

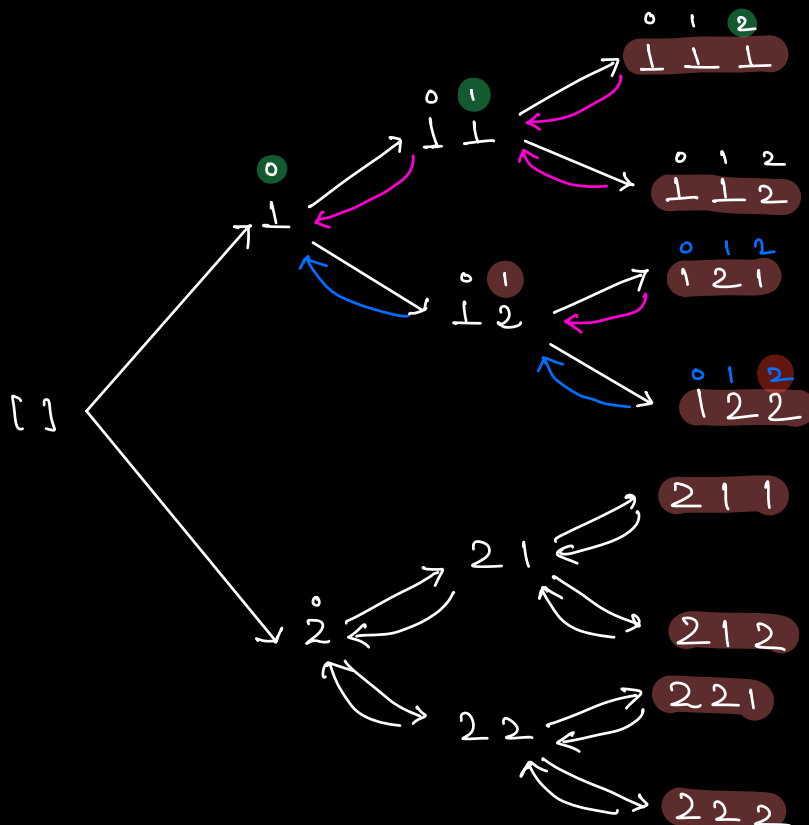
Backtracking  $\Rightarrow$  Try out all possibilities  
(Brute force)

Recursion + Backtrace

Q.1 Print all N digit numbers using {1, 2, 3}

$$\underline{\underline{N=1}} \Rightarrow \frac{1}{2}$$
$$\underline{\underline{N=3}} \quad \begin{bmatrix} \underline{1} & \underline{1} & \underline{1} \end{bmatrix}$$
$$\underline{\underline{N=2}} \Rightarrow \begin{array}{cc} \underline{1} & \underline{1} \\ \underline{1} & \underline{2} \\ \underline{2} & \underline{1} \\ \underline{2} & \underline{2} \end{array}$$

<u>1</u>	<u>2</u>	<u>1</u>
<u>1</u>	<u>2</u>	<u>2</u>
<u>2</u>	<u>1</u>	<u>1</u>
<u>2</u>	<u>1</u>	<u>2</u>
<u>2</u>	<u>2</u>	<u>1</u>
<u>2</u>	<u>2</u>	<u>2</u>

$$N=3 \quad \left( \frac{1}{2}, \frac{1}{2}, \frac{1}{2} \right)$$


```

void generateNumbers ( N, idx, currList ) {
    if ( idx == N ) {
        print ( currList );  $\Rightarrow O(N)$ 
        return;
    }

```

```

    3
    currList [ idx ] = 1
    generateNumbers ( N, idx + 1, currList );

