

Here we provide the pseudo code for linear SVM. We assume that the following parameters are known.

- \mathbf{w}, w_0 : the weights/parameters to be updated by SGD
- m : the size of minibatch
- n : the size of data
- l : the learning rate

And the gradient under different cases are as follows: (you need to compute $\mathbf{f}_1, \mathbf{f}_2, g_1, g_2$ by taking the derivatives of the objective function)

- $\frac{\partial f}{\partial \mathbf{w}} = \begin{cases} \mathbf{f}_1, & \text{if } 1 - y^t(\mathbf{w}^T x + w_0) \leq 0 \\ \mathbf{f}_2, & \text{if } 1 - y^t(\mathbf{w}^T x + w_0) > 0 \end{cases}$
- $\frac{\partial f}{\partial w_0} = \begin{cases} g_1, & \text{if } 1 - y^t(\mathbf{w}^T x + w_0) \leq 0 \\ g_2, & \text{if } 1 - y^t(\mathbf{w}^T x + w_0) > 0 \end{cases}$

In SVM, the Labels y are 1/-1 rather than 0/1, you need to make corresponding adjustment with the input data

Algorithm 1 fit(X, y)

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1: for  $epoch = 1, 2, \dots$  do
2:   for  $batch = 1, 2, \dots, \frac{n}{m}$  do
3:     Compute the gradient  $\partial f$  (you need to choose between  $\mathbf{f}_1, \mathbf{f}_2, g_1, g_2$ 
       by considering  $1 - y^t(\mathbf{w}^T x + w_0)$ ) (notice the  $x$  used here is the set that
       containing only the data in the corresponding mini-batch.
4:     Update weight:  $\mathbf{w} \leftarrow \mathbf{w} - l \frac{\partial f}{\partial \mathbf{w}}, w_0 \leftarrow w_0 - l \frac{\partial f}{\partial w_0}$ 
5:   end for
6:   (Optional) Early Stopping to terminate training when the models
       has already converge before the end of pre-defined number of epochs.
7: end for
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Algorithm 2 predict(X)

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1: for  $x = 1, 2, \dots, n$  do (we iterate over all the testing data instances)
2:    $score = \mathbf{w}^T x + w_0$ 
3:   if  $score > 0$  then
4:     Set corresponding label  $y$  as 1
5:   else
6:     Set corresponding label  $y$  as -1
7:   end if
8: end for
```
