

## 1. To handle the data:

- a) Converted 'GBp' to 'GBP' in the London data
- b) Removed the dates that were not there in either one of the datasets
- c) Converted both the datasets to prices in USD for that particular day for better development of the model.

### Model:

- a) Split the datasets into 60-40 train-test ratio in order to make sure the model works for fresh data
  - b) The rationale behind the model is to use **Pair Trading** which is a Market Neutral Statistical Arbitrage Strategy. We see that the two stocks are of the same company, so pair trading would be useful.
  - c) In order to get this working, we first check the correlation of the prices of the datasets (  $> 0.9$ ).
  - d) Now, the important part is that time series data of stocks is generally because of a trend, so we need to check if there is **co-integration between the stock prices**. That means, even though the stock prices are non-stationary, a linear combination of it is stationary.
  - e) Given that the linear combination of the stock prices is stationary, we run a regression to find the predicted London Stock Price from the Australian one.
  - f) Then we trade on the residual of the OLS regression, because we know that the **residual will oscillate around the mean**.
  - g) Each time we trade, **we create a perfectly hedged trade**, with 100 London Stocks and taking the other position in the equivalent amount of Australian Stock for the day.
  - h) The model assumes **no transaction cost** for trades and being able to **buy fraction number of stocks** to perfectly hedge the position
2. To validate the model, we split the data into training and test sets.  
For each set, first we check:
- a) If the **correlation** between the London and Australian stocks is high enough ( $> 0.9$ )
  - b) We check with a significance level of 10%. Null hypothesis is that there is no co-integration. **We use the Engle and Granger approach built in in python to check for co-integration**. We only move ahead by rejecting the null if the p value  $< 0.1$ , since co-integration is an important factor.
  - c) We check if the **OLS regression** run on the stock prices is statistically significant  
 $|t| > 1.65$ , at the 10% significance level.  
Y -> London Stock

X -> Australian Stock

We use **robust** Standard Error to account for heteroscedasticity

- d) We check if the **residuals are normally distributed**. Null Hypothesis being that the residuals are normal.

We only move ahead by failing to reject the null if the p value > 0.1, since only then can we use the Z-score

Training set

Co integration check: True

P value: 0.000108627093269

Correlation Coeff: 0.994027035021

OLS t-statistic: 864.586593585

P-value for normality check: 0.468346327566

Residuals are normally distributed: True

Test set

Co integration check: True

P value: 0.0988375144002

Correlation Coeff: 0.944560345704

OLS t-statistic: 618.300602053

P-value for normality check: 0.530123526821

Residuals are normally distributed: True

3. The parameters in my strategy are:

- a) **To Long London stock and Short Australian:**

If the **residual is less than 1 standard deviation below the mean**, that means that London stock is undervalued or Australian is overvalued.

Importantly, we create a perfectly hedged trade, where we long 100 London Stocks, and short equivalent ratio of Australian stocks

- b) **To Short London stock and Long Australian:**

If the **residual is more than 1 standard deviation above the mean**, that means that London stock is overvalued or Australian is undervalued.

Importantly, we create a perfectly hedged trade, where we short 100 London Stocks, and long equivalent ratio of Australian stocks

- c) **Exit the position:**

When the residual is **between 0.25 SD of the mean**.

**d) Stop Loss:**

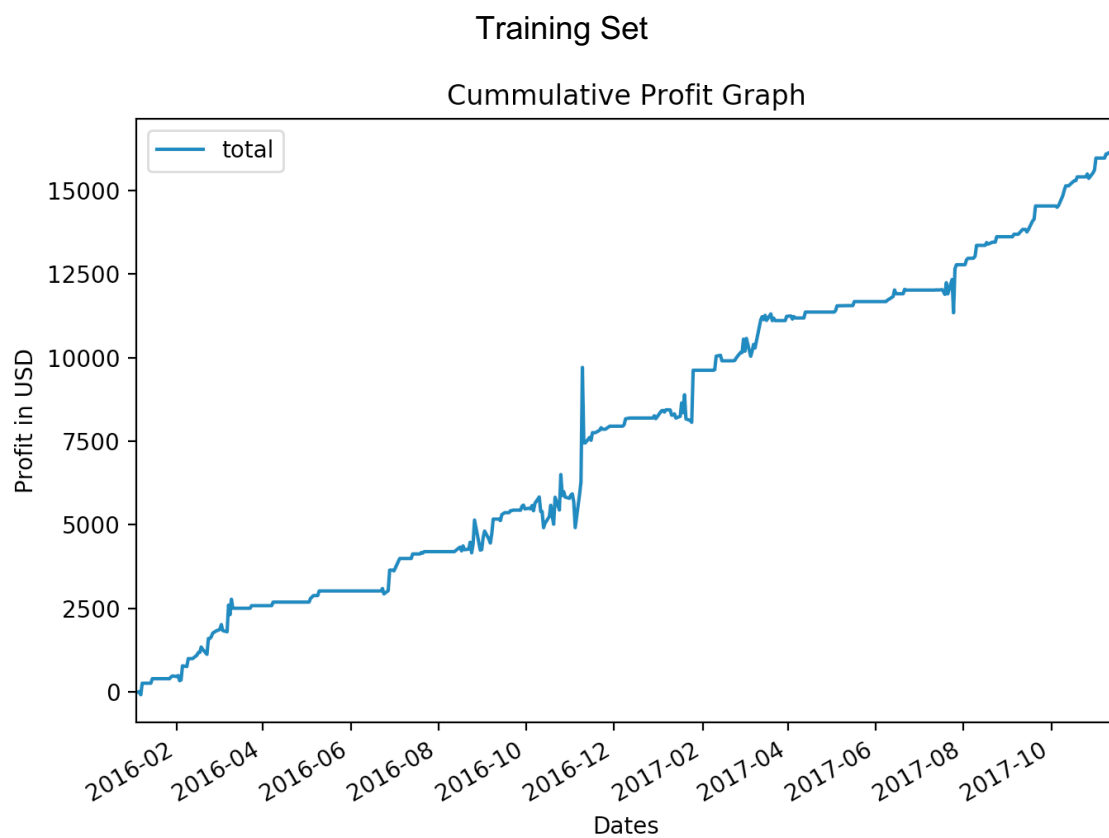
To prevent humungous losses, we exit our position if it is **more than 3 SD on either side of the mean**.