```

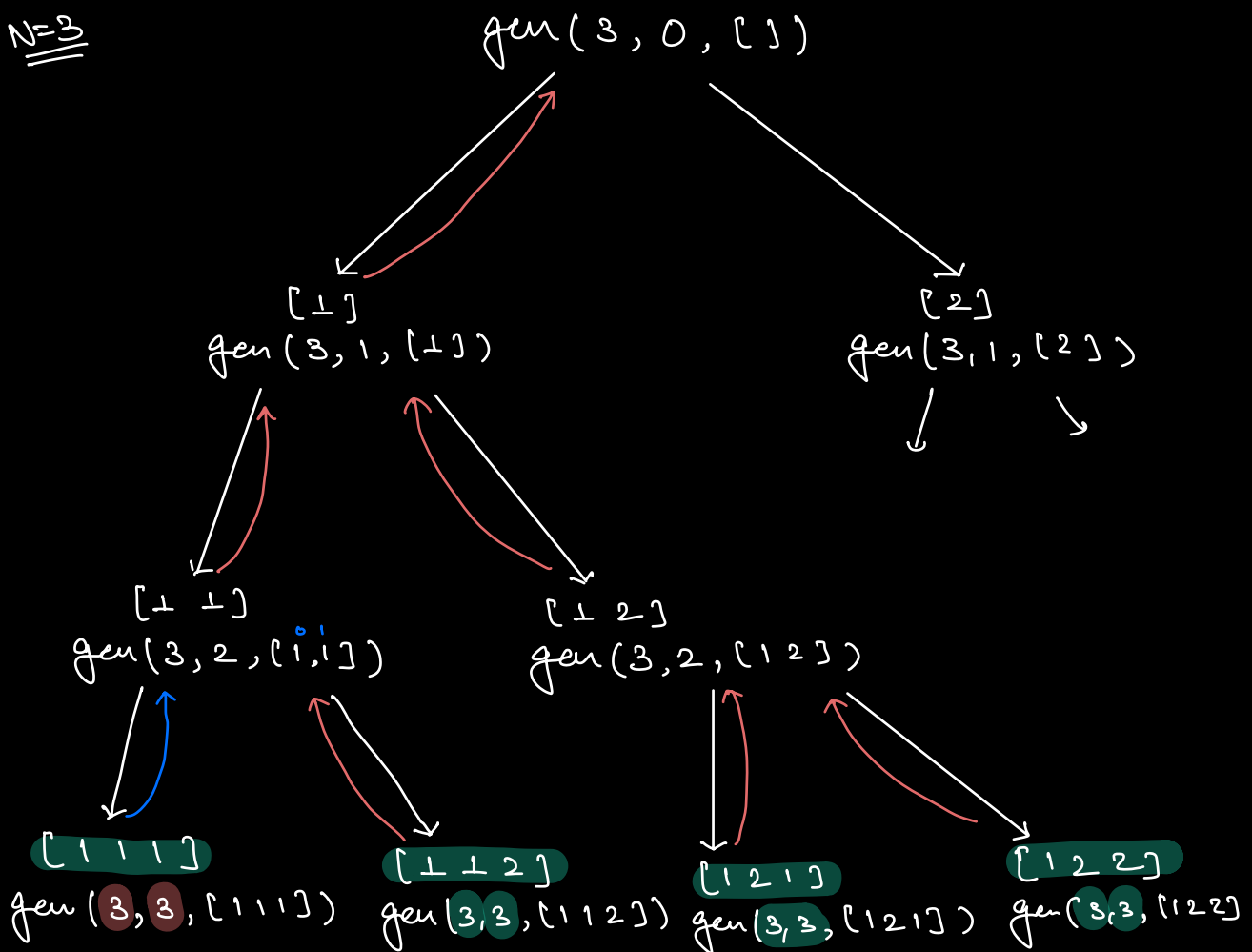
```

    Backtrack [ currList [ idx ] = 2
    generateNumbers ( N, idx + 1, currList );

```

3

N=3



Quiz      TC:

TC of a recursive fun<sup>n</sup>:

(# of recursive fun<sup>n</sup> calls) \* TC of each fun<sup>n</sup> call

↓

$$2^N * N$$

\*

$TC: O(N \cdot 2^N)$

$$SC: O(N)$$

\* Return a list of list

[ [1 1 1], [1 1 2], [1 2 1], [1 2 2], [2 1 1],  
[2 1 2], [2 2 1], [2 2 2] ]

list<list<int>> ans;

```

void generateNumbers ( N, idx, currList ) {
    if ( idx == N ) {
        ans.add(currList);  $\Rightarrow O(N)$ 
        return; reference.
        3
        currList[idx] = 1
        generateNumbers ( N, idx+1, currList );
        Backtrack currList[idx] = 2
        generateNumbers ( N, idx+1, currList );
        3
    }
}

```

ans: [ currList, currList, currList ]

[ 1 1 1 ]

