversedthepacificthesunappearedasathinri  
ngbehindthemoontopeopleinananarrowpathalongthecenterofthetrackwhichbeganinsouthern  
hinaheavycloudsobscuredtheviewinhongkongbutresidentsoftokyoandothercitieswereablet  
ogetaspectacularviewforaboutfourminutesaroundseventhirtytwoammondaysixthirtytwo  
pmetSundayevents werelhdschoolsandmuseumsinJapanwhilemanymorepeopletookintheu  
nusualastronomical eventathomeoronstreetcornersafterwhizzingacrossthepacifictheshado  
wemergedovernorthernCaliforniaandsouthernoregonwherethousandsofpeopleattendedpart  
estowatchtheeventthefirsttoappearintheunitedstatessincenineteenninetyfour expertswarned  
thathopefulviewersshouldnotpeerupattheskywithoutspecialviewingequipmentsincelookin  
gathesunwiththenakedeyecancauseblindnessderekr alstonaprofessionalphotographersaidh  
eusedaweldingfiltertocaptureadirectviewofeclipseinthefoothillsaboveorovillecaliforniahes  
haredthephotooncnreportnotingtheratherslimswathoftheglobewhocouldseetheimpactoft  
heeclipseralstonsaidhewantedtoenabletherestoftheworldtoseehowclearitlookedtothoseofus  
whowerefortunateenoughtoseeittheliverofsunshinethentraveledsoutheastacrosscentralnev  
adasouthernutahandnorthernarizonaandthennewmexicoitpassedoveralbuquerque newmexi  
coaboutseventhirtyfourpmninethirtyfourpmetbeforepeteringouteastoflubbocktexasaccordi  
ngtonasa

ciphertext:

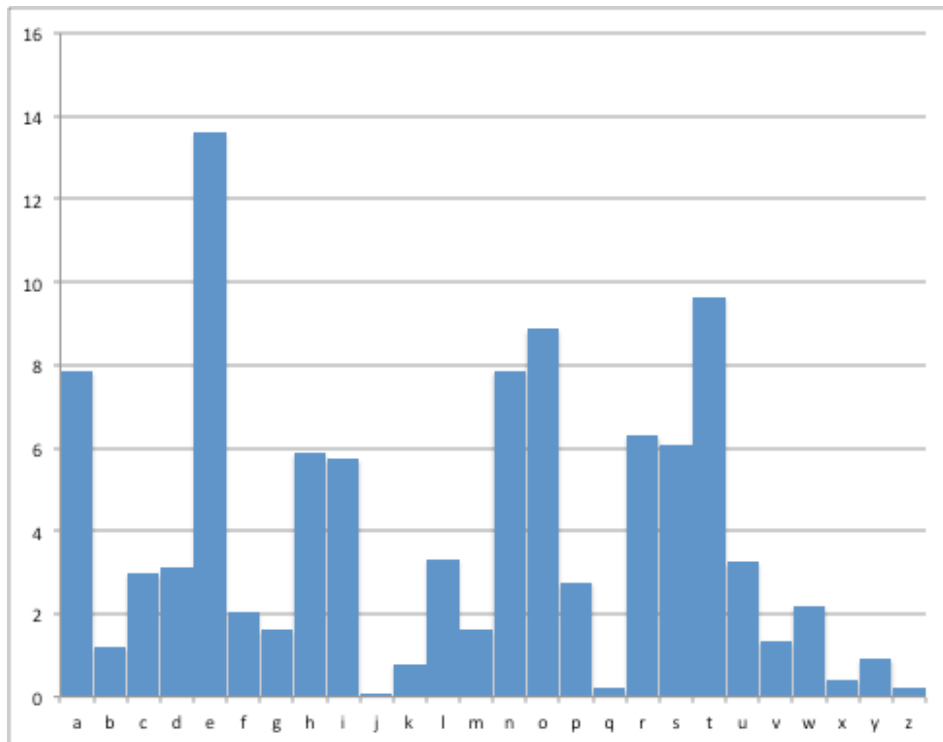
drocrknygypdrowyyxcgozdkmbyccdroqvylpbywryxquyxqdydrodohkczkxrknvokckbbk  
okxxevkbcyvk bomvszcoloqkxwyxnkiwybxsxqsxkskxndbkfobcondrozkm spsmdrocexk  
zzokbonkckdrsxbsxqlorsxndrowyyxdyzo yzv osxkxbbygzkdrkvxqdromoxdobypdrodbk  
mugrsmrloqkxsxcyedrobxmrsxkrokfimvyencylcm ebondrofsogsxryxquyxqledbocsnoxdcy  
pdyuiyxnydrobmsdsocgoboklvodyqodkczomdkmevkbfsogpybklyedpyebwsxedockbyex  
ncofoxdrsbidigykwwyxnkicshdrsbidgyzwodcexnkiofoxdcgoborovnkdc mryyvckxnweco  
ewcsxtkzkxgrsvowkxiwybozoyzvodyyusxdroexecekvkcdbyxywsmkvofoxdkdrywoybyxc  
dboodmybxobckpdobgrsjjsxqkmbyccdrozkm spsmdrocrknygowobqonyfobxybdrobxmkvs  
pybxskkxncyedrobxyboqyxgrobodryeckxncypzoyzvokddoxnonzkbsocdygkdmrdrofox  
ddropsbcdy kzzokbsxdroexsdoncdkdccsxmoxsxo doxxsxo dipyebohzobdcgkboxndrkdr  
yzopev fsogobccryevnxydzoo bezkddrocuigsdryedczomskv fsogsxqoeszwoxdcsmovyyus  
xqkddrocexgsdrdroxkuonoiomkxmkecolvsxn xocnoboubkvc dyxkzbypoccsyxkvzrydyqbk  
zrobcksnroeconkgovnsxqpsvdobdymkzdeboknsbomdf sogypomvszcosxdropy ydrsvvcklyf  
oybyfsvvomkvspybxskrocrkbondrozrydyxmxxsbozybdxydsxqdrobkdrobcvswcgkdrypdr  
oqvyl ogrymyevncoodros wzkm dypdroomvszobkvcdyxcksnrogkxdondyoxklvodrobocdyp  
drogybvndycoorygm vokbsdvyyuondy drycoypecgrygobopybdexkdooxyeqr dycoosddrocvs  
fobypcexcrsxodroxdbkfo voncyedrokcdkbyccmoxdbkvxofknkcyedrobxedkrkxnybdrob  
xkbsjyxkxndroxxogwohsmysdzkcony fobkvlaeobaexogwohsmyklyedcofoxdrsb dipye  
bzwxsxodr sbdipyebzwodlopybozodobsxqyedokcdypvellymudohkckmmybnsxqdyxkck

