

Inorder :-

Left Root Right

```
void InOrder (root) {
```

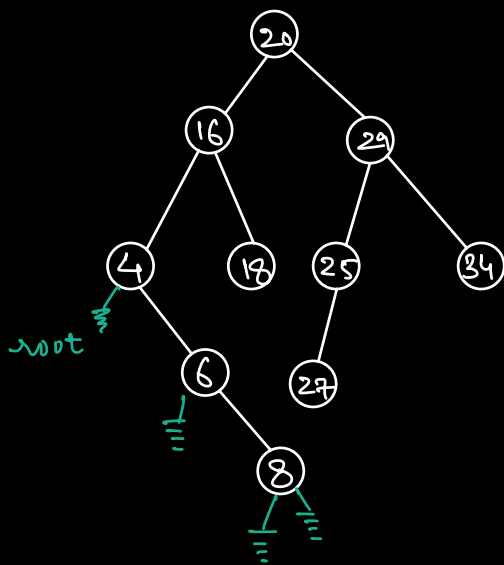
```
1) if (root == Null)
    return;
```

```
2) InOrder (root.left);
```

```
3) Print (root.data)
```

```
4) InOrder (root.right);
```

```
}
```

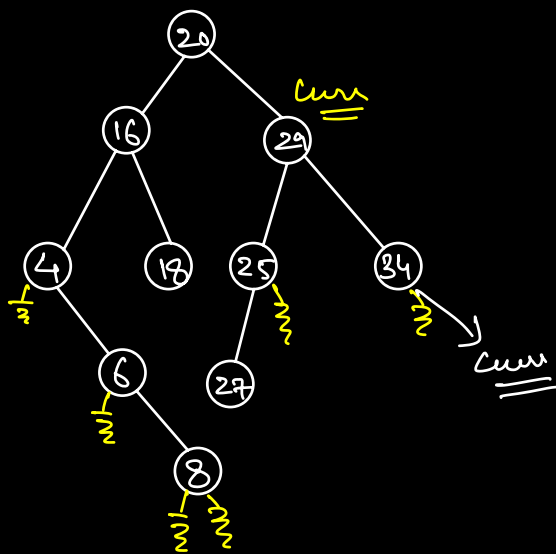


| | | | | | |
|----|---|---|---|---|---|
| 34 | : | X | X | X | X |
| 27 | : | X | X | X | X |
| 25 | : | X | X | X | X |
| 29 | : | X | X | X | X |
| 18 | : | X | X | X | X |
| 8 | : | X | X | X | X |
| 6 | : | X | X | X | X |
| 4 | : | X | X | X | X |
| 16 | : | X | X | X | X |
| 20 | : | X | X | X | X |

4, 6, 8, 16, 18, 20, 27, 25, 29, 34

1. Till we get a NULL on the left side, keep on inserting in the Stack.
2. If $root == NULL$, get the top element from Stack, print it & move towards right.

Q. Inorder traversal in iterative way.



18
8
6
4
16
20

4 6 8 16 18 20 27 25 29 34

```

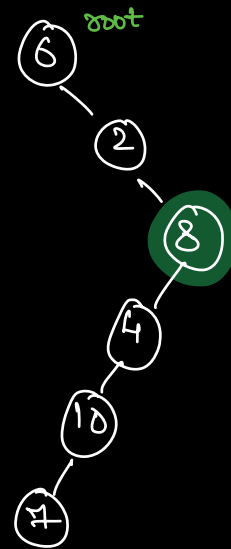
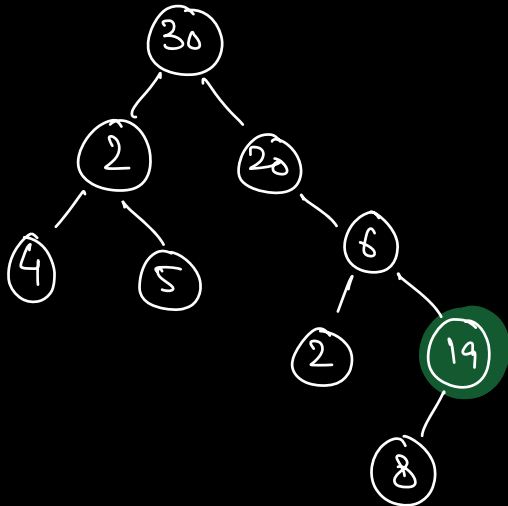
void inorderIterative ( root ) {
    curr = root;
    Stack < Node > st;
    while ( curr != Null || st.size() > 0 ) {
        if ( curr != Null ) {
            st.push ( curr )
            curr = curr.left;
        }
        else {
            Node temp = st.top()
            st.pop();
            print ( temp.data );
            curr = temp.right;
        }
    }
}

