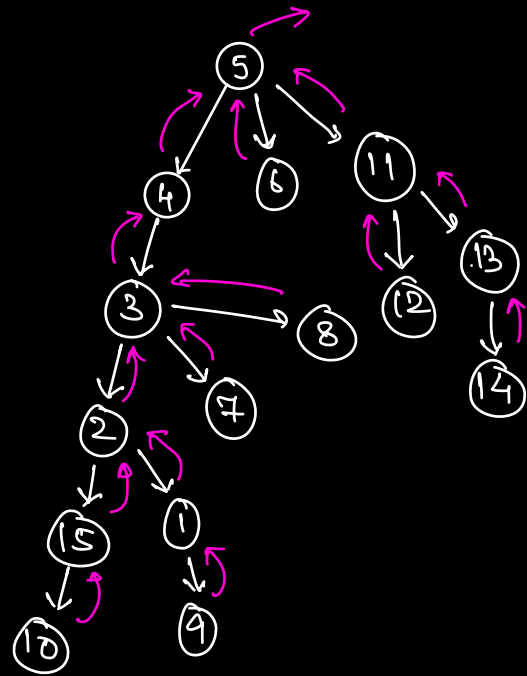
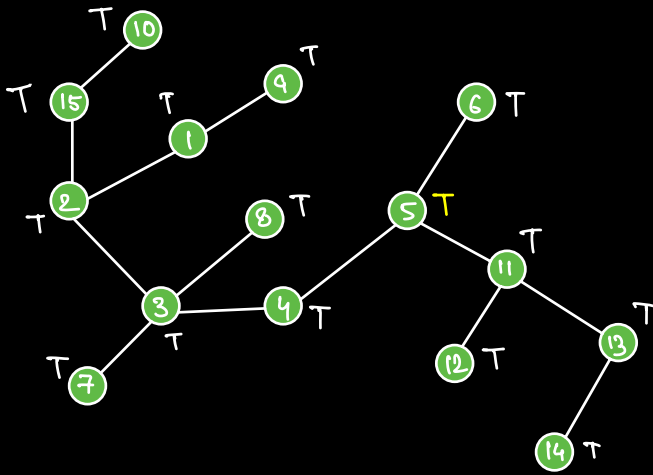


# Dfs (Depth First Search)

S=5, D=14



```
bool path(N, E, u[], v[], src, dest) {
```

```
    list<int> g[N+1]; // Graphs-1 class.
```

```
    bool vis[N+1] = {false};
```

```
    dfs(g, N, E, src);
```

```
    return vis[dest];
```

3

```
void dfs(list<int> g, N, E, src) {
```

```
    if (vis[src] == true) return;
```

```
    vis[src] = true;
```

```
    for (i=0; i < g[src].size(); i++) {
```

```
        v = g[src][i];
```

```
        dfs(g, N, E, v);
```

3

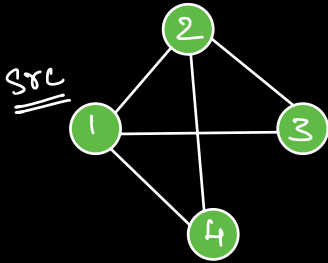
3

TC:  $O(E)$  {same as BFS}

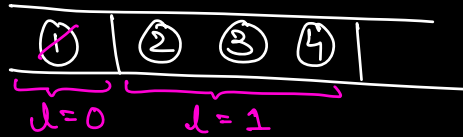
SC:  $O(E + N + N) \approx \underline{O(E)}$  { $E \gg N$ }

↓ Stack Visited  
Adj List

Ex

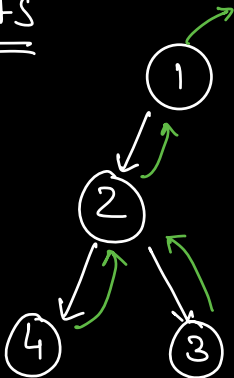


BFS



⇒ Shortest path of node 2, 3 & 4 from node ① is 1 only.

Dfs



⇒ length of path from ① to ④ = 2

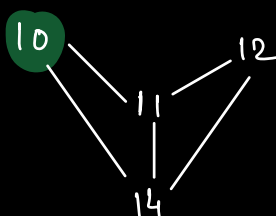
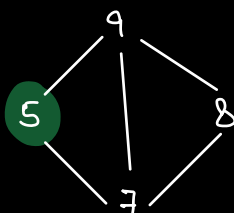
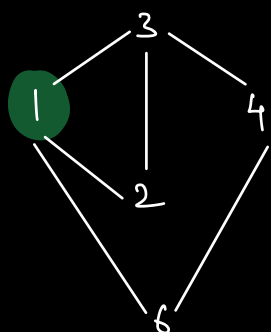
⇒ NOTE: Dfs won't always give you the shortest path b/w 2 nodes.

