

Foundations of Data Privacy

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Why Privacy Matters

- Organizations collect vast amounts of personal data: health, finance, location, online activity \implies important to preserve privacy of individual data
- Anonymized datasets can be re-identified

Anonymity and the Netflix Dataset

Last year, Netflix published 10 million movie rankings by 500,000 customers, as part of a challenge for people to come up with better recommendation systems than the one the company was using. The data was anonymized by removing personal details and replacing names with random numbers, to protect the privacy of the recommenders.

Arvind Narayanan and Vitaly Shmatikov, researchers at the University of Texas at Austin, [de-anonymized some of the Netflix data](#) by comparing rankings and timestamps with public information in the [Internet Movie Database](#), or IMDb.

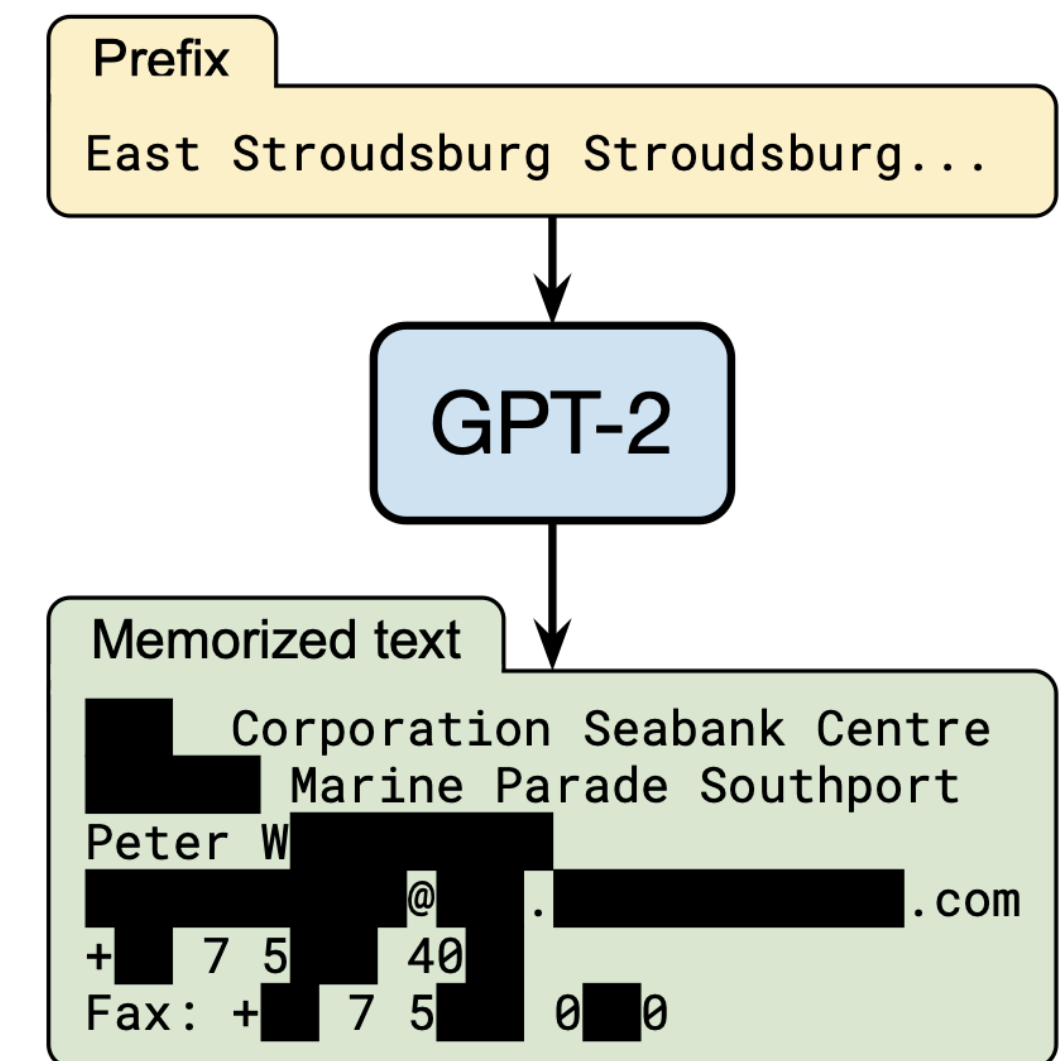
Why Privacy Matters

- In machine learning, large language models (LLMs) can leak private data

Extracting Training Data from Large Language Models

Nicholas Carlini ¹	Florian Tramèr ²	Eric Wallace ³	Matthew Jagielski ⁴
Ariel Herbert-Voss ^{5,6}	Katherine Lee ¹	Adam Roberts ¹	Tom Brown ⁵
Dawn Song ³	Úlfar Erlingsson ⁷	Alina Oprea ⁴	Colin Raffel ¹

- Data privacy laws like General Data Protection Regulation and California Consumer Protection Act mandate privacy of individual data



Building Towards a Definition of Privacy

- How can one learn about population of data whilst preserving individual level privacy?
- Thought experiments:
 - If we take a lot of individuals and release a statistic, then the influence of one person's data becomes considerably low \implies data privacy is inherent when population is high?
 - NO! Consider the following scenario...

