CHAPTER-5

Squares and Square Roots

1Mark Q&A

Exercise 5.1

- 1. What will be the unit digit of the squares of the following numbers?
- i. 81
- ii. 272
- iii. 799
- iv. 3853
- v. 1234
- vi. 26387
- vii. 52698
- viii. 99880
- ix. 12796
- x. 55555

Solution:

The unit digit of square of a number having 'a' at its unit place ends with $a \times a$.

- i. The unit digit of the square of a number having digit 1 as unit's place is 1.
- : Unit digit of the square of number 81 is equal to 1.
- ii. The unit digit of the square of a number having digit 2 as unit's place is 4.
- : Unit digit of the square of number 272 is equal to 4.
- iii. The unit digit of the square of a number having digit 9 as unit's place is 1.
- : Unit digit of the square of number 799 is equal to 1.
- iv. The unit digit of the square of a number having digit 3 as unit's place is 9.
- : Unit digit of the square of number 3853 is equal to 9.
- v. The unit digit of the square of a number having digit 4 as unit's place is 6.
- : Unit digit of the square of number 1234 is equal to 6.
- vi. The unit digit of the square of a number having digit 7 as unit's place is 9.
- : Unit digit of the square of number 26387 is equal to 9.
- vii. The unit digit of the square of a number having digit 8 as unit's place is 4.
- : Unit digit of the square of number 52698 is equal to 4.

viii. The unit digit of the square of a number having digit 0 as unit's place is 01.

- : Unit digit of the square of number 99880 is equal to 0.
- ix. The unit digit of the square of a number having digit 6 as unit's place is 6.
- : Unit digit of the square of number 12796 is equal to 6.
- x. The unit digit of the square of a number having digit 5 as unit's place is 5.
- : Unit digit of the square of number 55555 is equal to 5.
- 2. The following numbers are obviously not perfect squares. Give reason.
- i. 1057
- ii. 23453
- iii. 7928
- iv. 222222
- v. 64000
- vi. 89722
- vii. 222000
- viii. 505050

Solution:

We know that natural numbers ending in the digits 0, 2, 3, 7 and 8 are not perfect squares.

i. $1057 \Longrightarrow \text{Ends with } 7$

ii. $23453 \Rightarrow \text{Ends with } 3$

iii. $7928 \Longrightarrow \text{Ends with } 8$

iv. $222222 \Rightarrow$ Ends with 2

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v. $64000 \Longrightarrow \text{Ends with } 0$

vi. $89722 \implies \text{Ends with } 2$

vii. $222000 \Rightarrow$ Ends with 0

viii. $505050 \implies \text{Ends with } 0$

3. The squares of which of the following would be odd numbers?

i. 431

ii. 2826

iii. 7779

iv. 82004

Solution:

We know that the square of an odd number is odd and the square of an even number is even.

i. The square of 431 is an odd number.

- ii. The square of 2826 is an even number.
- iii. The square of 7779 is an odd number.
- iv. The square of 82004 is an even number.
- 4. Observe the following pattern and find the missing numbers. $11^2 = 121$

$$101^2 = 10201$$

$$1001^2 = 1002001$$

$$100001^2 = 1 \dots 2 \dots 1$$

$$10000001^2 = \dots$$

Solution:

We observe that the square on the number on R.H.S of the equality has an odd number of digits such that the first and last digits both are 1 and middle digit is 2. And the number of zeros between left most digits 1 and the middle digit 2 and right most digit 1 and the middle digit 2 is same as the number of zeros in the given number.

$$\therefore 100001^2 = 10000200001$$

$$10000001^2 = 100000020000001$$

5. Observe	the following	pattern and	supply the	missing	numbers.
112 = 121					

1012 = 10201

101012 = 102030201

10101012 =

 $\dots 2 = 10203040504030201$

Solution:

We observe that the square on the number on R.H.S of the equality has an odd number of digits such that the first and last digits both are 1. And, the square is symmetric about the middle digit. If the middle digit is 4, then the number to be squared is 10101 and its square is 102030201.

So, 10101012 = 1020304030201

1010101012 = 10203040505030201

6. Using the given pattern, find the missing numbers. $1^2 + 2^2 + 2^2 = 3^2$

$$2^2 + 3^2 + 6^2 = 7^2$$

$$3^2 + 4^2 + 12^2 = 13^2$$

$$4^2 + 5^2 + 2 = 21^2$$

$$5 + _{2}^{2} + 30^{2} = 31^{2}$$

$$6 + 7 + _{2}^{2} = _{2}^{2}$$

Solution:

Given,
$$1^2 + 2^2 + 2^2 = 3^2$$

i.e.
$$1^2 + 2^2 + (1 \times 2)^2 = (1^2 + 2^2 - 1 \times 2)^2$$

$$2^2 + 3^2 + 6^2 = 7^2$$

$$\therefore 2^2 + 3^2 + (2 \times 3)^2 = (2^2 + 3^2 - 2 \times 3)^2$$

$$3^2 + 4^2 + 12^2 = 13^2$$

$$\therefore 3^2 + 4^2 + (3 \times 4)^2 = (3^2 + 4^2 - 3 \times 4)^2$$

$$4^2 + 5^2 + (4 \times 5)^2 = (4^2 + 5^2 - 4 \times 5)^2$$

$$\therefore 4^2 + 5^2 + 20^2 = 21^2$$

$$5^2 + 6^2 + (5 \times 6)^2 = (5^2 + 6^2 - 5 \times 6)^2$$

$$\therefore 5^2 + 6^2 + 30^2 = 31^2$$

$$6^2 + 7^2 + (6 \times 7)^2 = (6^2 + 7^2 - 6 \times 7)^2$$

$$\therefore 6^2 + 7^2 + 42^2 = 43^2$$

7. Without adding, find the sum.

i.
$$1+3+5+7+9$$

Solution:

Sum of first five odd number = $(5)^2 = 25$

ii.
$$1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19$$

Solution:

Sum of first ten odd number = $(10)^2 = 100$

iii.
$$1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21 + 23$$

Solution:

Sum of first thirteen odd number = $(12)^2 = 144$

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8. (i) Express 49 as the sum of 7 odd numbers.

Solution:

We know, sum of first n odd natural numbers is n^2 . Since, $49 = 7^2$

 \therefore 49 = sum of first 7 odd natural numbers = 1 + 3 + 5 + 7 + 9 + 11 + 13

(ii) Express 121 as the sum of 11 odd numbers.

Solution:

Since, $121 = 11^2$

 \therefore 121 = sum of first 11 odd natural numbers = 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21

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- 9. How many numbers lie between squares of the following numbers?
- i. 12 and 13
- ii. 25 and 26
- iii. 99 and 100

Solution:

Between n^2 and $(n+1)^2$, there are 2n non-perfect square numbers.

- i. 122 and 132 there are $2 \times 12 = 24$ natural numbers.
- ii. 252 and 262 there are $2 \times 25 = 50$ natural numbers.
- iii. 992 and 1002 there are $2 \times 99 = 198$ natural numbers.

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Exercise 5.2

1. Find the square of the following numbers.

- i. 32
- ii. 35
- iii. 86
- iv. 93
- v. 71
- vi. 46

Solution:

i.
$$(32)^2$$

$$=(30+2)^2$$

=
$$(30)^2 + (2)^2 + 2 \times 30 \times 2$$
 [Since, $(a+b)^2 = a^2 + b^2 + 2ab$]

$$=900 + 4 + 120$$

$$= 1024$$

132

$$=(30+5)^2$$

=
$$(30)^2 + (5)^2 + 2 \times 30 \times 5$$
 [Since, $(a+b)^2 = a^2 + b^2 + 2ab$]

$$=900 + 25 + 300$$

iii.
$$(86)^2$$

= $(90-4)^2$
= $(90)^2 + (4)^2 - 2 \times 90 \times 4$ [Since, $(a+b)^2 = a^2 + b^2 + 2ab$]
= $8100 + 16 - 720$
= $8116 - 720$
= 7396
iv. $(93)^2$
= $(90+3)^2$
= $(90)^2 + (3)^2 + 2 \times 90 \times 3$ [Since, $(a+b)^2 = a^2 + b^2 + 2ab$]
= $8100 + 9 + 540$
= 8649
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v. $(71)^2$
= $(70+1)^2$
= $(70)^2 + (1)^2 + 2 \times 70 \times 1$ [Since, $(a+b)^2 = a^2 + b^2 + 2ab$]
= $4900 + 1 + 140$
= 5041

vi. (46)²

$$=(50-4)^2$$

=
$$(50)^2 + (4)^2 - 2 \times 50 \times 4$$
 [Since, $(a+b)^2 = a^2 + b^2 + 2ab$]

$$= 2500 + 16 - 400$$

$$= 2116$$

- 2. Write a Pythagorean triplet whose one member is.
- i. 6
- ii. 14
- iii. 16
- iv. 18

Solution:

For any natural number m, we know that 2m, m2-1, m2+1 is a Pythagorean triplet.

i.
$$2m = 6$$

$$\Rightarrow$$
 m = 6/2 = 3

$$m2-1=32-1=9-1=8$$

$$m2+1=32+1=9+1=10$$

 \therefore (6, 8, 10) is a Pythagorean triplet.

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ii.
$$2m = 14$$

 \Rightarrow m = 14/2 = 7

m2-1=72-1=49-1=48

m2+1 = 72+1 = 49+1 = 50

∴ (14, 48, 50) is not a Pythagorean triplet.

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iii. 2m = 16

 \Rightarrow m = 16/2 = 8

m2-1 = 82-1 = 64-1 = 63

m2+1 = 82+1 = 64+1 = 65

 \therefore (16, 63, 65) is a Pythagorean triplet.

iv. 2m = 18

 \Rightarrow m = 18/2 = 9

m2-1 = 92-1 = 81-1 = 80

m2+1 = 92+1 = 81+1 = 82

∴ (18, 80, 82) is a Pythagorean triplet.

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5Mark Q&A

Exercise 5.3

- 1. What could be the possible 'one's' digits of the square root of each of the following numbers?
- i. 9801
- ii. 99856
- iii. 998001
- iv. 657666025

Solution:

i. We know that the unit's digit of the square of a number having digit as unit's

Place 1 is 1 and also 9 is $1[9^2=81$ whose unit place is 1].