Only visit ⇒ Dfs

Shortest path ⇒ BFS.

Q: Given an undirected graph, find the no. of connected components.

**Connected Component:** A component is said to be connected if from every node we can visit all the nodes inside the component.



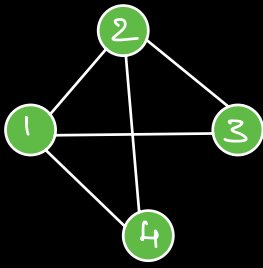
Adj. List

0		
1	→ 2, 3, 6	(Apply DFS)
2	→ 1, 3	
3	→ 1, 2, 4	
4	→ 3, 6	
5	→ 7, 9	(Apply DFS)
6	→ 1, 4	
7	→ 5, 8, 9	
8	→ 7, 9	
9	→ 5, 7, 8	
10	→ 11, 14	(Apply DFS)
11	→ 10, 12, 14	
12	→ 11, 14	
13	→ 15	
14	→ 10, 11, 12	
15	→ 13	(Apply DFS)

⇒ Inside one component if we apply BFS/DFS then all the nodes of that component will be visited.

⇒ So apply DFS/BFS algo. on all the nodes.

No. of connected components  
 $\equiv$  No. of BFS/DFS fun<sup>n</sup> calls.



No. of connected components = 1



No. of connected components = 6

```

int components (N, E, u[], v[]) {
    // Create Adjacency list.
    list<int> g[N+1];
    bool vis[N+1] = false;
    C = 0;
    for (i = 1; i <= N; i++) {
        if (!vis[i]) {
            dfs(g, N, E, i, vis);
            C++;
        }
    }
    return C;
}

```

3

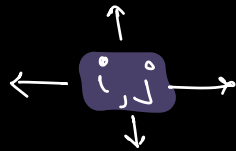
TC:  $O(E)$   
 SC:  $O(E)$

Q. No. of Islands.  $\rightarrow (N \times M)$

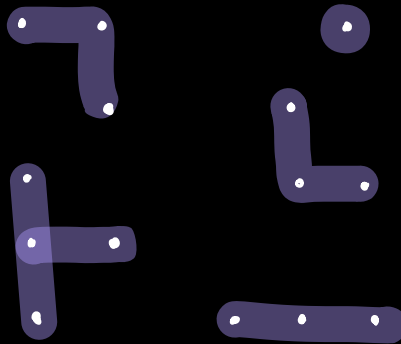
Given a matrix of 1's & 0's. find the no. of islands in the matrix.

1  $\Rightarrow$  land mass

0  $\Rightarrow$  water body.



	0	1	2	3	4
0	1	1	0	0	1
1	0	1	0	1	0
2	1	0	0	1	1
3	1	1	0	0	0
4	1	0	1	1	1



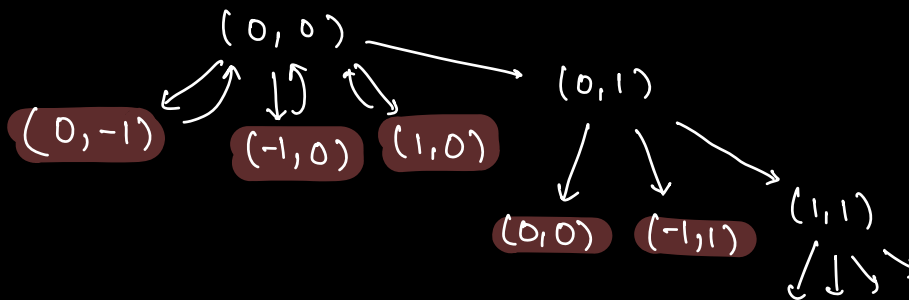
No. of islands = 5

$\rightarrow$  No. of connected components.

$\Rightarrow$  Adjacency list isn't required as we can use the given matrix itself.

