

DAY 3

1. Find the area of the minor segment, if radius of the circle is 21 cm and the chord makes angle 120° at the centre. [Example 3]

Sol:- Here $r = 21 \text{ cm}$, $\theta = 120^\circ$

$$\begin{aligned}\text{Area of Minor segment} &= \frac{\pi r^2 \theta}{360^\circ} - \frac{1}{2} r^2 \sin \theta \\&= \frac{22}{7} \times 21 \times 21 \times \frac{120^\circ}{360^\circ} - \frac{1}{2} \times 21 \times 21 \times \sin 120^\circ \\&= 462 - \frac{1}{2} \times 21 \times 21 \times \cos 30^\circ \quad \{\text{As } \sin 120^\circ = \cos 30^\circ\} \\&= 462 - \frac{441}{2} \times \frac{\sqrt{3}}{2} = \left(462 - \frac{441\sqrt{3}}{4}\right) \text{ cm}^2\end{aligned}$$

2. Find the area of a quadrant of a circle whose circumference is 22 cm. [Ex 12.2. Q2]

Sol:- Given Circumference of circle = 22

$$\Rightarrow 2\pi r = 22 \quad \Rightarrow 2 \times \frac{22}{7} \times r = 22$$

$$\Rightarrow r = \frac{22 \times 7}{22 \times 2} = \frac{7}{2} \text{ cm}$$

$$\text{Area of quadrant} = \frac{1}{4} \pi r^2 = \frac{1}{4} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} = \frac{77}{8} \text{ cm}^2$$

3. A brooch is made with silver wire in the form of a circle with diameter 35mm. The wire is used in making 5 diameters which divide the circle into 10 equal sectors as shown in the figure. Find:

i) The total length of the silver wire required.

ii) The area of each sector of the brooch

Sol:- Diameter of the circle = 35mm \Rightarrow radius (r) = $\frac{35}{2}$ mm

i) According to question, the silver wire is used in making circumference and 5 diameters.

$$\begin{aligned}\therefore \text{The total length of the silver wire} &= \left(\text{Circumference of the circle}\right) + 5(\text{diameters}) \\&= 2\pi r + 5 \times 35 = 2 \times \frac{22}{7} \times \frac{35}{2} + 175 = 110 + 175 = 285 \text{ mm}\end{aligned}$$

ii) Now Given The brooch is divided into 10 equal sectors.

$$\therefore \text{Area of each sector} = \frac{1}{10} \pi r^2 = \frac{1}{10} \times \frac{22}{7} \times \frac{35}{2} \times \frac{35}{2} = \frac{385}{4} \text{ mm}^2$$

4. An umbrella has 8 ribs which are equally spaced. Assuming that umbrella to be flat circle of radius 45 cm. Find the area between the two consecutive ribs of the circle.

[Ex 12.2, Q10]

Sol:- radius (r) = 45 cm

Given circular umbrella is divided into 8 equal parts.

$$\therefore \text{Area of each sector} = \frac{1}{8} \pi r^2 = \frac{1}{8} \times \frac{22}{7} \times 45 \times 45 = \frac{22275}{28} \text{ cm}^2$$



5. A round table cover has six equal designs, If the radius of the cover is 28 cm. Find the cost of making the designs at the rate of ₹ 0.35 per cm^2 . (Use $\sqrt{3} = 1.7$) [Ex 12.2, Q13]

Sol:- radius (r) = 28 cm

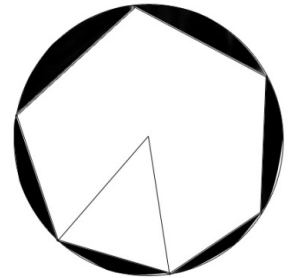
Given table cover divided into six equal designs. So angle made at the centre is

$$\frac{360^\circ}{6} = 60^\circ \text{ and each design is in the shape of minor segment.}$$

$$\begin{aligned} \text{Area of complete design} &= 6 \left(\frac{\pi r^2 \theta}{360^\circ} - \frac{1}{2} r^2 \sin \theta \right) \\ &= 6 \times \left(\frac{22}{7} \times 28 \times 28 \times \frac{60^\circ}{360^\circ} - \frac{1}{2} \times 28 \times 28 \times \sin 60^\circ \right) \\ &= 6 \times \left(\frac{1232}{3} - 392 \times \frac{\sqrt{3}}{2} \right) = 6 \times \left(\frac{1232}{3} - 392 \times \frac{1.7}{2} \right) \end{aligned}$$

$$= 6 \times (410.67 - 333.2) = 6 \times 7.47 = 464.82 \text{ cm}^2$$

$$\text{Now cost of making the design} = 464.82 \times 0.35 = 162.69 \text{ ₹}$$



EXERCISE

1. Ex 12.2, Q 8,11,12,14