```

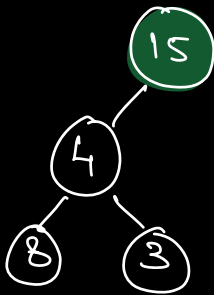
TC : $O(N)$
 SC : $O(N)$

HIN
 Pre Order } ✓
 Post Order } ✓

Q. Given a tree, find the last inorder node that we print.



⇒ Keep going on right side until we get a NULL.



⇒ Right most node.

Morris Inorder Traversal.

↓
Expected SC: $O(1)$

6 8

```
inOrder (Node root) {
```

```
Node curr = root;
```

```
while (curr != NULL)
```

```
{
    if (curr.left == NULL) {
```

```
        print(curr.data)
```

```
        curr = curr.right;
```

3

```
    } else { // curr.left != NULL
```

```
        temp = curr.left;
```

```
        while (temp.right != NULL &&
```

```
            temp.right != curr) {
```

```
            temp = temp.right;
```

```
        } if (temp.right == NULL) {
```

```
            // Visiting curr Node 1st time
```

```
            temp.right = curr;
```

```
            curr = curr.left;
```

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```
        } else { // temp.right = curr, i.e. visiting
```

```
            // curr node 2nd time.
```

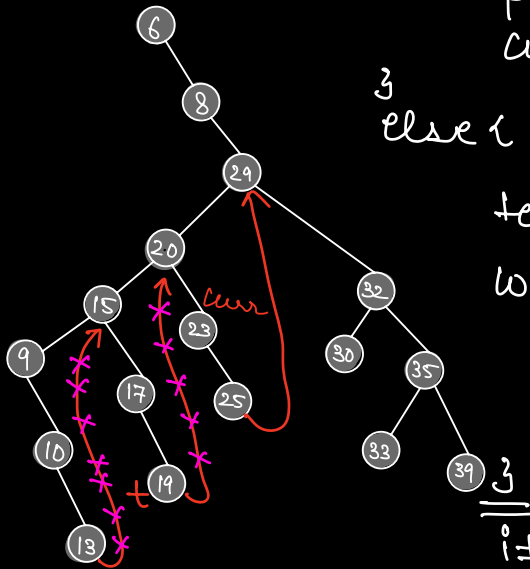
```
            temp.right = NULL
```

```
            print(curr.data);
```

```
            curr = curr.right;
```

3

3



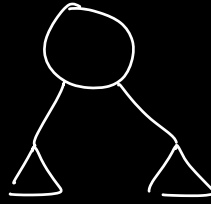
TC: $O(N)$

SC: $O(1)$

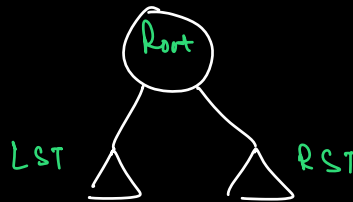
Q. Given a Binary Tree, check if it is a BST or not.

* nodes :

$$LST < \text{Root.val} < \underline{\underline{RST}}$$



(1)



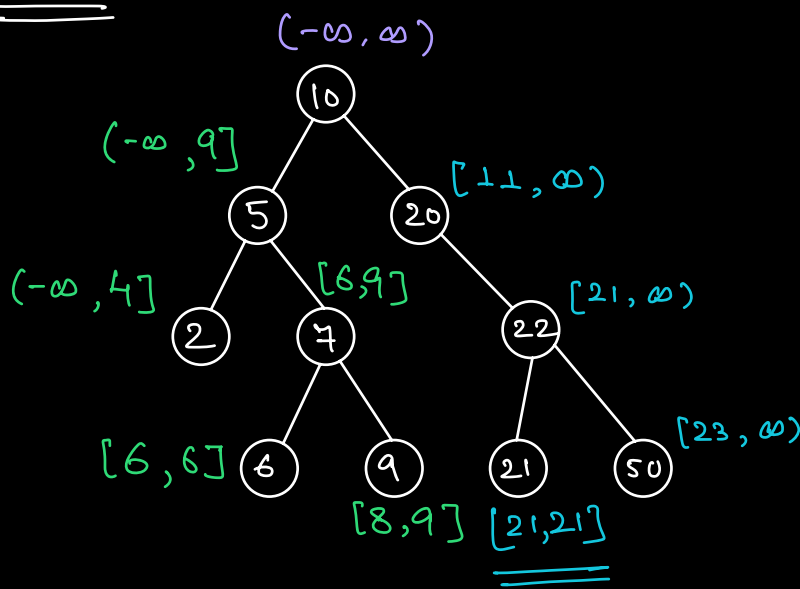
⇒ Inorder: $\underbrace{LST \quad \text{Root} \quad RST}_{\underline{\underline{\text{Sorted.}}}}$

- Store the inorder traversal of BT
- If it is sorted in ascending order return true, else return false.

TC : $O(N)$

SC : $O(N)$

II Pre Order