	0	1	2	3	4
0	1 <sub>0</sub>	1 <sub>0</sub>	0	0	1 <sub>0</sub>
1	0	1 <sub>0</sub>	0	0 <sub>1</sub>	0
2	1 <sub>0</sub>	0	0	1 <sub>0</sub>	1 <sub>0</sub>
3	1 <sub>0</sub>	1 <sub>0</sub>	0	0	0
4	1 <sub>0</sub>	0	1 <sub>0</sub>	1 <sub>0</sub>	1 <sub>0</sub>

No. of islands  $\equiv$   
No. of connected  
components.



```

int islands (int mat[N][M], N, M) {
    int c = 0;
    for (i = 0; i < N; i++) {
        for (j = 0; j < M; j++) {
            if (mat[i][j] == 1) {
                dfs(mat, N, M, i, j);
                c++;
            }
        }
    }
    return c;
}

```

```
void dfs(int mat[N][M], N, M, i, j) {
```

```
    if (i < 0 || j < 0 || i == N || j == M || mat[i][j] == 0)
        return;
```

```
    mat[i][j] = 0;
```

```
    { dfs(mat, N, M, i+1, j) // Down
```

```
      dfs(mat, N, M, i-1, j) // Up
```

```
      dfs(mat, N, M, i, j+1) // Right
```

```
      dfs(mat, N, M, i, j-1) // Left
```

```
    int x[]: {1, -1, 0, 0}
```

```
    int y[]: {0, 0, 1, -1}
```

```
    for (k = 0; k < 4; k++) {
```

```
        dfs(mat, N, M, i + x[k], j + y[k]);
```

```
    }
```

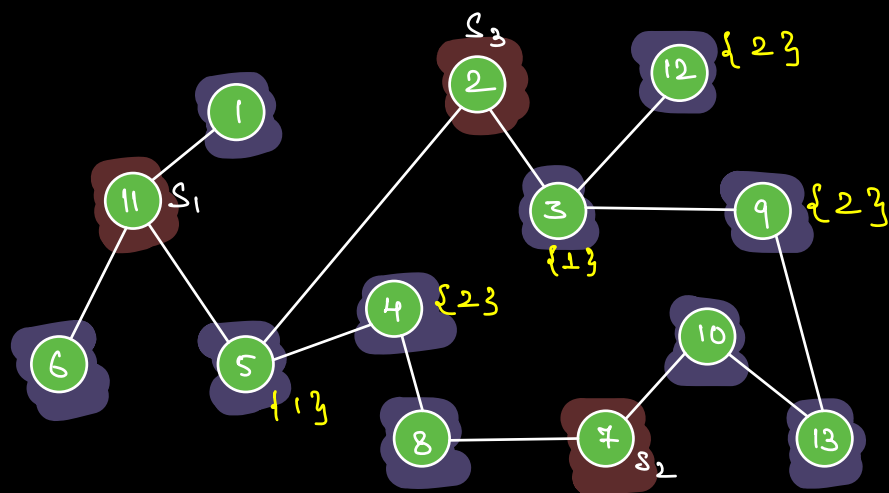
TC:  $O(NM)$

SC:  $O(NM)$

↳ Stack size.

## # Multi source BFS

Given  $N$  nodes & multiple sources  $S_1, S_2$  &  $S_3$ . Find the length of shortest path for all the nodes to any of the source nodes.

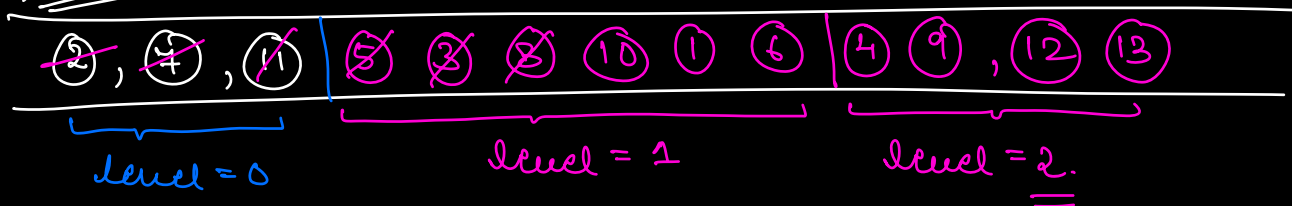


$S_1 : 11$

$S_2 : 7$

$S_3 : 2$

## Queue



⇒ Only change is to push all the source nodes in the queue at the start.

