

ADCA-12  
2<sup>nd</sup> Year Examination, Academic Batch 2016-17  
Discrete Mathematics

Time : 3 Hours ]

[ Max. Marks : 100

*Note. Attempt any **five** questions. Each questions carry equal marks.*

- Q.1.(a) Show that inverse of an element  $a$  in a group  $G$  is unique.  
(b) Every subgroup of a cyclic group is cyclic.

**Q2.** Differentiate between the following with truth table:

- (a) Disjunction vs. Conjunction  
(b) Conditional vs. Bi- Conditional  
(c) Tautology vs. Contradiction:

- Q3.** (a) Explain “AND, “OR” & NOT operators with logic diagram and truth table.  
(b) Define the term ‘MINTERM’.  
(c) Define the term ‘MAXTERM’

**Q.4.** Let  $T:V \rightarrow W$  be a linear transformation. Then  $T$  is onto iff  $\rho(T) = \dim W$ .

**Q.5.** Write short notes on: [any four]

- (1) path and circuit (2) Planar graph (3) Binary tree  
(4) Multigraph (5) Tree.

**Q.6.** Write Short notes on: [Any Four]

- (i) Connected graph (ii) regular graph (iii) Weighted graph (iv) Rooted Trees  
(v) Sub- graph

**Q 7** (a) consider the set  $M$  of all  $2 \times 2$  matrices of the type  $\begin{bmatrix} x & -y \\ y & -x \end{bmatrix}$  where  $x, y$  are the conjugates of  $x$  and  $y$ . Is  $M$  a field?

- (b) Prove that  $G = \{ 1, 2, 3, 4, 5, 6 \}$  is a finite abelian group of order 6 under multiplication modulo 7.

**Q.8.** Explain the application of graph.