- : Unit's digit of the square root of number 9801 is equal to 1 or 9.
- ii. We know that the unit's digit of the square of a number having digit as unit's

Place 6 is 6 and also 4 is 6 $[6^2=36 \text{ and } 4^2=16, \text{ both the squares have unit digit 6}].$

- : Unit's digit of the square root of number 99856 is equal to 6.
- iii. We know that the unit's digit of the square of a number having digit as unit's

Place 1 is 1 and also 9 is $1[9^2=81$ whose unit place is 1].

- : Unit's digit of the square root of number 998001 is equal to 1 or 9.
- iv. We know that the unit's digit of the square of a number having digit as unit's

Place 5 is 5.

- : Unit's digit of the square root of number 657666025 is equal to 5.
- 2. without doing any calculation, find the numbers which are surely not perfect squares.
- i. 153
- ii. 257
- iii. 408
- iv. 441

Solution:

We know that natural numbers ending with the digits 0, 2, 3, 7 and 8 are not perfect square.

- i. $153 \Rightarrow$ Ends with 3.
- ∴, 153 is not a perfect square
- ii. $257 \Longrightarrow$ ends with 7
- ∴, 257 is not a perfect square
- iii. $408 \Longrightarrow$ ends with 8
- ∴, 408 is not a perfect square

iv. $441 \Longrightarrow$ ends with 1

 \therefore , 441 is a perfect square.

3. Find the square roots of 100 and 169 by the method of repeated subtraction.

Solution:

100

$$100 - 1 = 99$$

$$99 - 3 = 96$$

$$96 - 5 = 91$$

$$91 - 7 = 84$$

$$84 - 9 = 75$$

$$75 - 11 = 64$$

$$64 - 13 = 51$$

$$51 - 15 = 36$$

$$36 - 17 = 19$$

$$19 - 19 = 0$$

Here, we have performed subtraction ten times.

∴
$$\sqrt{100} = 10$$

169

$$169 - 1 = 168$$

$$168 - 3 = 165$$

$$165 - 5 = 160$$

$$160 - 7 = 153$$

$$153 - 9 = 144$$

$$144 - 11 = 133$$

$$133 - 13 = 120$$

$$120 - 15 = 105$$

$$105 - 17 = 88$$

$$88 - 19 = 69$$

$$69 - 21 = 48$$

$$48 - 23 = 25$$

$$25 - 25 = 0$$

Here, we have performed subtraction thirteen times.

$$1.0 \cdot 100 = 13$$

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4. Find the square roots of the following numbers by the Prime Factorisation Method.

- i. 729
- ii. 400
- iii. 1764

iv. 4096

v. 7744

vi. 9604

vii. 5929

viii. 9216

ix. 529

x. 8100

Solution:

i.

3

1

$$729 = 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 1$$

$$\Rightarrow 729 = (3 \times 3) \times (3 \times 3) \times (3 \times 3)$$

$$\Rightarrow 729 = (3 \times 3 \times 3) \times (3 \times 3 \times 3)$$

$$\Rightarrow 729 = (3 \times 3 \times 3)^2$$

$$\Rightarrow \sqrt{729} = 3 \times 3 \times 3 = 27$$

ii.

$$400 = 2 \times 2 \times 2 \times 2 \times 5 \times 5 \times 1$$

$$\Rightarrow 400 = (2 \times 2) \times (2 \times 2) \times (5 \times 5)$$

$$\Rightarrow 400 = (2 \times 2 \times 5) \times (2 \times 2 \times 5)$$

$$\Rightarrow 400 = (2 \times 2 \times 5)^2$$

$$\Rightarrow \sqrt{400} = 2 \times 2 \times 5 = 20$$

iii.

$$1764 = 2 \times 2 \times 3 \times 3 \times 7 \times 7$$

$$\Rightarrow$$
 1764 = (2×2) × (3×3) × (7×7)

$$\Rightarrow$$
 1764 = (2×3×7) × (2×3×7)

$$\Rightarrow 1764 = (2 \times 3 \times 7)^2$$

$$\Rightarrow \sqrt{1764} = 2 \times 3 \times 7 = 42$$

iv.

$$\Rightarrow 4096 = (2 \times 2) \times (2 \times 2)$$

$$\Rightarrow 4096 = (2 \times 2 \times 2 \times 2 \times 2 \times 2) \times (2 \times 2 \times 2 \times 2 \times 2 \times 2)$$

$$\Rightarrow 4096 = (2 \times 2 \times 2 \times 2 \times 2 \times 2)^{2}$$

$$\Rightarrow \sqrt{4096} = 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 64$$

v.