Building Towards a Definition of Privacy

Data Curator

x_1, x_2, \dots, x_n

n

m_1

m_2

How many points
do you have?

Give me the mean
of those points

Remove any one
point and return the
mean again

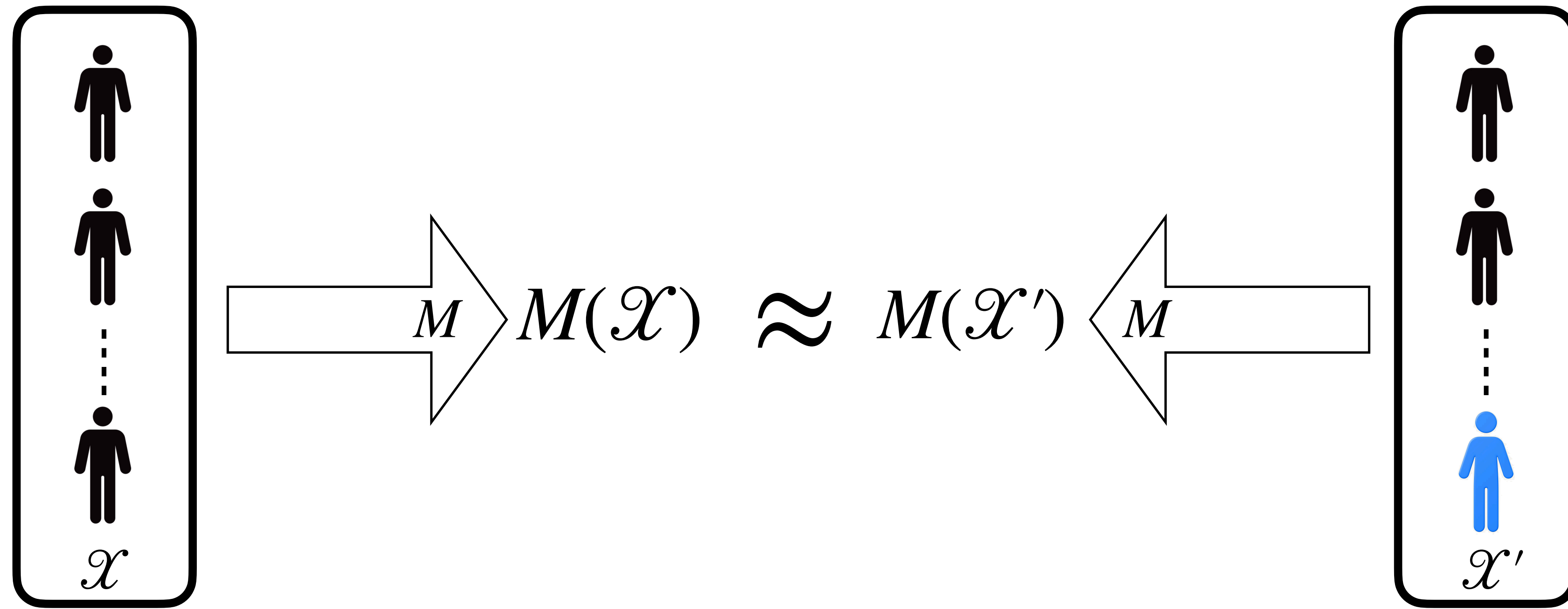
One of your points
is $nm_1 - (n - 1)m_2$

Adversary

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- How can one learn about population of data whilst preserving individual level privacy?
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 - NO! Consider mean of n data points...
- **Goal:** Ensure that the output of an analysis does not noticeably change whether any one person's data is included or not.

Differential Privacy



- A randomized algorithm M is (ϵ, δ) **differentially private** if for every databases \mathcal{X} and \mathcal{X}' which differ by one entry ($\mathcal{X} \sim \mathcal{X}'$) and all $S \subseteq \text{Range}(M)$

$$\Pr[M(\mathcal{X}) \in S] \leq e^\epsilon \Pr[M(\mathcal{X}') \in S] + \delta$$

Differential Privacy: Some Features

- **In simple terms:** Your data does not have a significant influence on the distribution of the result.
- ϵ (epsilon): Privacy loss. Smaller is better
- δ (delta): Probability of a “failure” of privacy
- It is immune to any kind of data independent post processing
- Can be achieved by adding a carefully decided amount of noise?
 - In the mean example, if the curator simply adds some zero mean Gaussian noise to its answers \implies much much tougher for the adversary to guess the exact number

Real World Applications and Deployments

- **US Census:** DP is used in releasing Census data
- **Apple:** Uses DP for keyboard suggestions
- **Google:** Chrome data collection uses local DP
- **Meta, Microsoft:** Research and product applications

<https://machinelearning.apple.com/research/differential-privacy-aggregate-trends>

<https://www.census.gov/programs-surveys/decennial-census/decade/2020/planning-management/process/disclosure-avoidance/differential-privacy.html>

<https://developers.googleblog.com/en/sharing-our-latest-differential-privacy-milestones-and-advancements/>

<https://engineering.fb.com/2022/06/14/production-engineering/federated-learning-differential-privacy/>

<https://blogs.microsoft.com/ai-for-business/differential-privacy/>