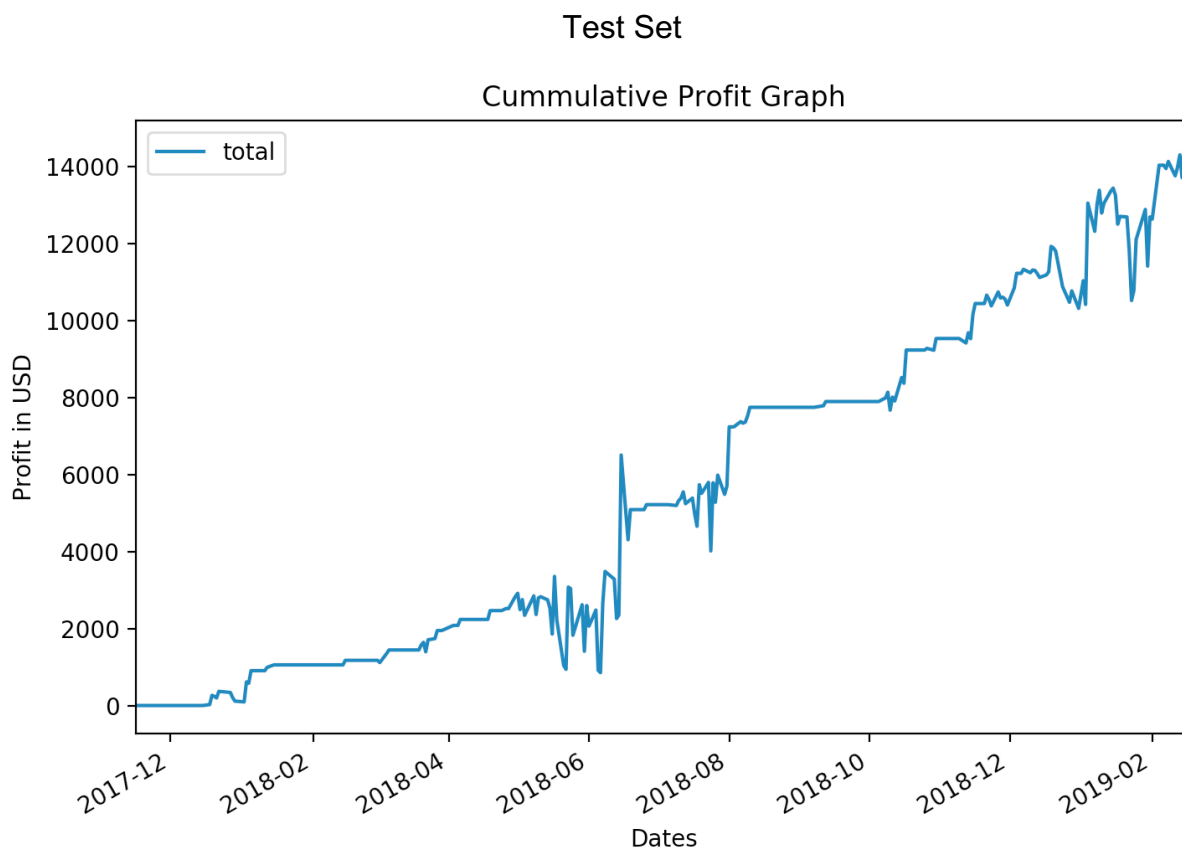
To come up with these numbers, I mainly used a graph to see how much the residual is oscillating around the mean, along with some trial and error on the training set

**4. Important Note:**

Since in the pair trading strategy I am using, **I start off with 0 capital** because for every long and short, the amount is perfectly hedged, I am not being able to gauge the return on the investment since the starting capital is 0, and thus cannot calculate the other parameters like the Sharpe Ratio etc.

I have attached the profit graph that is being generated for the strategy where according to the signals mentioned in point 3 above.





**5. Limitations:**

- a) The model does not account for transaction cost for trades
- b) Assumption of being able to buy fraction number of stocks to perfectly hedge the position
- c) Because of small dataset, only using 10% significance level instead of 5%.

**Risks:**

- a) Forex risk because the entire model is based on USD
- b) Execution Risk because we need to long and short simultaneously
- c) Australian Market opens before the London Market

6. In order to improve my model further, I would try to get more data, in order to use a better significance level to be more confident about my results.  
I would also try to get the dividend information to calculate the adjusted close price instead of the normal close price.