 $7744 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 11 \times 11 \times 1$

$$\Rightarrow$$
 7744 = (2×2) × (2×2) × (2×2) × (11×11)

$$\Rightarrow$$
 7744 = (2×2×2×11) × (2×2×2×11)

$$\Rightarrow$$
 7744 = $(2 \times 2 \times 2 \times 11)^2$

$$\Rightarrow \sqrt{7744} = 2 \times 2 \times 2 \times 11 = 88$$

vi.

$$9604 = 62 \times 2 \times 7 \times 7 \times 7 \times 7$$

$$\Rightarrow 9604 = (2 \times 2) \times (7 \times 7) \times (7 \times 7)$$

$$\Rightarrow$$
 9604 = (2 × 7 × 7) × (2 × 7 × 7)

$$\Rightarrow$$
 9604 = $(2 \times 7 \times 7)^2$

$$\Rightarrow \sqrt{9604} = 2 \times 7 \times 7 = 98$$

vii.

$$5929 = 7 \times 7 \times 11 \times 11$$

$$\Rightarrow 5929 = (7 \times 7) \times (11 \times 11)$$

$$\Rightarrow 5929 = (7 \times 11) \times (7 \times 11)$$

$$\Rightarrow 5929 = (7 \times 11)^2$$

$$\Rightarrow \sqrt{5929} = 7 \times 11 = 77$$

Viii.

- 2 9216 2 4608 2 2304
- 2 1152
- 2 576
- 2 288
- 2 144
- 2 72
- 2 36
- 2 18
- 3 9
- 3 3

$$\Rightarrow 9216 = (2 \times 2) \times (3 \times 3)$$

$$\Rightarrow 9216 = (\ 2 \times 2 \times 2 \times 2 \times 2 \times 3) \times (\ 2 \times 2 \times 2 \times 2 \times 2 \times 3)$$

$$\Rightarrow$$
 9216 = 96 \times 96

$$\Rightarrow$$
 9216 = $(96)^2$

$$\Rightarrow \sqrt{9216} = 96$$

ix.

$$529 = 23 \times 23$$

$$529 = (23)^2$$

$$\sqrt{529} = 23$$

X.

2	8100
2	4050
3	2025
3	675
3	225
3	75
5	25
5	5
	1

$$8100 = 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 5 \times 5 \times 1$$

$$\Rightarrow 8100 = (2 \times 2) \times (3 \times 3) \times (3 \times 3) \times (5 \times 5)$$

$$\Rightarrow 8100 = (2 \times 3 \times 3 \times 5) \times (2 \times 3 \times 3 \times 5)$$

$$\Rightarrow 8100 = 90 \times 90$$

$$\Rightarrow 8100 = (90)^2$$

$$\Rightarrow \sqrt{8100} = 90$$

5. For each of the following numbers, find the smallest whole number by which it should be multiplied so as to get a perfect square number. Also find the square root of the square number so obtained.

- i. 252
- ii. 180
- iii. 1008
- iv. 2028
- v. 1458
- vi. 768

Solution:

i.

2	252
2	126
3	63
3	21
7	7
	1

$$252 = 2 \times 2 \times 3 \times 3 \times 7$$

$$=(2\times2)\times(3\times3)\times7$$

Here, 7 cannot be paired.

∴ We will multiply 252 by 7 to get perfect square.

New number = $252 \times 7 = 1764$

$$1764 = 2 \times 2 \times 3 \times 3 \times 7 \times 7$$

$$\Rightarrow 1764 = (2 \times 2) \times (3 \times 3) \times (7 \times 7)$$

$$\Rightarrow 1764 = 2^2 \times 3^2 \times 7^2$$

$$\Rightarrow 1764 = (2 \times 3 \times 7)^2$$

$$\Rightarrow \sqrt{1764} = 2 \times 3 \times 7 = 42$$

ii.

$$180 = 2 \times 2 \times 3 \times 3 \times 5$$

$$= (2 \times 2) \times (3 \times 3) \times 5$$

Here, 5 cannot be paired.

∴ We will multiply 180 by 5 to get perfect square.

New number = $180 \times 5 = 900$

2	900
2	450
3	225
3	75
5	25
5	5
	1

$$900 = 2 \times 2 \times 3 \times 3 \times 5 \times 5 \times 1$$

$$\Rightarrow 900 = (2 \times 2) \times (3 \times 3) \times (5 \times 5)$$

$$\Rightarrow 900 = 2^2 \times 3^2 \times 5^2$$

$$\Rightarrow 900 = (2 \times 3 \times 5)^2$$

$$\Rightarrow \sqrt{900} = 2 \times 3 \times 5 = 30$$

iii.

2	1008
2	504
2	252
2	126
3	63
3	21
7	7
	1

$$1008 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7$$

$$= (2\times2)\times(2\times2)\times(3\times3)\times7$$

Here, 7 cannot be paired.

∴ We will multiply 1008 by 7 to get perfect square.

New number = $1008 \times 7 = 7056$

$$7056 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7 \times 7$$

$$\Rightarrow$$
 7056 = (2×2) × (2×2) × (3×3) × (7×7)

$$\Rightarrow$$
 7056 = $2^2 \times 2^2 \times 3^2 \times 7^2$

$$\Rightarrow 7056 = (2 \times 2 \times 3 \times 7)^2$$

$$\Rightarrow \sqrt{7056} = 2 \times 2 \times 3 \times 7 = 84$$

iv.

2	2028
2	1014
3	507
13	169
13	13
	1

$$2028 = 2 \times 2 \times 3 \times 13 \times 13$$

$$= (2 \times 2) \times (13 \times 13) \times 3$$

Here, 3 cannot be paired.