```

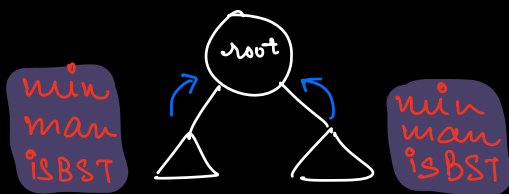
bool isBST (root, -∞ l, +∞ r) {
    if (root == NULL) return true;
    if (root->val >= l && root->val <= r) {
        bool lst = isBST (root->left, l, root->val-1);
        bool rst = isBST (root->right, root->val+1, r);
        return lst && rst;
    }
    return false;
}

```

3

Preorder

TC: $O(N)$
SC: $O(N)$



```

class TreeInfo {
    int min;
    int max;
    bool isBST;
}

```

3

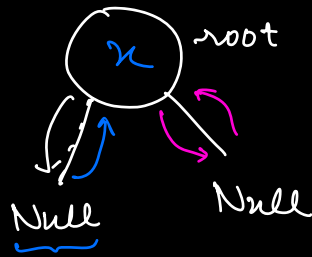
```

TreeInfo isBST(root) {
    if (root == NULL) {
        return new TreeInfo(+∞, -∞, true);
    }
    TreeInfo l = isBST(root.left);
    TreeInfo r = isBST(root.right);
    if (l.isBST && r.isBST &&
        root.val > l.max && root.val < r.min) {
        return new TreeInfo(
            min(root.val, l.min, r.min),
            max(root.val, l.max, r.max),
            true
        );
    }
    return new TreeInfo(
        min(root.val, l.min, r.min),
        max(root.val, l.max, r.max),
        false
    );
}

```

3

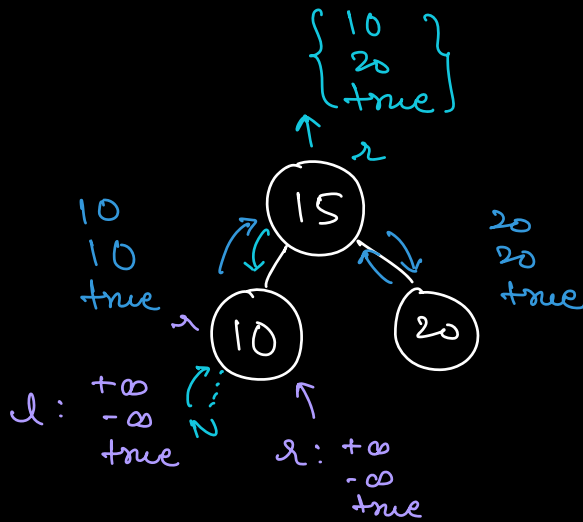
$MIN \rightarrow +\infty$
 $MAX \rightarrow -\infty$
 $isBST \rightarrow true$



$+\infty \leftarrow \underline{MIN}$
 $-\infty \leftarrow \underline{MAX}$
 $true$

TC: $O(N)$

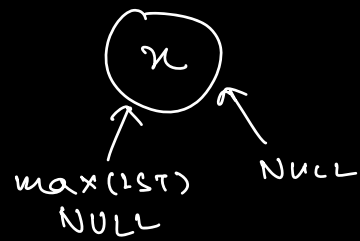
SC: $O(N)$



min
 max
 $isBST$



$x > M1$
 $\&$
 $x < m2$



$$\underline{n} > \text{max(LST)}$$

$$\Downarrow$$

$$\underline{-\infty}$$

$$n < \text{min(RST)}$$



$$\left\{ \begin{array}{l} \text{min} = +\infty \\ \text{max} = -\infty \\ \text{isBST} = \text{true} \end{array} \right\}$$
