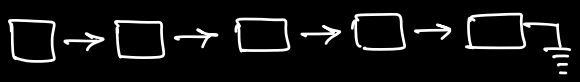
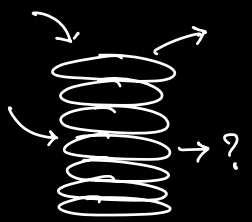
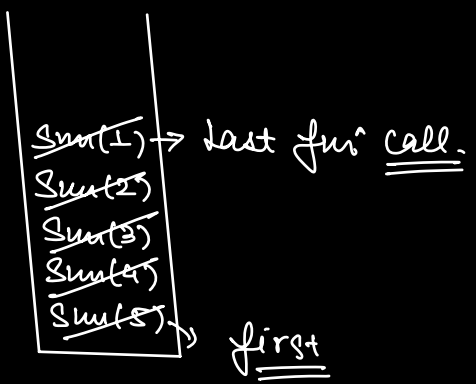
Stack.

→ Arrays ⇒

→ Linked List ⇒





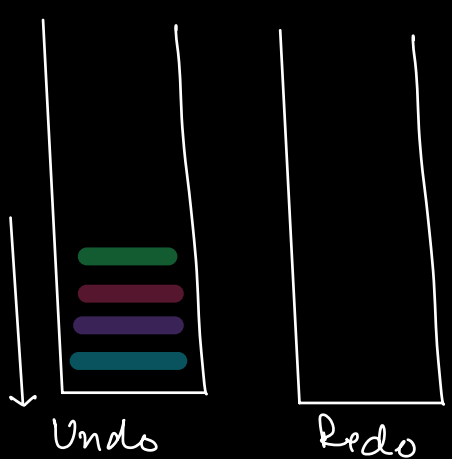


→ Recursion Call Stack

Last In, First Out.

⇒ Stack.

① Recursion Call Stack
② Web browsers.
③ Undo | Redo

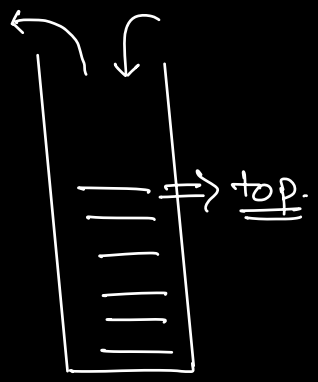


→ Abstract Data Type (ADT)

Stack as an ADT

↓

LIFO.



TC: O(1)

- push(x) ✱
- pop() ✱
- top() / peek()
- size()
- isEmpty()
- Clear()

Stack Implementation :-

① Array

② LL.

✱ Array implementation of Stack.

```
int arr[5];
top = -1;
```

Stack is Empty.

0	1	2	3	4
5	3	2	6	8

↑ top

- push(5):
  - → top++
  - → arr[top] = 5

} ⇒ O(1)

- push(3), push(2), push(6), push(8),

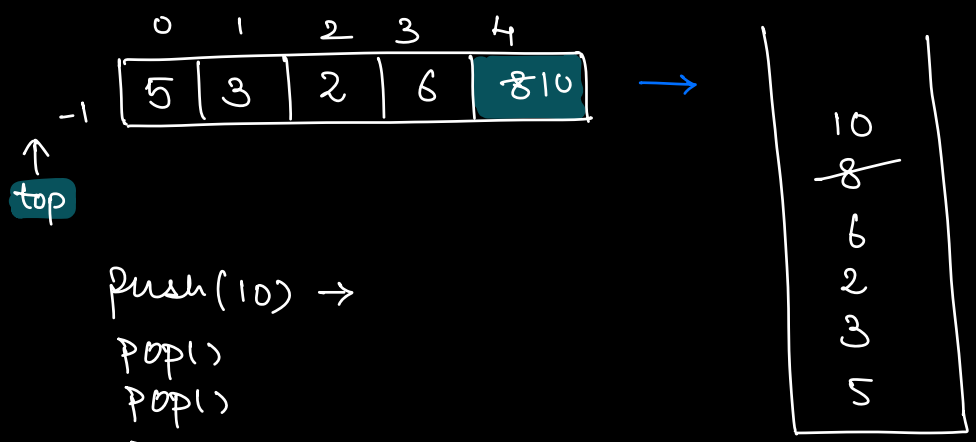
push(1)

