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B.Sc.(PCM)-10, B.A. (Math)-4
2nd Year Examination, Academic Batch 2016-17
Mathematics-V (Special Function an Mechanics)

Time : 3 Hours]

[Max. Marks : 100

*Note. Attempt any **five** questions. Each questions carry equal marks.*

- Q.1** Prove that [20]

$$\int_{-1}^1 x^2 p_{n+1} p_{n-1} dx = \frac{2n(n+1)}{(2n-1)(2n+1)(2n+3)}$$
- Q.2** Solve [20]

$$\frac{d^2 y}{y t^2} + y = 0$$
 Under the condition that $y = 1, \frac{dy}{dx} = 0$
- Q.3** If the radial and transverse velocities of a particle are always proportional to each other, [20]
 show that the path is an equiangular spiral.
- Q.4** Prove that the acceleration of a point moving in a curve with uniform speed is [20]

$$e \left(\frac{dx}{dt} \right)^2$$
- Q.5** Find the complete integral of $2zx - px^2 - 2qxy + pq = 0$ [20]
- Q.6** Show that $f_n(x)$ is even and odd function for even n and for odd n respectively. [20]
- Q.7** Solve [20]

$$z^2 (p^2 + q^2) = x^2 + y^2$$
- Q.8** Find the laplace transform of the function $3 \cosh 5t - 4 \sinh 5t$ [20]