b) (2pt) How many possible keys can you use to encrypt this message using this cipher? What does that say about the susceptibility of the message to brute force attacks?

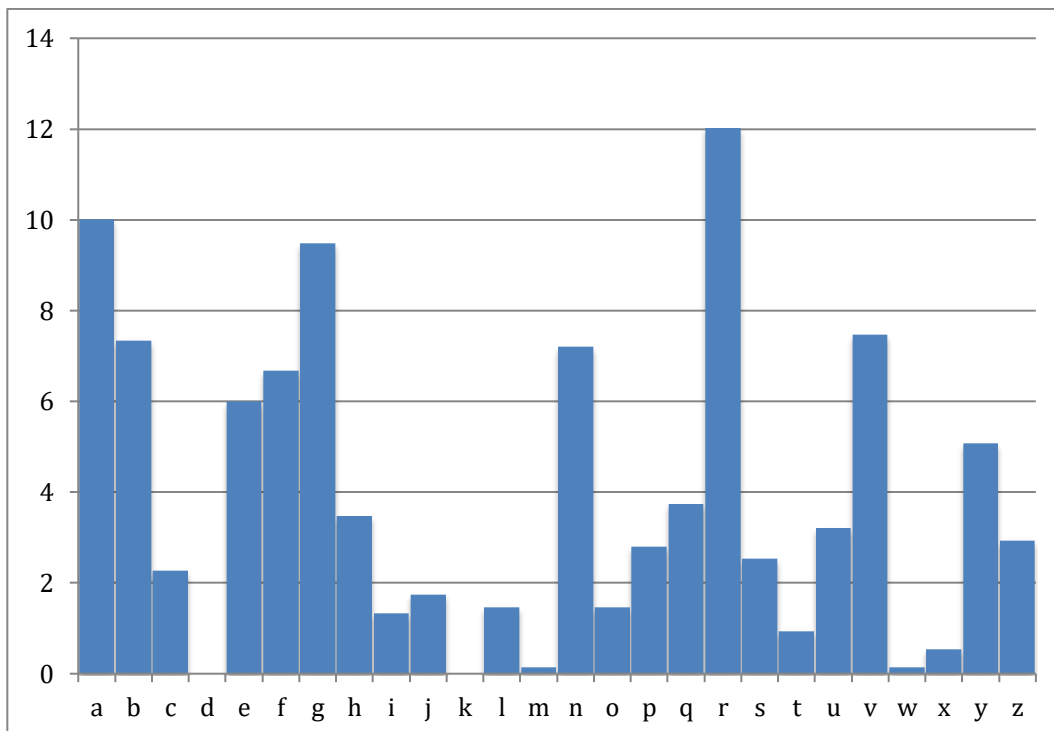
25 keys can be used to give unique outputs.