↳ Array Index Out of bound

→ Overflow. ✓

⇒ Dynamic Arrays.

pop() : if (top > -1) top--

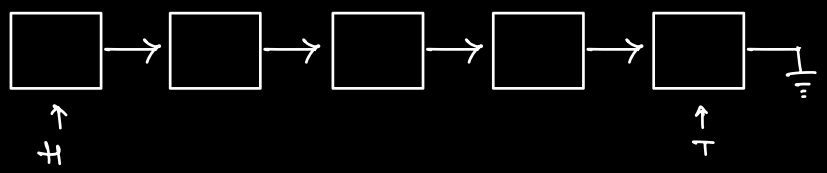


push(10) →

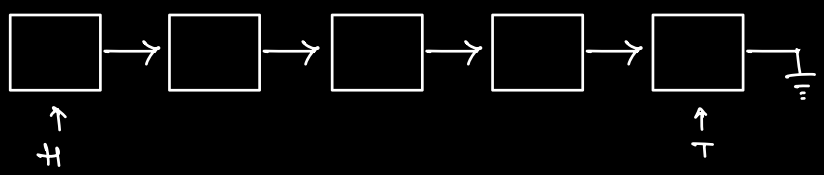
pop()
pop()
pop()
pop()
pop()
pop()

⇒ Underflow.

Linked list implementation of stack.



TC of insertion at tail ⇒ O(1)
TC of deletion at tail ⇒ O(N)



TC of insertion at head ⇒ O(1)
TC of deletion at head ⇒ O(1)

push(x)
pop()
} O(1)

```
Stack<Int> st = new Stack<>(); → Java
Stack<int> st; → C++
st.push(x);
st.pop();
```

* Q: Given the library stack, Create a new Stack like DS that gives us :

- push(x)
- pop()
- getMin()

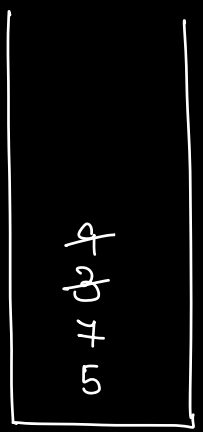
TC: O(1)

New Stack :

push(5)
push(6)
push(4)
push(7)
getMin() → 4
pop()
pop()
getMin() → 5
push(3)
getMin() → 3
pop()
getMin() → 5

* push(5)
push(7)
push(3)
push(9)
getMin() → 3
pop()
getMin() → 3
pop()
getMin() → 3 ✗✗
→ 5

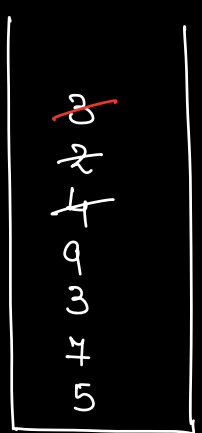
min = ~~5~~ ~~3~~ 3



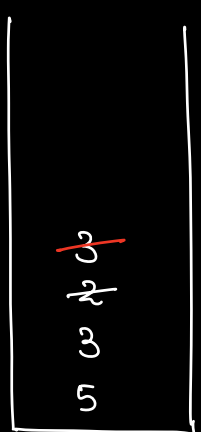
minStack.

