

Backtracking \Rightarrow Try out all possibilities
(Brute force)

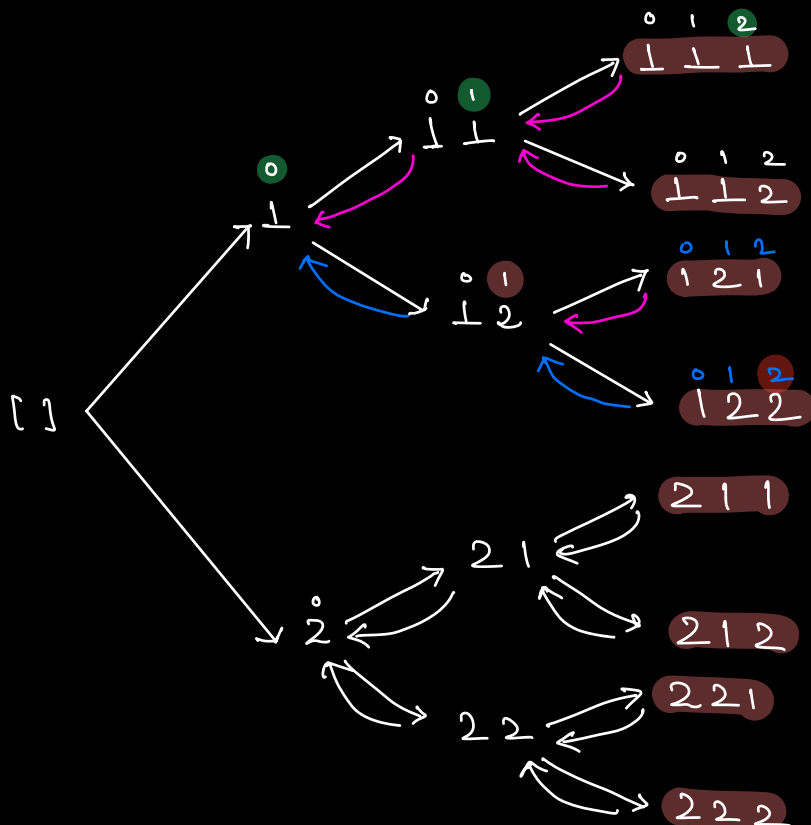
Recursion + Backtrace

Q.1 Print all N digit numbers using {1, 2, 3}

$$\underline{\underline{N=1}} \Rightarrow \frac{1}{2}$$
$$\underline{\underline{N=3}} \quad \begin{bmatrix} \underline{1} & \underline{1} & \underline{1} \end{bmatrix}$$

$$\begin{bmatrix} \underline{1} & \underline{1} & \underline{2} \end{bmatrix}$$
$$\underline{\underline{N=2}} \Rightarrow \begin{array}{cc} \underline{1} & \underline{1} \\ \underline{1} & \underline{2} \\ \underline{2} & \underline{1} \\ \underline{2} & \underline{2} \end{array}$$

<u>1</u>	<u>2</u>	<u>1</u>
<u>1</u>	<u>2</u>	<u>2</u>
<u>2</u>	<u>1</u>	<u>1</u>
<u>2</u>	<u>1</u>	<u>2</u>
<u>2</u>	<u>2</u>	<u>1</u>
<u>2</u>	<u>2</u>	<u>2</u>

$$N=3 \quad \left(\frac{1}{2} \quad \frac{1}{1} \quad \frac{1}{2} \right)$$


```

void generateNumbers ( N, idx, currList ) {
    if ( idx == N ) {
        print ( currList );  $\Rightarrow O(N)$ 
        return;
    }

