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B.Sc.(PCM)-18, B.A.(Math)-6
3rd Year Examination, Academic Batch 2015-16
Mathematics-VI

Time : 3 Hours]

[Max. Marks : 100

Note. Attempt any five questions. All questions carry equal marks.

- Q.1 (a)** A field has no proper ideals. [20]
(b) Every field is an Euclidean ring.
- Q.2 (a)** Every field is an integral domain? [20]
(b) The intersection of two sub rings is again a sub ring
- Q.3 (a)** Prove that the vectors $(2, -1, 4), (1, -1, 2), (3, 1, -2)$ form a basis for \mathbb{R}^3 [10]
(b) Prove that the vectors $(1, 1, 0), (3, 1, 3)$ and $(5, 3, 3)$ are linearly dependent.
- Q.4** Show that the mapping $d: \mathbb{R}^2 \times \mathbb{R}^2 \rightarrow \mathbb{R}$ defined by $d(x, y) = \max\{|x_1 - y_1|, |x_2 - y_2|\}$ where $x = (x_1, x_2), y = (y_1, y_2) \in \mathbb{R}^2$ is metric on \mathbb{R}^2 [20]
- Q.5** Let A and B be subset of a matrix space X. then [20]
(i) $A \subset B \Rightarrow D(A) \subset D(B)$
(ii) $D(A \cap B) \subset D(A) \cap D(B)$
(iii) $D(A \cup B) = D(A) \cup D(B)$
- Q.6** Find the dual basis of the basis set $B = \{(1, -1, 3), (0, 1, -1), (0, 3, -2)\}$ for $V_3(\mathbb{R})$ [20]
- Q.7** If the matrix of a linear transformation T on a vector space $V_2(\mathbb{C})$ w.r.t. the ordered basis $B = \{(1, 0), (0, 1)\}$ is $\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ what is the matrix of T w.r.t. the ordered basis $B = \{(1, 1), (1, -1)\}$? [20]
- Q.8 (a)** The intersection of any two subspaces of a vector space is a subspace. [20]
(b) Is the vector $(2, -5, 3)$ in the subspace of \mathbb{R}^3 spanned by the vectors $(1, -3, 2), (2, -4, -1), (1, -5, 7)$.