: We will multiply 2028 by 3 to get perfect square. New number = $2028 \times 3 = 6084$

2	6084
2	3042
3	1521
3	507
13	169
13	13
	1

$$6084 = 2 \times 2 \times 3 \times 3 \times 13 \times 13$$

$$\Rightarrow 6084 = (2 \times 2) \times (3 \times 3) \times (13 \times 13)$$

$$\Rightarrow 6084 = 2^2 \times 3^2 \times 13^2$$

$$\Rightarrow 6084 = (2 \times 3 \times 13)^2$$

$$\Rightarrow \sqrt{6084} = 2 \times 3 \times 13 = 78$$

v.

2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

$$1458 = 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3$$

$$= (3 \times 3) \times (3 \times 3) \times (3 \times 3) \times 2$$

Here, 2 cannot be paired.

: We will multiply 1458 by 2 to get perfect square. New number = 1458 \times 2 = 2916

2	2916
2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

$$2916 = 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3$$

$$\Rightarrow$$
 2916 = (3×3)×(3×3)×(3×3)×(2×2)

$$\Rightarrow 2916 = 3^2 \times 3^2 \times 3^2 \times 2^2$$

$$\Rightarrow 2916 = (3 \times 3 \times 3 \times 2)^2$$

$$\Rightarrow \sqrt{2916} = 3 \times 3 \times 3 \times 2 = 54$$

vi.

2	768
2	384
2	192
2	96
2	48
2	24
2	12
2	6
3	3
	1

$$768 = 2 \times 3$$

$$= (2\times2)\times(2\times2)\times(2\times2)\times(2\times2)\times3$$

Here, 3 cannot be paired.

∴ We will multiply 768 by 3 to get perfect square.

New number = $768 \times 3 = 2304$

2	2304
2	1152
2	576
2	288
2	144
2	72
2	36
2	18
3	9
3	3
	1

$$2304 = 2 \times 3 \times 3$$

$$\Rightarrow 2304 = (2 \times 2) \times (2 \times 2) \times (2 \times 2) \times (2 \times 2) \times (3 \times 3)$$

$$\Rightarrow 2304 = 2^2 \times 2^2 \times 2^2 \times 2^2 \times 3^2$$

$$\Rightarrow 2304 = (2 \times 2 \times 2 \times 2 \times 3)^2$$

$$\Rightarrow \sqrt{2304} = 2 \times 2 \times 2 \times 2 \times 3 = 48$$

6. For each of the following numbers, find the smallest whole number by which it should be divided so as to get a perfect square. Also find the square root of the square number so obtained.

- i. 252
- ii. 2925
- iii. 396
- iv. 2645
- v. 2800
- vi. 1620

Solution:

i.

2	252
2	126
3	63
3	21
7	7
	1

$$252 = 2 \times 2 \times 3 \times 3 \times 7$$

$$= (2 \times 2) \times (3 \times 3) \times 7$$

Here, 7 cannot be paired.

 \therefore We will divide 252 by 7 to get perfect square. New number = $252 \div 7$ = 36

$$36 = 2 \times 2 \times 3 \times 3$$

$$\Rightarrow 36 = (2 \times 2) \times (3 \times 3)$$

$$\Rightarrow 36 = 2^2 \times 3^2$$

$$\Rightarrow 36 = (2 \times 3)^2$$

$$\Rightarrow \sqrt{36} = 2 \times 3 = 6$$

ii.

3	2925
3	975
5	325
5	65
13	13
	1

$$2925 = 3 \times 3 \times 5 \times 5 \times 13$$

$$= (3\times3)\times(5\times5)\times13$$

Here, 13 cannot be paired.

∴ We will divide 2925 by 13 to get perfect square. New number = 2925 \div 13 = 225

3	225
3	75
5	25
5	5
	1

$$225 = 3 \times 3 \times 5 \times 5$$

$$\Rightarrow$$
 225 = (3×3)×(5×5)

$$\Rightarrow 225 = 3^2 \times 5^2$$

$$\Rightarrow 225 = (3 \times 5)^2$$

$$\Rightarrow \sqrt{36} = 3 \times 5 = 15$$

iii.

$$396 = 2 \times 2 \times 3 \times 3 \times 11$$

$$= (2 \times 2) \times (3 \times 3) \times 11$$

Here, 11 cannot be paired.

 \therefore We will divide 396 by 11 to get perfect square. New number = 396 \div 11 = 36

2	36
2	18
3	9
3	3
	1

$$36 = 2 \times 2 \times 3 \times 3$$

$$\Rightarrow$$
 36 = (2×2) × (3×3)

$$\Rightarrow$$
 36 = $2^2 \times 3^2$

$$\Rightarrow 36 = (2 \times 3)^2$$

$$\Rightarrow \sqrt{36} = 2 \times 3 = 6$$

iv.

$$2645 = 5 \times 23 \times 23$$

$$\Rightarrow$$
 2645 = (23×23)×5

Here, 5 cannot be paired.

∴ We will divide 2645 by 5 to get perfect square.

New number = $2645 \div 5 = 529$

$$529 = 23 \times 23$$

$$\Rightarrow 529 = (23)^2$$

$$\Rightarrow \sqrt{529} = 23$$

V.

2	2800
2	1400
2	700
2	350
5	175
5	35
7	7
	1

$$2800 = 2 \times 2 \times 2 \times 2 \times 5 \times 5 \times 7$$

$$= (2 \times 2) \times (2 \times 2) \times (5 \times 5) \times 7$$

Here, 7 cannot be paired.