2

ans: [ [2 2 2] [2 2 2] ... ]

\* HW

\* Hard Copy vs Soft Copy  $\Rightarrow$  Java

\* Deep Copy vs Shallow Copy

currList: [ 1 1 1 ]

temp: [ 1 1 1 ]

ans:

$$TC: O(N \cdot 2^N)$$

Q. Print all N digit numbers using {1, 2, 3, 4, 5}.

```
void generateNumbers (N, idx, currList) {
    if (idx == N) {
        print(currList);  $\Rightarrow O(N)$ 
        return;
    }
```

3  
currList[idx] = 1

generateNumbers(N, idx+1, currList);

currList[idx] = 2

generateNumbers(N, idx+1, currList);

currList[idx] = 3

generateNumbers(N, idx+1, currList);

currList[idx] = 4

generateNumbers(N, idx+1, currList);

currList[idx] = 5

generateNumbers(N, idx+1, currList);

5

for (i = 1; i <= 5; i++) {  
 currList[idx] = i;

generateNumbers(N, idx+1, currList);

3

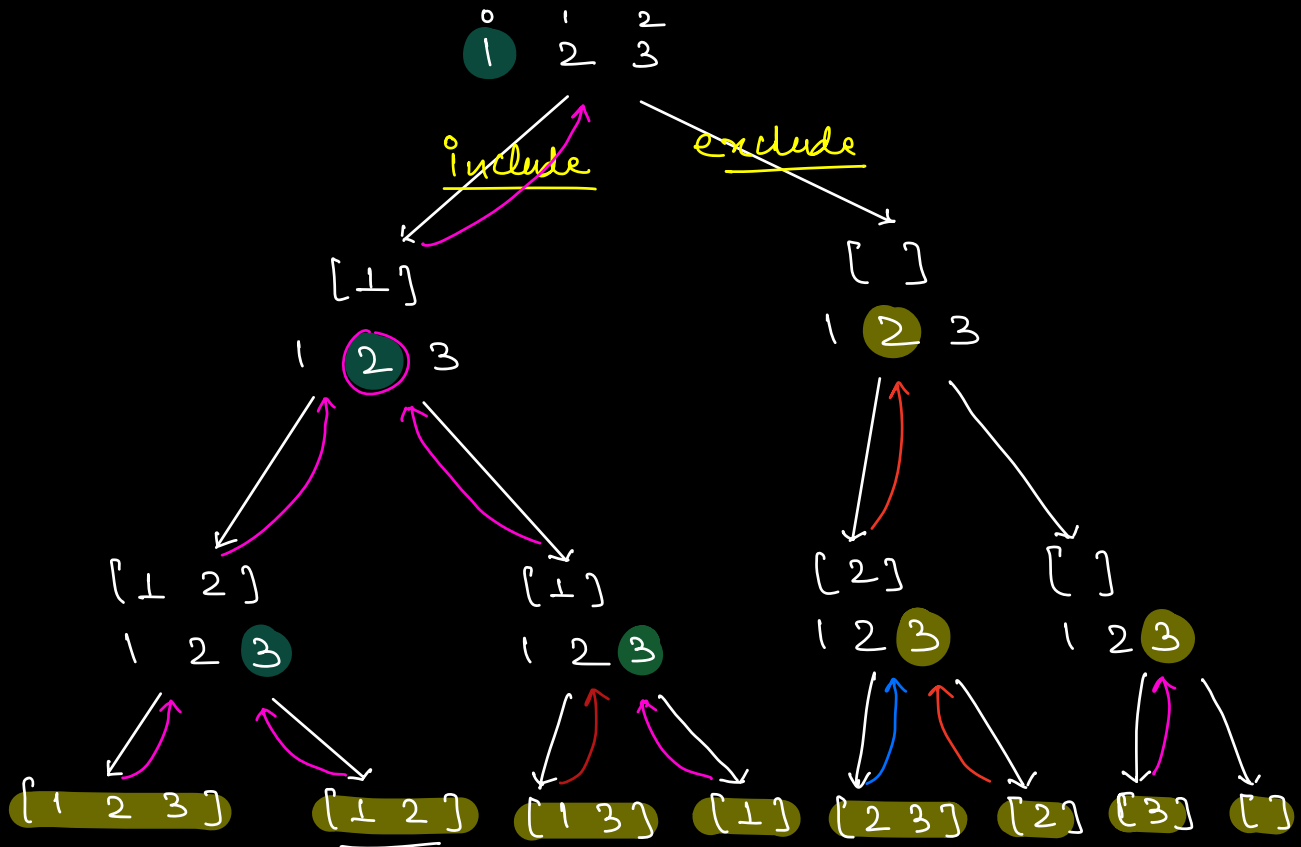
$$\underline{\underline{TC: O(N \cdot 2^N)}}$$