If the language along with the statically frequency inference is known, Caesar can be easily broken even if the key space is large (key space is small though, which makes ciphertext even easier to crack).

c) (2pt) Calculate and plot the letter frequencies of the ciphertext (use the spreadsheet provided) and compare it to that of the English letters shown below. What is the relationship between both?



Source: [https://en.wikipedia.org/wiki/Letter\\_frequency](https://en.wikipedia.org/wiki/Letter_frequency)



It can be seen that the second plot is shifted (by 10) from the first plot.

### Q3 (8pts) Vigenere Cryptanalysis

The ciphertext is posted to the blackboard (same folder as the assignment) in a file called “ciphertext”

a) (2pts) Do a **repetition test on the cipher**. You can use this site:

[http://www.simonsingh.net/The\\_Black\\_Chamber/vigenere\\_cracking\\_tool.html](http://www.simonsingh.net/The_Black_Chamber/vigenere_cracking_tool.html).

Add a screenshot (make it fit in the space below) of some of the repeated sequences

Vigenere Repeat Distance		Possible length of key (or factors)																			
Repeated Sequence	Spacing	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	
TLG	219		X																		
TLG	132	X	X	X		X					X	X									
TLG	978	X	X			X															
TLG	690	X	X		X	X				X					X						
GJL	435		X		X										X						
JLF	744	X	X	X		X		X				X									
JLF	189		X				X		X												
FKI	1026	X	X			X			X									X	X		
KIE	483		X				X														
KIE	543		X																		
IEY	495		X		X				X		X				X						
YBR	114	X	X			X													X		
YBR	360	X	X	X	X	X		X	X	X		X			X			X		X	
YBR	732	X	X	X		X						X									
YBR	75		X		X										X						
YBR	114	X	X			X													X		
YBR	39		X										X								
YBR	189		X				X		X												
YBR	168	X	X	X		X	X	X				X		X							
YBR	12	X	X	X		X						X									
YBR	279		X						X												
YBR	54	X	X			X			X										X		
BRS	1696	X		X				X								X					
RSY	612	X	X	X		X			X			X					X	X			
SYJ	741		X										X							X	
IEP	1449		X				X		X												
NVR	2190	X	X		X	X				X					X						
VRY	875				X		X														
YFY	78	X	X			X							X								
YFY	1908	X	X	X		X			X			X							X		
YCY	825		X		X						X				X						
YCY	484	X		X							X										
CZJ	825		X		X						X				X						
JUA	1644	X	X	X		X						X									
UAI	78	X	X			X							X								
UAI	72	X	X	X		X		X	X			X							X		
UAI	1362	X	X			X															

Based on the test, what do you think the key size is? 3

b) (2pts) Break the ciphertext into sets, where each set corresponds to the letters shifted by a given key. List the sets below

Set1:

wtjksdpryjimuqftwzynyfaktjjlylyshwyxithxqyrxtqlqgnitwttyyxhiisihrrffsdwsttmwxw  
wxhyxusnzxyssfnnewjqsfwwwjhngffsdwfftmurlrdjyablftjkwjjnxwskfnifjfrfryisfjrj



fbisywkrnfuytmiiwdxifmjjyjgyzldxajrjghkrswrghnxfnsjjhytxqsjjfnjjfwstsnnhuxjgx  
 sfllwyxtfujfjsxfjhqjtssfbmjwnfgjhhqhuytttdtmjtyjxfssfyqtjxisfxyjmcifqzjkuijhyifxdz  
 thntsdqxjxsttjmnxfzsiwkurjfwxwyfuijsqfjftsqsniftnfjffafzonnrfsxkeqfxjaryylzmljf  
 jwyxdhwjijqjtxstjntftqabqjtyuujtwkplxqlitmzttnwngfqxyqfzhygyfkntjsywyibqjsijbmy  
 gswxsrbpfxulxjnstrsnfhufgtgstmnxiwyfcjfbmlsxitjtxfmfwjtjnjjwttjyqnzztynbjwhwjddj  
 xftryftqtrsxsxnwjhjjwjsjntyswntnmjwjtryfynfsyuqiftwjyxfbmtwmyjwsjjxttfjstwjfsjwts  
 rsjfifxhjaxawjjtfenxybjstnzyhyyyqtmymchjijbxxfxtfinfdyxxsywjizsbfayfjsiaffyntftwlyn  
 yxnjnznfzmyqnrjxxfbwyhjl