 \therefore We will divide 2800 by 7 to get perfect square. New number = 2800 \div 7 = 400

$$400 = 2 \times 2 \times 2 \times 2 \times 5 \times 5$$

$$\Rightarrow 400 = (2 \times 2) \times (2 \times 2) \times (5 \times 5)$$

$$\Rightarrow 400 = (2 \times 2 \times 5)^2$$

$$\Rightarrow \sqrt{400} = 20$$

vi.

2	1620
2	810
3	405
3	135
3	45
3	15
5	5
	1

$$1620 = 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 5$$

$$= (2 \times 2) \times (3 \times 3) \times (3 \times 3) \times 5$$

Here, 5 cannot be paired.

: We will divide 1620 by 5 to get perfect square. New number = $1620 \div 5 = 324$

2	324
2	162
3	81
3	27
3	9
3	3
	1

$$324 = 2 \times 2 \times 3 \times 3 \times 3 \times 3$$

$$\Rightarrow 324 = (2 \times 2) \times (3 \times 3) \times (3 \times 3)$$

$$\Rightarrow 324 = (2 \times 3 \times 3)^2$$

$$\Rightarrow \sqrt{324} = 18$$

7. The students of Class VIII of a school donated Rs 2401 in all, for Prime Minister's National Relief Fund. Each student donated as many rupees as the number of students in the class. Find the number of students in the class.

Solution:

Let the number of students in the school be, x.

∴ each student donate Rs.x.

Total amount contributed by all the students= $x \times x = x^2$ given, $x^2 = Rs.2401$

$$x^2 = 7 \times 7 \times 7 \times 7$$

$$\Rightarrow$$
 X2 = (7×7) × (7×7)

$$\Rightarrow x^2 = 49 \times 49$$

$$\Rightarrow x = \sqrt{(49 \times 49)}$$

$$\Rightarrow$$
 x = 49

 \therefore The number of students = 49

121

8. 2025 plants are to be planted in a garden in such a way that each row contains as many plants as the number of rows. Find the number of rows and the number of plants in each row.

Solution

Let the number of rows be, x.

 \therefore the number of plants in each rows = x.

Total plants to be planted in the garden = $x \times x = x^2$

Given,

 $x_2 = Rs.2025$

3	2025
3	675
3	225
3	75
5	25
5	5
	1

$$x^2 = 3 \times 3 \times 3 \times 3 \times 5 \times 5$$

$$\Rightarrow X2 = (3 \times 3) \times (3 \times 3) \times (5 \times 5)$$

$$\Rightarrow$$
 X2 = (3×3×5) ×(3×3×5)

$$\Rightarrow$$
 x2 = 45×45

$$\Rightarrow$$
 x = $\sqrt{45} \times 45$

$$\Rightarrow$$
 x = 45

 \therefore The number of rows = 45 and the number of plants in each rows = 45.

9. Find the smallest square number that is divisible by each of the numbers 4, 9 and 10.

Solution:

L.C.M of 4, 9 and 10 is $(2 \times 2 \times 9 \times 5)$ 180.

$$180 = 2 \times 2 \times 9 \times 5$$

$$=(2\times2)\times3\times3\times5$$

$$= (2 \times 2) \times (3 \times 3) \times 5$$

Here, 5 cannot be paired.

: we will multiply 180 by 5 to get perfect square.

Hence, the smallest square number divisible by 4, 9 and $10 = 180 \times 5 = 900$

10. Find the smallest square number that is divisible by each of the numbers 8, 15 and 20.

Solution:

L.C.M of 8, 15 and 20 is $(2 \times 2 \times 5 \times 2 \times 3)$ 120.

$$120 = 2 \times 2 \times 3 \times 5 \times 2$$

$$=(2\times2)\times3\times5\times2$$

Here, 3, 5 and 2 cannot be paired.

 \therefore We will multiply 120 by (3×5×2) 30 to get perfect square.

Hence, the smallest square number divisible by 8, 15 and $20 = 120 \times 30 = 3600$

Exercise 5.4

- 1. Find the square root of each of the following numbers by Division method.
- i. 2304
- ii. 4489
- iii. 3481
- iv. 529
- v. 3249
- vi. 1369
- vii. 5776
- viii. 7921
- ix. 576
- x. 1024
- xi. 3136
- xii. 900

Solution:

i.

$$\therefore \sqrt{2304} = 48$$

ii.

$$... \sqrt{4489} = 67$$

iii.

$$... \sqrt{3481} = 59$$

iv.

$$\therefore \sqrt{529} = 23$$

v.

$$\therefore \sqrt{3249} = 57$$

vi.

$$1.0 \cdot \sqrt{1369} = 37$$

Vii.

$$\therefore \sqrt{5776} = 76$$

Viii

$$... \sqrt{7921} = 89$$

ix.

∴
$$\sqrt{576} = 24$$

X.

∴
$$\sqrt{1024} = 32$$

xi.

$$\therefore \sqrt{3136} = 56$$

xii.

$$\therefore \sqrt{900} = 30$$

2. Find the number of digits in the square root of each of the following numbers (without any

Calculation).64

- i. 144
- ii. 4489
- iii. 27225
- iv. 390625

Solution:

i.

