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B.Sc. (PCM)-1, B.A. (Math)-1
1st Year Examination, Calendar Batch 2017
Mathematics-1 (Algebra, Trigonometry & Vectors)

Time : 3 Hours]

[Max. Marks : 100

*Note. Attempt any **five** questions. Each questions carry equal marks.*

Q.1. Use matrix method to solve the equation-
 $2x-y+3z=9$, $x+y+z=6$, $x-y+z=2$

Q.2. Prove that $[a + b, b + c, c + a] = 2[a \ b \ c]$.

Q.3. If $(G,*)$ be a group ,then the inverse of each element of G is unique.

Q.4. Show that every finite group G is isomorphic to a permutation group

Q.5. If $u = \log \tan \left(\frac{\pi}{4} + \frac{\theta}{2} \right)$, prove that $\tanh \frac{u}{2} = \tan \frac{\theta}{2}$.

Q.6. Prove that the $\text{div} (\text{curl } V) = 0$.

Q.7. Show that the set Z of all integers form a group with respect to binary operation $*$ defined by $a * b = a + b + 1$ for all $a, b \in Z$ is an abelian group.

Q.8. determine the rank of the matrix

$$\begin{vmatrix} 1 & 2 & 3 \\ 3 & 4 & 5 \\ 4 & 5 & 6 \end{vmatrix}$$