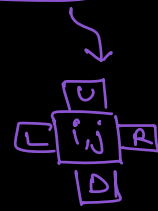
⇒ HW



## Q. Rotten Oranges.

mat[N][M]  $\rightarrow$   $\begin{cases} 0 : \text{Empty} \\ 1 : \text{fresh orange} \\ 2 : \text{Rotten orange} \end{cases}$

Every minute any fresh orange, adjacent to a rotten orange will become rotten.  
find the min time in which all the oranges will become rotten.



If NOT possible, return -1;

	0	1	2	3	4
0	$+_3$	0	$+_3$	0	$+_5$
1	$+_2$	$+_1$	$+_2$	$+_3$	$+_4$
2	0	2	0	$+_4$	0
3	0	$+_1$	$+_2$	$+_3$	$+_4$
4	$+_3$	$+_2$	$+_3$	0	$+_5$

$\Rightarrow$  ans = 5

	0	1	2	3	4
0	$t_3$	0	$t_1$	$2_0$	$t_1$
1	$t_2$	$t_1$	$t_2$	$t_1$	$t_2$
2	0	$2_0$	0	$t_2$	0
3	0	$t_1$	$t_2$	$t_1$	$t_2$
4	$t_3$	$t_2$	$t_1$	$2_0$	0

$\Rightarrow t = 3 : \underline{\underline{\text{Ans.}}}$

	0	1	2	3	4
0	0	0	0	1	1
1	0	1	1	1	0
2	1	2	0	2	0
3	1	1	1	0	0
4	1	2	1	0	1

$\Rightarrow \underline{\underline{-1}}$

	0	1	2	3	4
0	$t_3$	0	$t_1$	$2_0$	$t_1$
1	$t_2$	$t_1$	$t_2$	$t_1$	$t_2$
2	0	$2_0$	0	$t_2$	0
3	0	$t_1$	$t_2$	$t_1$	$t_2$
4	$t_3$	$t_2$	$t_1$	$2_0$	0

$\text{time}[][] = -1$

	0	1	2	3	4
0	-1	-1	<del><math>t_1</math></del>	<del><math>t_1</math></del>	<del><math>t_1</math></del>
1	-1	<del><math>t_1</math></del>	-1	<del><math>t_1</math></del>	-1
2	-1	<del><math>t_1</math></del>	-1	-1	-1
3	-1	<del><math>t_1</math></del>	-1	<del><math>t_1</math></del>	-1
4	-1	-1	<del><math>t_1</math></del>	<del><math>t_1</math></del>	<del><math>t_1</math></del>

---

~~(0,3)~~ ~~(2,1)~~ (4,3) (0,4) (0,2) (1,3)

---

⇒ Queue (pair (int, int) > q;

(0,3) → (0,4)  
          → (0,2)  
          → (1,3)

⇒ After creating the time matrix, find max.

⇒ After the complete iteration if matrix still contains ① then return -1.

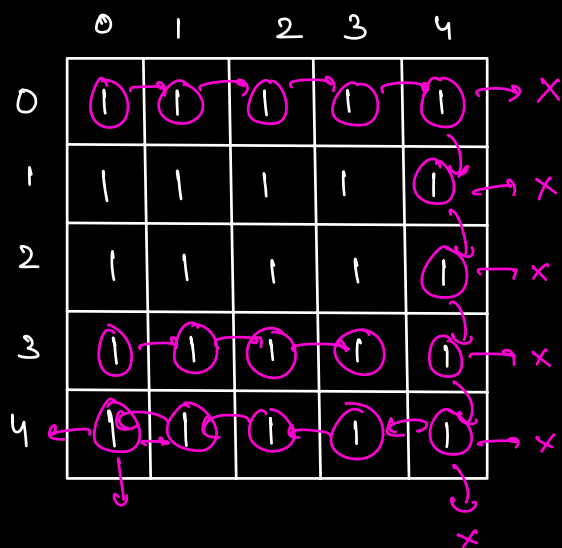
⇒ Create a separate time[][] matrix.

	0	1	2	3	4
0	$t_3$	0	$t_3$	0	$t_5$
1	$t_2$	$t_1$	$t_2$	$t_3$	$t_4$
2	0	$2_0$	0	$t_4$	0
3	0	$t_1$	$t_2$	$t_3$	$t_4$
4	$t_3$	$t_2$	$t_3$	0	$t_5$

HW: Implement

—————\*—————

$time[i][j] = \text{time of source} + 1$   
                                  cell



$$\left. \begin{matrix} 2 \\ 1 \\ 0 \end{matrix} \right\}$$

$O(NM)$