# CS4551 Multimedia Software Systems (Spring 2018)

## **DCT-Based Image Compression**

- No due date. No submission is required.
- Do not use any Java built-in image class methods, library, or tools to complete this task.

## What your program should do

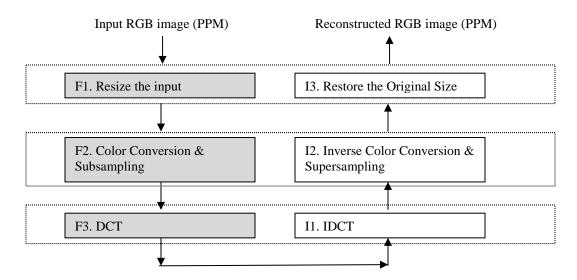
Name your main application as *CS4551\_[Your\_Last\_Name].java*. Your program should accept one command line argument indicating for the input PPM file name.

## <eg> On Command Prompt

java CS4551\_Doe Ducky.ppm

# **DCT-based Image Compression**

Implement a DCT transform algorithm.



Encoding Steps	Decoding Steps
F1. Read and resize the input image	I3. Remove Padding and Display the image
Read the input ppm file containing RGB pixel values for encoding. First, if the image size is not a multiple of 8 in each dimension, make (increase) it become a multiple of 8 and pad with zeros. For example, if your input image size is 21x14, make it become 24x16 and fill the extra pixels with zeros (black pixels).	Display the reconstructed image. Remember that you padded with zeros if the input image size is not multiple of 8 in both dimensions (width and height). Restore the original input image size by removing extra padded rows and columns.
F2. Color space transformation and Subsampling	I2. Inverse Color space transformation and
	Supersampling

Transform each pixel from RGB to YCbCr using the equation below:

$$\begin{pmatrix} Y \\ Cb \\ Cr \end{pmatrix} = \begin{bmatrix} 0.2990 & 0.5870 & 0.1140 \\ -0.1687 & -0.3313 & 0.5000 \\ 0.5000 & -0.4187 & -0.0813 \end{bmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix}$$

Initially, RGB value ranges from 0 and 255. After color transformation, Y should range from 0 to 255, while Cb and Cr should range from -127.5 to 127.5. (*Truncate if necessary*.)

Subtract 128 from Y and 0.5 from Cb and Cr so that they span the same range of values [-128,127]

Subsample Cb and Cr using 4:2:0 (MPEG1) chrominance subsampling scheme. *If* Cb(Cr) *is not divisible by 8, pad with zeros.* 

Supersample Cb and Cr so that each pixel has Cb and Cr. This means that one Cb will be used for 4 Y values.

Add 128 to the values of the Y component and 0.5 to the values of the Cb and Cr components.

If using a color image, transform from the YCbCr space to the RGB space according to the following equation:

$$\begin{pmatrix} R \\ G \\ B \end{pmatrix} = \begin{bmatrix} 1.0000 & 0 & 1.4020 \\ 1.0000 & -0.3441 & -0.7141 \\ 1.0000 & 1.7720 & 0 \end{bmatrix} \begin{pmatrix} Y \\ Cb \\ Cr \end{pmatrix}$$

Common mistake: After this step, you have to make sure that the resulting RGB values are in the range between 0 and 255. Truncate if necessary.

### F3. Discrete Cosine Transform

Perform the DCT for Y image using the following steps:

- Divide the image into 8x8 blocks. Scan each block in the image in raster order (left to right, top to bottom)
- For each 8x8 block, perform the DCT transform to get the values  $F_{uv}$  from the values  $f_{xy}$ . The elements  $F_{uv}$  range from  $-2^{10}$  to  $2^{10}$ . Check max and min and assign  $-2^{10}$  or  $2^{10}$  for the values outside of the range so that the values range from  $-2^{10}$  to  $2^{10}$ .

Perform the DCT for Cb image and Cr image, too.

### I1. Inverse DCT

Perform the inverse DCT to recover the values  $f_{xy}$  from the values  $F_{uv}$  and recover Y, Cb, Cr images.

#### DCT Formula

$$F_{uv} = \frac{1}{4} C_u C_v \sum_{x=0}^{7} \sum_{y=0}^{7} f_{xy} \cos \frac{(2x+1)u\pi}{16} \cos \frac{(2y+1)v\pi}{16}$$

 $C_u = 1/\sqrt{2}$  for u = 0,  $C_u = 1$  otherwise.  $C_v = 1/\sqrt{2}$  for v = 0,  $C_v = 1$  otherwise.  $f_{xy}$  is the x-th row and y-th column pixel of the 8x8 image block (x and y range from 0 to 7). The element  $F_{uv}$  is DCT coefficient value in the u-th row and v-th column after DCT transformation. (u and v range from 0 to 7).

#### The inverse DCT Formula

$$f'_{xy} = \frac{1}{4} \sum_{u=0}^{7} \sum_{v=0}^{7} C_u C_v F'_{uv} \cos \frac{(2x+1)u\pi}{16} \cos \frac{(2y+1)v\pi}{16}$$