```

3
 currList[idx] = 1

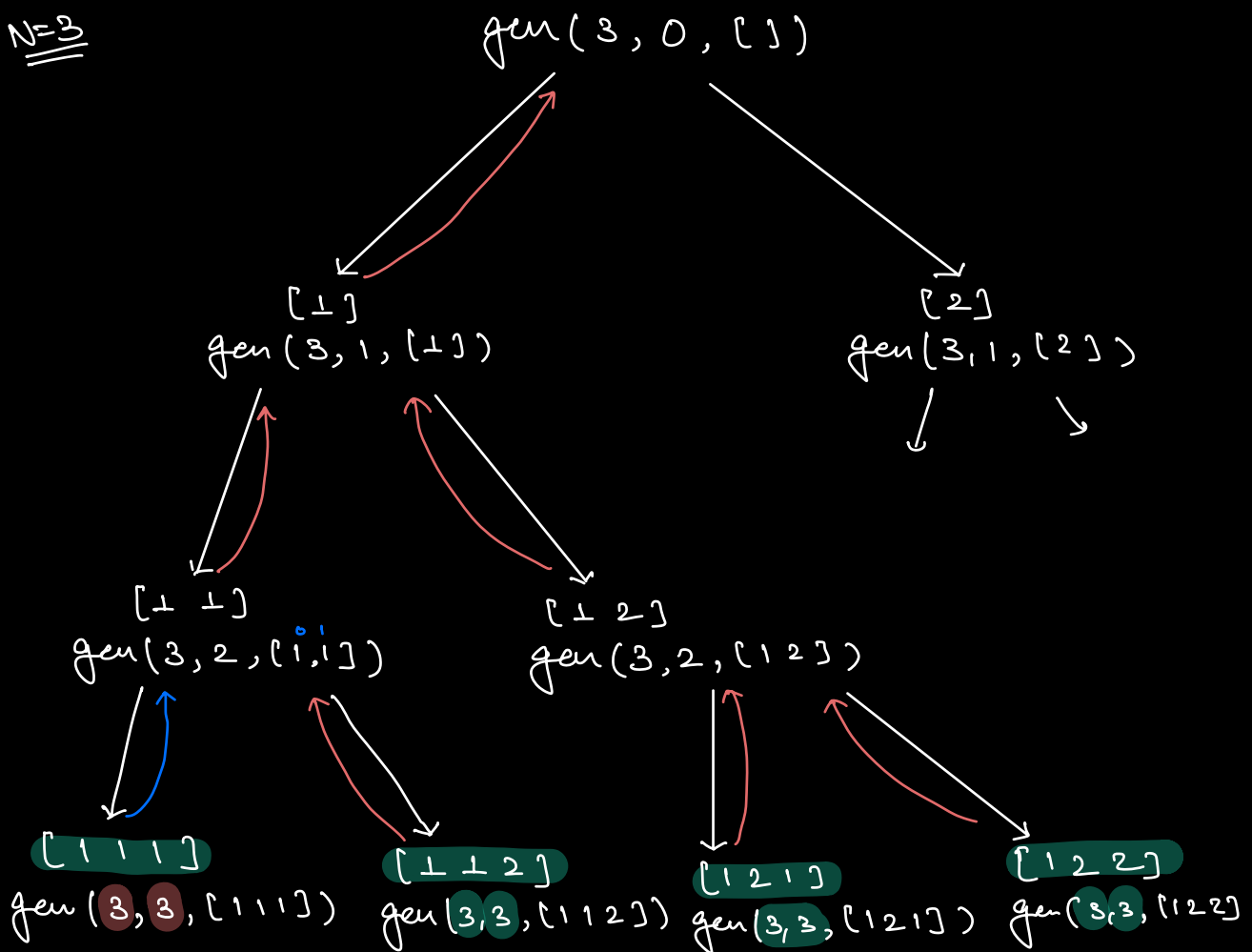
generateNumbers (N, idx+1, currList);

Backtrack [currList[idx] = 2

generateNumbers (N, idx+1, currList);

3

N=3



Quiz

TC:

TC of a recursive funⁿ:

(# of recursive funⁿ calls) * TC of each funⁿ call.



$$2^N * N$$

Recurrence relation :-
 $T(N) = 2 * T(N-1) + N$

*

$$\boxed{TC: O(N \cdot 2^N)}$$

$$SC: O(N)$$

SC = Height of tree. $O(N)$ + Current List is also $O(N)$
so overall $O(N)$

* Return a list of list

$[[1, 1, 1], [1, 1, 2], [1, 2, 1], [1, 2, 2], [2, 1, 1],$
 $[2, 1, 2], [2, 2, 1], [2, 2, 2]]$

`list<list<int>> ans;`

```
void generateNumbers ( N, idx, currList ) {
```

```
    if ( idx == N ) {
```

```
        ans.add(currList);  $\Rightarrow$  O(N)
```

Need to create new temp list and add that list to ansList. Its O(N) for time

```
        return;  $\downarrow$  reference.
```

```
        3  
        currList[idx] = 1
```