#

push(5)
push(7)
push(3)
push(9)
getMin() ⇒ 3
push(4)
push(2)
getMin() ⇒ 2
pop()
getMin() ⇒ 3
pop()
getMin() ⇒ 3 ✓
push(3)
pop()



Stack



minStack

push(x) : st.push(x)
O(1)
if (x <= minStack.top()) {
    minStack.push(x);
}

Check if stack isn't Empty.

pop() :
O(1)
x = st.top();
st.pop()
if (x == minStack.top()) {
    minStack.pop();
}

getMin() ⇒ minStack.top()
O(1)

Q: Given a string, Remove pairs of consecutive elements repeatedly until there are NO duplicate pairs.

Amazon
MS.

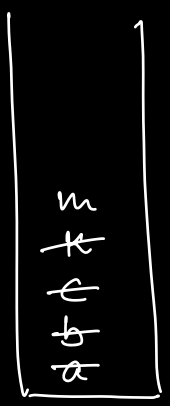
S: a b c d d c b k
a b c c b k
a b b k
a k.

Quiz

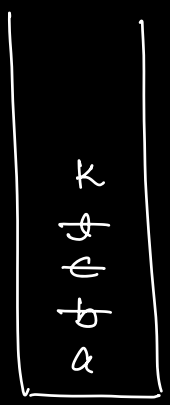
S: a a a b
a b.

Quiz

S: a b c k k c b a m



S: a b c d d c b k



ka

reverse.

* Expression Evaluation.

x /
+ -

$7 \times 1 + 2 - 8 \times 3 + 10/5 \Rightarrow$

$7 + 2 - 24 + 2 = -13$

Computers uses

Infix Notation	Postfix Notation
A + B	A B +
A - B	A B -
A x B	A B x
A / B	A B /

* $10 + 3 \times 4 \Rightarrow 10 + 3 \times 4$

$= 10 + 34\times$

$= 10\ 34 \times +$

- Infix to Postfix ✓
- Evaluate the postfix

$A + B \times C$

$\Downarrow$

$A + BC \times$

$\Downarrow$

$A\ BC \times +$

$A \times B + C$

$\Downarrow$

$AB \times + C$

$\Downarrow$

$AB \times C +$

- Infix to Postfix

Quiz

$4 + 8 * 7$

$\downarrow$

$4 + 8\ 7\ *$

$4\ 8\ 7\ * +$

Quiz

$10 + 3 * 4 - 7$

$\downarrow$

$10 + 3\ 4\ * - 7$

$10\ 3\ 4\ * + - 7$

$10\ 3\ 4\ * + 7 -$

Quiz

$10 / (4 - 2) * 6 + 9$

$\downarrow$

$10 / (4\ 2\ -) * 6 + 9$

$\downarrow$

$(10\ 4\ 2\ - /) * 6 + 9$

$\downarrow$

$(10\ 4\ 2\ - /\ 6\ *) + 9$

$\downarrow$

$(10\ 4\ 2\ - /\ 6\ *)\ 9\ +$

Quiz $(10+3) * 2 - (7-6) * (4+8)$

$10\ 3+ * 2 - 7\ 6- * 4\ 8+$

$10\ 3+\ 2\ * - 7\ 6-\ 4\ 8+\ * -$

⇒ Operands follows the same relative order b/w infix & postfix notation.

$10 + 3 \longrightarrow 10\ 3\ +$

$4 + 8 * 7 \longrightarrow 4\ 8\ 7\ \times\ +$

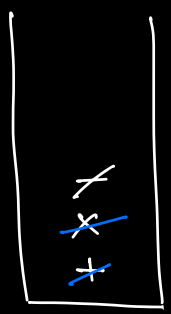
Box 

precedence

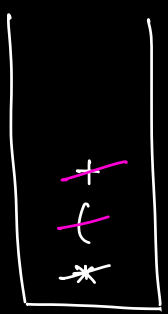
$4 \times 8 + 7 \longrightarrow 4\ 8\ \times\ 7\ +$

⇒ STACK.