 $1.0 \cdot \sqrt{144} = 12$

Hence, the square root of the number 144 has 2 digits.

ii.

$$44489 = 67$$

Hence, the square root of the number 4489 has 2 digits.

iii.

$$\sqrt{27225} = 165$$

Hence, the square root of the number 27225 has 3 digits.

iv.

$$\therefore \sqrt{390625} = 625$$

Hence, the square root of the number 390625 has 3 digits.

3. Find the square root of the following decimal numbers.

- i. 2.56
- ii. 7.29
- iii. 51.84
- iv. 42.25
- v. 31.36

Solution:

i.

 $\therefore \sqrt{2.56} = 1.6$

121

ii.

$$... \sqrt{7.29} = 2.7$$

35

iii.

$$... \sqrt{51.84} = 7.2$$

39

iv.

$$42.25 = 6.5$$

$$\therefore \sqrt{31.36} = 5.6$$

4. Find the least number which must be subtracted from each of the following numbers so as to get a perfect square. Also find the square root of the perfect square so obtained.

- i. 402
- ii. 1989
- iii. 3250
- iv. 825
- v. 4000

Solution:

i.

∴ We must subtract 2 from 402 to get a perfect square.

New number = 402 - 2 = 400

$$... \sqrt{400} = 20$$

ii.

	44
4	1989
+4	16
84	389
+4	336
88	53

: We must subtract 53 from 1989 to get a perfect square. New number = 1989 - 53 = 1936

$$1.01936 = 44$$

iii.

∴ We must subtract 1 from 3250 to get a perfect square.

New number = 3250 - 1 = 3249

$$\therefore \sqrt{3249} = 57$$

iv.

∴ We must subtract 41 from 825 to get a perfect square.

New number = 825 - 41 = 784

∴
$$\sqrt{784} = 28$$

- : We must subtract 31 from 4000 to get a perfect square. New number = 4000 31 = 3969
- $\therefore \sqrt{3969} = 63$
- 5. Find the least number which must be added to each of the following numbers so as to get a perfect square. Also find the square root of the perfect square so obtained.
- (i) 525
- (ii) 1750
- (iii) 252
- (iv)1825
- (v)6412

Solution:

(i)

23
525
4
125
129

Here, (22)2 < 525 > (23)2

We can say 525 is (129 - 125) 4 less than (23)2.

 \therefore If we add 4 to 525, it will be perfect square. New number = 525 + 4 = 529

$$... \sqrt{529} = 23$$

(ii)

Here, $(41)2 < 1750 > (42)^2$

We can say 1750 is (164 - 150) 14 less than $(42)^2$.

 \therefore If we add 14 to 1750, it will be perfect square.

New number = 1750 + 14 = 1764

$$1.0 \cdot \sqrt{1764} = 42$$

(iii)

Here, (15)2 < 252 > (16)2

We can say 252 is (156 - 152) 4 less than (16)2.

: If we add 4 to 252, it will be perfect square.

New number = 252 + 4 = 256

$$\therefore \sqrt{256} = 16$$

(iv)

Here, (42)2 < 1825 > (43)2

We can say 1825 is (249 - 225) 24 less than (43)2.

∴ If we add 24 to 1825, it will be perfect square.

New number = 1825 + 24 = 1849

$$1.0 \cdot \sqrt{1849} = 43$$

(v)

Here, (80)2 < 6412 > (81)2

We can say 6412 is (161 - 12) 149 less than (81)2.

∴ If we add 149 to 6412, it will be perfect square.

New number = 6412 + 149 = 656

81	
8	6561
+8	64
161	161
+1	161
162	0

$$... \sqrt{6561} = 81$$

6. Find the length of the side of a square whose area is 441 m2.

Solution:

Let the length of each side of the field = a Then, area of the field = 441 m2

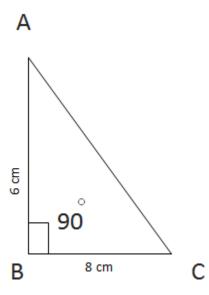
$$\Rightarrow$$
 a2 = 441 m2

$$\Rightarrow$$
a = $\sqrt{441}$ m

- \therefore The length of each side of the field = a m = 21 m.
- 7. In a right triangle ABC, $\angle B = 90^{\circ}$.
- a. If AB = 6 cm, BC = 8 cm, find AC
- b. If AC = 13 cm, BC = 5 cm, find AB

Solution:

a.



Given, AB = 6 cm, BC = 8 cm

Let AC be x cm.

$$\therefore$$
 AC2 = AB2 + BC2

$$AC = \sqrt{AB^2 + BC^2}$$

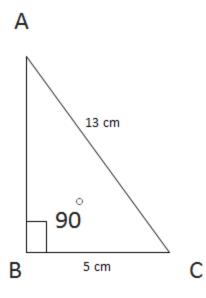
$$= \sqrt{6^2 + 8^2}$$

$$= \sqrt{36 + 64}$$

$$= \sqrt{100} = 10$$

Hence, AC = 10 cm.

b.