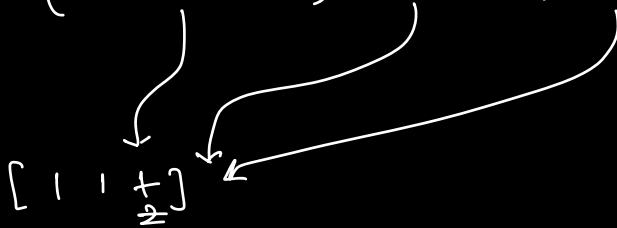
```
        generateNumbers ( N, idx+1, currList );
```

```
    Backtrack [ currList[idx] = 2
```

```
        generateNumbers ( N, idx+1, currList );
```

```
    3
```

```
ans: [ currList, currList, currList
```



```
ans: [ [2 2 2] [2 2 2] ... ]
```

* HW

* Hard Copy vs Soft Copy. \Rightarrow Java

* Deep Copy vs Shallow Copy

```
currList: [1 1 1]
```

```
    temp: [1 1 1]
```

```
    ans:
```

$$TC: O(N \cdot 2^N)$$

Q. Print all N digit numbers using {1, 2, 3, 4, 5}.

```
void generateNumbers (N, idx, currList) {
    if (idx == N) {
        print(currList);  $\Rightarrow O(N)$ 
        return;
    }
```

3
currList[idx] = 1

generateNumbers(N, idx+1, currList);

currList[idx] = 2

generateNumbers(N, idx+1, currList);

currList[idx] = 3

generateNumbers(N, idx+1, currList);

currList[idx] = 4

generateNumbers(N, idx+1, currList);

currList[idx] = 5

generateNumbers(N, idx+1, currList);

5

for (i = 1; i <= 5; i++) {
 currList[idx] = i;

generateNumbers(N, idx+1, currList);

3

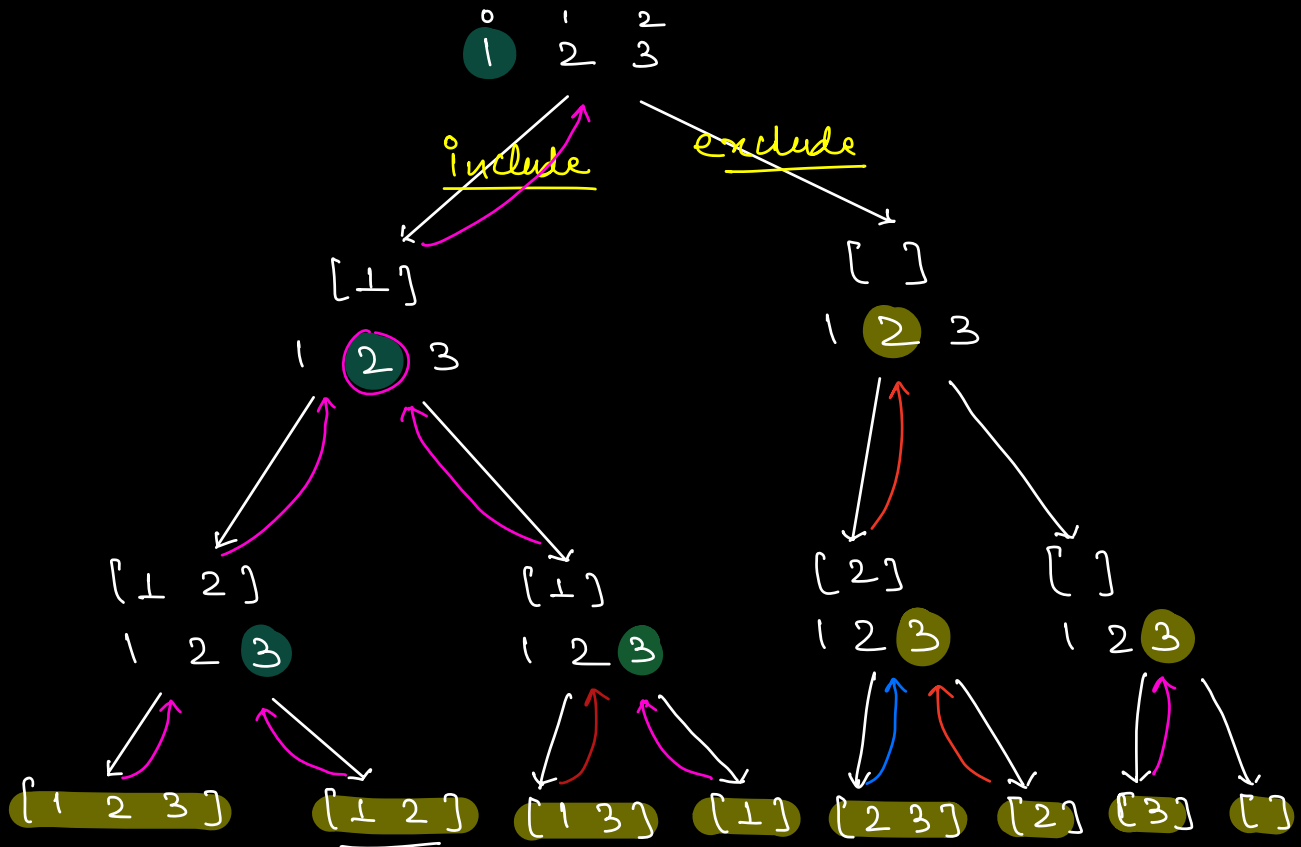
$$\underline{\underline{TC: O(N \cdot 2^N)}}$$

