```
safemath.sol
```

```
pragma solidity ^0.4.25;
* @title SafeMath
* @dev Math operations with safety checks that throw on error
library SafeMath {
 /**
 * @dev Multiplies two numbers, throws on overflow.
 function mul(uint256 a, uint256 b) internal pure returns (uint256) {
  if (a == 0) {
   return 0;
  }
  uint256 c = a * b;
  assert(c / a == b);
  return c;
 }
 /**
 * @dev Integer division of two numbers, truncating the quotient.
 function div(uint256 a, uint256 b) internal pure returns (uint256) {
  // assert(b > 0); // Solidity automatically throws when dividing by 0
  uint256 c = a / b;
  // assert(a == b * c + a % b); // There is no case in which this doesn't hold
  return c;
 }
 * @dev Subtracts two numbers, throws on overflow (i.e. if subtrahend is
greater than minuend).
 */
 function sub(uint256 a, uint256 b) internal pure returns (uint256) {
  assert(b <= a);
  return a - b;
 }
 * @dev Adds two numbers, throws on overflow.
 */
```

```
function add(uint256 a, uint256 b) internal pure returns (uint256) {
  uint256 c = a + b;
  assert(c >= a);
  return c;
 }
}
/**
* @title SafeMath32
* @dev SafeMath library implemented for uint32
library SafeMath32 {
 function mul(uint32 a, uint32 b) internal pure returns (uint32) {
  if (a == 0) {
   return 0;
  }
  uint32 c = a * b;
  assert(c / a == b);
  return c;
 }
 function div(uint32 a, uint32 b) internal pure returns (uint32) {
  // assert(b > 0); // Solidity automatically throws when dividing by 0
  uint32 c = a / b;
  // assert(a == b * c + a % b); // There is no case in which this doesn't hold
  return c;
 }
 function sub(uint32 a, uint32 b) internal pure returns (uint32) {
  assert(b <= a);
  return a - b;
 }
 function add(uint32 a, uint32 b) internal pure returns (uint32) {
  uint32 c = a + b;
  assert(c >= a);
  return c;
 }
}
/**
* @title SafeMath16
* @dev SafeMath library implemented for uint16
library SafeMath16 {
```

```
function mul(uint16 a, uint16 b) internal pure returns (uint16) {
  if (a == 0) {
   return 0;
  }
  uint16 c = a * b;
  assert(c / a == b);
  return c;
 }
 function div(uint16 a, uint16 b) internal pure returns (uint16) {
  // assert(b > 0); // Solidity automatically throws when dividing by 0
  uint16 c = a / b;
  // assert(a == b * c + a % b); // There is no case in which this doesn't hold
  return c;
 }
 function sub(uint16 a, uint16 b) internal pure returns (uint16) {
  assert(b <= a);
  return a - b;
 }
 function add(uint16 a, uint16 b) internal pure returns (uint16) {
  uint16 c = a + b;
  assert(c >= a);
  return c;
 }
}
```