Q. Given an Array, generate all subsets of the Array.  
Amazon  
MS.  
----

A: [ 1 2 3 ]

[ ]  
 [ 1 ]  
 [ 2 ]  
 [ 3 ]  
 [ 1 2 ]  
 [ 1 3 ]  
 [ 2 3 ]  
 [ 1 2 3 ]

curlist: [ ]



No. of subsets  $\Rightarrow \underline{\underline{2^N}}$

```
void generateSubsets (A[], N, idx, curList) {  
    if (idx == N) {  
        print(curList);  
        return;  
    }
```

3

// Include A[idx] in the subset

curList.add(A[idx]);

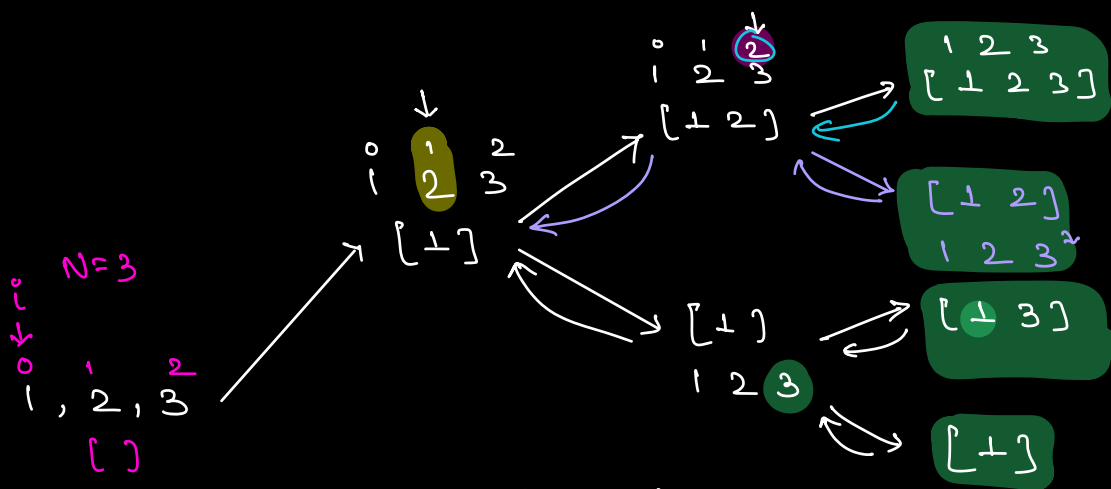
generateSubsets(A, N, idx+1, curList);

// Exclude A[idx] in the subset

curList.pop(A[idx]);

generateSubsets(A, N, idx+1, curList);

3



TC:  $O(N \cdot 2^N)$



$$2^{10} = 1024 \approx 10^3$$

$$2^{20} \approx 10^6$$

$$N \cdot 2^N \Rightarrow \underline{\underline{N=30}}$$

$$\downarrow$$

$$\underline{\underline{\sim 10^9}} \times$$

$$N=10^6 \Rightarrow O(N)$$

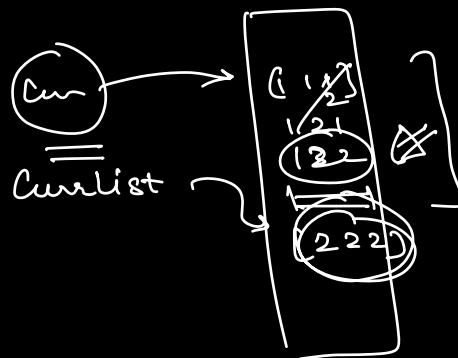
$$N=10^3 \Rightarrow N^2$$

$$N=20 \Rightarrow \text{Recursive}$$

or

Backtracking

110



[Cur]

~~11~~

121

[2222] [2222]

[111] [121] [122] ...

