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**B.Sc. (PCM)-2, B.A. (Math)-2**  
**1<sup>st</sup> Year Examination, Calendar Batch 2017**  
**Mathematics-2 (Geometry & Calculus)**

Time : 3 Hours ]

[ Max. Marks : 100

*Note. Attempt any five questions. Each questions carry equal marks.*

**Q.1.** Prove that the functions  $1, x, x^2$  are linearly independent. Hence form the differential equation whose roots are  $1, x, x^2$ .

**Q.2.** Find the equation of the plane passing through the points  $(1, -1, 2)$  and  $(2, -2, 2)$  and which is perpendicular to the plane

$$6x - 2y + 2z = 9$$

**Q.3.** Find the projection of the line  $3x - y + 2z - 1 = 0, x + 2y - z = 2$  on the plane  $3x + 2y + z = 0$ .

**Q.4.** Find the shortest distance between the lines

$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}; \frac{x-2}{3} = \frac{y-4}{4} = \frac{z-5}{5}$$

**Q.5.** Find the equation to the cone whose vertex is the point  $(a, b, c)$  and whose generating lines intersects the conic  $px^2 + qy^2 = 1, z = 0$ .

**Q.6.** Find the common area between the curve

$$y^2 = 4ax \text{ and } x^2 = 4ay.$$

**Q.7.** Evaluate  $\log_{x+\frac{\pi}{2}}(\sec x - \tan x)$ .

**Q.8.** Find the whole length of the astroid

$$x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}} \text{ or}$$

$$x = a \cos^3 \theta, \quad y = a \sin^3 \theta.$$