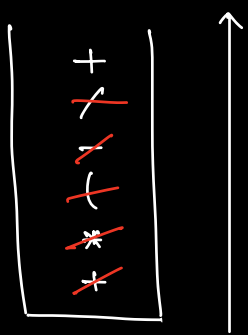
$10 + 3 \times 4 - 7 \longrightarrow 10\ 3\ 4\ \times\ +\ 7\ -$

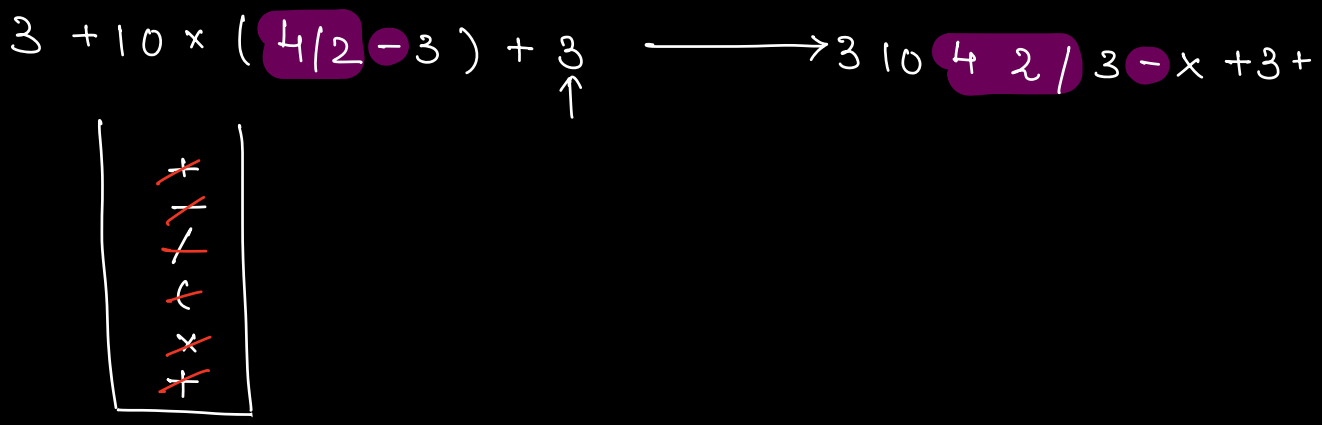


$10 * (3+4) \longrightarrow 10\ 3\ 4\ +\ *$



$3 + 10 \times (3 - 4/2) + 3 \longrightarrow 3\ 10\ 3\ 4\ 2\ /\ -\ *\ +\ 3\ +$





Traverse the string S[i]

Operand.
Add it to postfix string

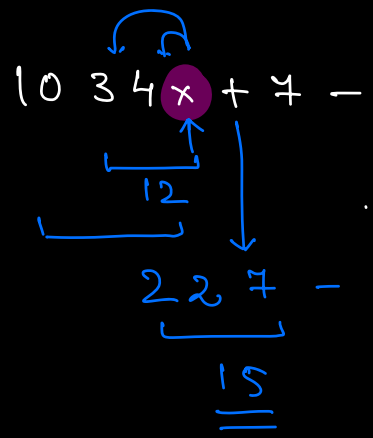
'('
- Push to Stack

')'
Keep popping & apply the operators till we get '('

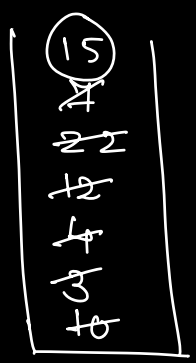
Operator(curr)
if (prec(curr) <= prec(St.top()))

- **true**
  - Keep popping from until we get a lesser precedence operator on top **or** Stack becomes empty.
- **false**
  - Push to Stack.

Keep popping the stack & apply until Stack is Empty.



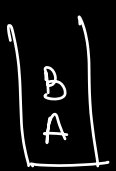
10 3 4 x + 7 -
↑



A B (op)

A op B

A - B ⇒ A B -



A-B