Given, AC = 13 cm, BC = 5 cm

Let AB be x cm.

$$\therefore$$
 AC2 = AB2 + BC2

$$\Rightarrow$$
 AC2 – BC2 = AB2

$$AB = \sqrt{AC^2 - BC^2}$$

$$= \sqrt{13^2 - 5^2}$$

$$= \sqrt{169 - 25}$$

$$= \sqrt{144} = 12$$

Hence, AB = 12 cm

8. A gardener has 1000 plants. He wants to plant these in such a way that the number of rows

and the number of columns remain same. Find the minimum number of plants he needs more for this.

Solution:

Let the number of rows and column be, x.

 \therefore Total number of row and column= $x \times x = x2$ As per question, x2 = 1000

$$\Rightarrow$$
 x = $\sqrt{1000}$

$$\begin{array}{c|cccc}
 & 31 \\
\hline
 & \overline{1000} \\
 & +3 & 9 \\
\hline
 & 61 & 100 \\
 & +1 & 61 \\
\end{array}$$

$$\begin{array}{c|cccc}
 & 32 \\
\hline
 & \overline{1000} \\
 & +3 & 9 \\
\hline
 & 62 & 100 \\
 & +2 & 124 \\
\end{array}$$

Here, (31)2 < 1000 > (32)2

We can say 1000 is (124 - 100) 24 less than (32)2.

- ∴ 24 more plants are needed.
- 9. There are 500 children in a school. For a P.T. drill they have to stand in such a manner that the number of rows is equal to number of columns. How many children would be left out in this arrangement.

Solution:

Let the number of rows and column be, x.

∴ Total number of row and column= $x \times x = x2$ As per question, x2 = 500

$$x = \sqrt{500}$$

Hence, 16 children would be left out in the arrangement

1Mark Q&A:

Multiple-choice questions and answers

Exercise 5.5:

- 1. What is the square of 9?
 - A) 18
 - B) 81
 - C) 27
 - D) 72

Answer: B) 81

- 2. What is the square root of 144?
 - A) 12
 - B) 14

C) 10	
D) 16	
Answer: A) 12	
3. Which of the following is a perfect square?	
A) 17	
B) 36	
C) 53	
D) 29	
Answer: B) 36	
4. What is the square of -5?	
A) 25	
B) 5	
C) -25	
D) -5	
Answer A) 25	

A) 7	
B) -7	
C) 14	
D) -14	
Answer: A) 7	
6. Which of the fo	llowing numbers is not a perfect square
A) 64	
B) 81	
C) 100	
D) 90	
Answer: D) 90	
7. What is the squ	are root of 169?
A) 13	
B) 14	
C) 15	
D) 12	

Answer: A) 13 8. If $y^2 = 25$, what are the possible values of y? A) 5 and -5 B) 25 and 5 C) 10 and -10 D) 5 and 10 Answer: A) 5 and -5 9. What is the square of 11? A) 121 B) 112 C) 132 D) 111 Answer: A) 121 10. If the square of a number is 36, what are the possible values of the number? A) 6 and -6

D) 6 and 12

Answer: A) 6 and -6

Exercise 5.6:

Fill in the blanks:

- a) The square of 7 is____.
- b) If $x^2 = 25$, then $x = ____.$
- c) The square root of 144 is_____
- d) The square of a number is always____ or positive.
- e) If $y^2 = 81$, then $y = ____.$
- f) The square root of 64 is_____.
- g) The square of 10 is equal to_____.
- h) If $z^2 = 36$, then $z = ____.$
- i) The square root of 121 is____.

Answers:

- a) 49
- b) x = 5
- c) 12
- d) Non-negative

- e) y = 9
- f) 8
- g) 100
- h) Z = 6
- i) 11

Summary

1. Understanding Squares:

- A square of a number is obtained by multiplying the number by itself.
 - For example, the square of 5 is 5 * 5 = 25, denoted as $5^2 = 25$.
- Squares are always non-negative since a negative number multiplied by it yields a positive result.

2. Properties of Squares:

- Squares of even numbers always result in an even number.
- Squares of odd numbers always result in an odd number.
- The square of any number, whether positive or negative, is always positive.

3. Perfect Squares:

- Some numbers are perfect squares, meaning they can be expressed as the square of an integer.
 - Examples include 1, 4, 9, 16, 25, etc.

4. Square Roots:

- The square root of a number is the value that, when multiplied by itself, gives the original number.
- For instance, the square root of 25 is 5 because 5*5=25 denoted as $\sqrt{25}=5$.
- A square root can be positive or negative. For example, both -5 and 5 are square roots of 25.

5. Notation and Representation:

- The symbol for square root is $\sqrt{.}$ For instance, $\sqrt{16} = 4$.
- Square roots of perfect squares are whole numbers.
- Square roots of non-perfect squares are irrational numbers and cannot be represented as simple fractions.

6. Calculating Square Roots:

- Methods such as prime factorization, long division, or using calculators are employed to calculate square roots.
- Estimation techniques like the Babylonian method are used for manual calculations.

7. Applications:

- Squares and square roots are used extensively in various fields like geometry, physics, engineering, and computer science.
- They're crucial in solving problems involving areas, volumes, equations, and in understanding patterns in sequences.

8. Relationship between Squares and Square Roots:

- Squares and square roots are inverse operations of each other.
- If $x^2 = y$, then $\sqrt{y} = x$ and vice versa.