Q. Given an Array, generate all subsets of the Array.
Amazon
MS.

A: [1 2 3]

[]
 [1]
 [2]
 [3]
 [1 2]
 [1 3]
 [2 3]
 [1 2 3]

curlist: []



No. of subsets $\Rightarrow \underline{\underline{2^N}}$

```
void generateSubsets (A[], N, idx, curList) {
    if (idx == N) {
        print(curList);
        return;
    }
```

3

// Include A[idx] in the subset

curList.add(A[idx]);

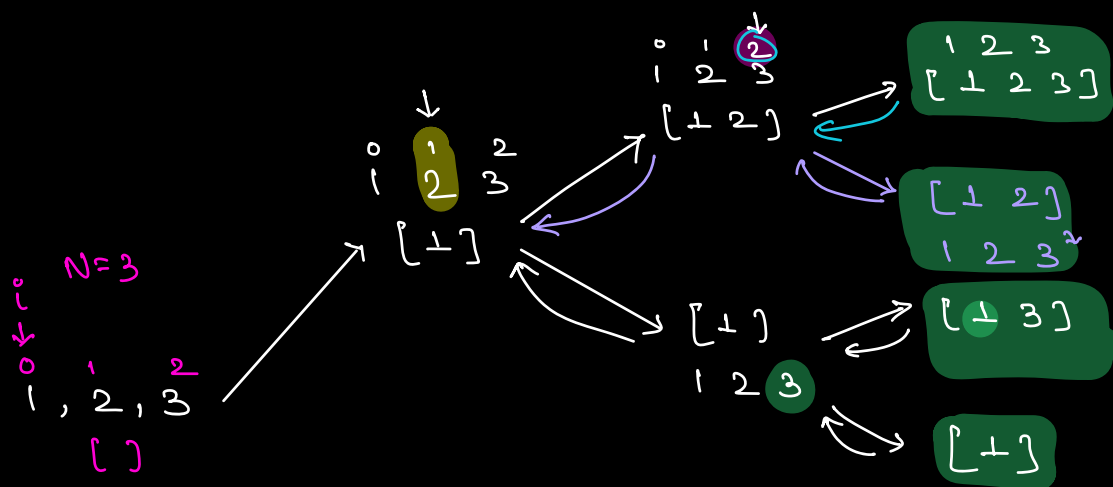
generateSubsets(A, N, idx+1, curList);

// Exclude A[idx] in the subset

curList.pop(A[idx]);

generateSubsets(A, N, idx+1, curList);

3



TC: $O(N \cdot 2^N)$

$$2^{10} = 1024 \approx 10^3$$

$$2^{20} \approx 10^6$$

$$N \cdot 2^N \Rightarrow \underline{\underline{N=30}}$$

$$\downarrow$$

$$\underline{\underline{\sim 10^9}} \times$$

$$N=10^6 \Rightarrow O(N)$$

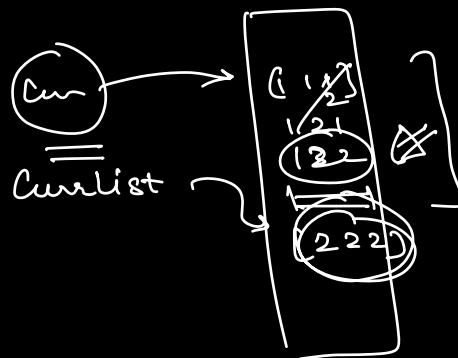
$$N=10^3 \Rightarrow N^2$$

$$N=20 \Rightarrow \text{Recursive}$$

or

Backtracking

111



CurList

~~111~~

121

[2222] [2222]

[111] [121] [122] ...