**Set2:**

yllibyincuiyocnhymimmqymlmhlcgcjnyuujxyuibvyhfusnhjjnzhbqbeuzwvclfnlqaeall  
 eygxixnibmswlyyugnmwgyysudwjumonljwlnicyfnhlywcwyncycxfjmoyuxfjmuchuu  
 ihlcycolivmummimxbciuliyholnuniucfuvhihizlaunbyyujfmuumyjfuiqwlylnyuowxam  
 mvmxxilwyoumwlfujfbagcxuibnmpmqlhywhfunmfmsncauymhufiyyiynlfqxyqlcmmla  
 wluyghgyycvqhyniclswmololilchimxwblgujwnqbahmgutnnxbocqxilchwyxyihlolacdc  
 mfmlewwpjhvfwingclhiygutyulynnmmyiilymcmflxibibecfycxljxkmizgnhlcicuoblizu  
 cccnyimlylmzchlnyucyvnofonnhfxfsbcolixwmyxfecbixciiuijwhcuiwhawgnwycfhleuy  
 zygupcsfmhxucjnclmhnnjxmnlnjnmvubuhlcziyypyiuiinnfwymnhysxmyynaabclc  
 mugfhcuuyhhipqhwymeblsnbociclyhiqlccocnijnguzggghmxphhawmynwgilhyxmbub  
 yyhxqlhuiqbclazlguybwflyicydahymmwyzwccxfbcnwbyuiignuhynngxwyahbhlhhibi  
 abmlxmmivniiynuconnmuuyily

**Set3**

cgferjevzageopvfsrqpfnbgvqvnabbvhfeaeheysrnqvrybnrerflnnnrarrlvaferybvs  
 agbnhrhvnevbcbgraevrjigvqpgvzbbbgrrelrucryagvvsghbabquaervgvpvayfszrbyap  
 ygaggaaafgyrvfcfenbraegareqrarrorsgayirfynhbgbvornoaqhvbevgnhvgauurievao  
 gbvyfgyuzvinnweygfhrhvvqnanszverafcfjuaifyugrbqngegyuelanqazsuybgalz  
 vuvhuvopzgnvzyrrgreeavfpfypbfghaqagvbnjnznunvgcgcfruevnaabfebaggfvpeq  
 bpnabrjysnybrryghqycebrbqygrtvfzvyrurafhnbgafrasransmypagrbghgaeavn  
 rraaogrblvgsaabaabsgccrjgtrufepfbfgrguvgiinbraflhobvejgarhnrseyeyrvayqyv  
 gbrzuyrlqbfefggranrfrgznfabbrgecqugerbaczebrgexrjcfgefarahtaabrghaavnpb  
 novfqbefaqjgvanganbyijyrjruqhazrrjvbropanfghrrgaetfebbuyxepcvntrzgrvnaab  
 bizlprhyxncfgaftvgavnqnrppfafnnsgrzefhznrrugsgaihyavanrryfsprffrauqnrb  
 qrszvohgyungeqpfabnfstvgfrunbeaqin

- c) (2pts) Find the letter that has the highest frequency in each set (you can use the spreadsheet provided) and use it to guess the key.

Sets	Letter with highest freq.	Assuming this letter is “e” then the key to decrypt this set is
set 1	j	5 (f)
set 2	y	20 (u)
set3	r	13 (n)

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Key: fun

d) (2) What is the plaintext?

reporters for the new york times and other publications refuse to discuss a wave of stories denigrating motion picture stars and producers all of them based on illegally obtained property of sony that was hacked and fenced by criminals apparently working for north korea's murderous dictatorship. sony pictures entertainment was victimized recently in a major corporate security breach apparently in retaliation for the upcoming comedy the interview. digital copies of fun released films, personal financial data on entertainment industry notables, email passwords and other information are reported to be one hundred terabytes of data. in all, have been stolen about forty gigabytes have been made public. so far, mainstream publications which are never reticent about scolding less established media over arcane journalistic scruples are publishing damaging data from this trove as newspapers and news channels call the stolen sony data with great relish and barely concealed contempt for hollywood. the new york times is sharing gunchar's charitable comments made in emails between the extraordinarily successful producers scott rudin and sony studio co-chair woman amy pascal. the washington post emphasizes that rudin had unkind words for prominent actress, director and producer angeline jolie as well as for an ill-conceived plan to build a cleopatra movie around joliet. time magazine's sam frizell teases these seven most outrageous things we learned from the sony hack. frizell declined to respond to questions from national review online about the propriety of trafficking in stolen goods for the purpose of writing breathless articles about scuttlebutt that if it involved any other industry would be considered well within the boundaries of normal workplace gossip. in a similar declining to comment, michael cieply and brooks barnes of the times and variety's alex stedman. a washington post editor responds that the paper does not permit reporters to break the law in pursuit of stories. we never encourage anyone to steal documents, national economy and business editor greg schneider writes in an email to national review online. how ever, when documents make their way into the public domain or are sent to us, we are within our right to report on them. leaks from companies and government agencies are not uncommon. over many decades, such leaks have presented news organizations with a wider range of circumstances that call for them to exercise judgment. we assess each set of facts individually. in this instance, the release of documents was an event that demanded coverage and the information brought to light has stirred discussion about a host of legitimate issues that also warrant adequate coverage.