

## Stack

### Stack Example

#### 1) Polish Notation

There are three types of Notation

- 1) Infix Notation  $(A+B)$
- 2) Prefix Notation  $(+AB)$
- 3) Postfix Notation  $(AB+)$

How to Convert Infix to Postfix

- 1) Solve brackets or Parentheses
- 2) Solve Exponent or Power  $(^ or \uparrow)$
- 3) Solve multiply or Divide [Left To Right].
- 4) Solve Addition or Subtract [Left to Right].

Convert this infix to Postfix

1<sup>st</sup> way  $(A+B) * C / D - E$

Solution:-

$$(A+B) * C / D - E$$

$$(AB+) * C / D - E$$

$$T * C / D - E$$

$$(TC*) / D - E$$

$$M / D - E$$

$$(MD/) - E$$

$$K - E$$

$$T = AB+$$

$$M = TC*$$

$$K = MD/$$

$$\begin{aligned}
 &\Rightarrow KE - \\
 &\Rightarrow MD | E - \\
 &\Rightarrow TC * D | E - \\
 &\Rightarrow \boxed{AB + C * D | E -}
 \end{aligned}$$

II<sup>nd</sup> way

$$(A+B) * C | D - E$$

step	Symbol Scanned	Stack	Expression
1	(	(	
2	+	( +	
3	B	( + B	
4	)	(	AB +
5	*	( *	AB +
6	C	( * C	AB + C
7		( * C	AB + C *
8	D	( * C   D	AB + C * D
9	-	( * C   D -	AB + C * D -
10	E	( * C   D - E	AB + C * D   E
11	)		$\boxed{AB + C * D   E -}$

Solve this Infix to Postfix

12, 4, /, 5, 4, +, \*, 9, /

input	Action	stack	Intermediate Result
12	Push	12	
4	Push	12, 4	
/	Pop 2 operand Push Result	Empty 3	$12/4 = 3$
5	Push	3, 5	
4	Push	3, 5, 4	
+	Pop 2 operand Push Result	3 9	$5+4 = 9$
*	Pop 2 operand Push Result	Empty 27	$9*3 = 27$
9	Push	27, 9	
/	Pop 2 operand Push Result	Empty 3	$27/9 = 3$

0/P = 3



Convert this infix Expression to Post fix.

$$(A + (B * C - (D / E \uparrow F) * G) * H)$$

Step	Symbol & comment	Stack	Expression
1	A	(	A
2	+	( +	A
3	(	( + (	
4	B	( + ( B	AB
5	*	( + ( * B	AB*
6	C	( + ( * C	ABC
7	-	( + ( -	ABC*
8	(	( + ( - (	ABC*
9	D	( + ( - ( D	ABC* D
10	/	( + ( - ( /	ABC* D
11	E	( + ( - ( / E	ABC* D E
12	↑	( + ( - ( / ↑	ABC* D E
13	F	( + ( - ( / ↑ F	ABC* D E F
14	)	( + ( -	ABC* D E F ↑
15	*	( + ( - *	ABC* D E F ↑
16	G	( + ( - * G	ABC* D E F ↑ G
17	)	( +	ABC* D E F ↑ G *
18	*	( + *	ABC* D E F ↑ G * -
19	H	( + * H	ABC* D E F ↑ G * - H
20	)		ABC* D E F ↑ G * - H * +

Evaluate the following Expression in Post fix form using a stack

True, false, true, not, false, true, or, not and, or, and

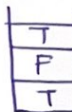
1) true is an operand  
Push onto Stack



2) false is an operand  
push onto stack



3) true



4) not operator

Pop 1 operand

Not True  $\Rightarrow$  false



5) false



6) True



7)

or is an operator

not 2 operands

T or F  $\Rightarrow$  T



8 Not operator

F
F
F
T

9 and

F
F
T

10 or

F
T

11 and

F
---

Ans



# Stack

10.4  $(A + ((B + C) + (D + E) * F)) / G$

step	Symbol Scanned	stack	Expression
1	A	(	A
2	+	( +	A +
3	(	( + (	A + (
4	(	( + ((	A + ((
5	B	( + ((	A B
6	+	( + (( +	A B +
7	C	( + (( +	A B C
8	)	( + (	A B C +
9	+	( + ( +	A B C +
10	(	( + ( + (	A B C +
11	D	( + ( + (	A B C + D
12	+	( + ( + ( +	A B C + D +
13	E	( + ( + ( +	A B C + D E
14	)	( + ( +	A B C + D E +
15	*	( + ( + *	A B C + D E +
16	=	( + ( + *	A B C + D E + F

17 ) (+  $ABC + DE + F * +$   
18 / (+/  $ABC + DE + F * + *$   
19 G (+/  $ABC + DE + F * + G$   
20 )  $ABC + DE + F * + G / +$

[4, 10, 5, +, \*, 15, 3, /, -]

input	Action	stack	
4	Push	4	
10	Push	4, 10	
5	Push	4, 10, 5	
+	Pop 2 operand	4, 15	$10 + 5 = 15$
*	Pop 2 operand	60	$4 * 15 = 60$
15	Push	60, 15	
3	Push	60, 15, 3	
/	Pop 2 operand	60, 5	$15 / 3 = 5$
-	Pop 2 operand	55	$60 - 5 = 55$



$$+ 15 + 10 \quad 15 \quad 3 \quad 2 + 17 + 2 \quad *$$

15

15

3

15, 3

2

15, 3, 2

+

15, 5

$$3+2=5$$

1

-

3

$$15/5=3$$

7

3, 7

+

10

$$3+7=10$$

2

10, 2

20

F, T, Not, AND, E, OR, T, AND

F

F

T

F

F

T

F

F

→ E

F

ABC \* DEF

)

( \* (-

ABC \* DEF ↑

\*

( \* ( \* - \*

ABC \* DEF ↑ / G

G

( \* + \*

ABC \* DEF A / G \* -

)

\* +

50, 60, +, 20, 10, -, \*

50  
60  
+  
20  
10  
-  
\*

50  
50, 60  
110  
110, 20  
110, 20, 10  
110, 10  
1100

F, T, NOT, OR, AND, XOR

$\begin{bmatrix} T \\ F \end{bmatrix}$   $\begin{bmatrix} F \\ F \end{bmatrix}$   $\begin{bmatrix} F \\ F \end{bmatrix}$   $\begin{bmatrix} T \\ F \end{bmatrix}$   $\begin{bmatrix} F \\ F \end{bmatrix}$   $\begin{bmatrix} F \\ F \end{bmatrix}$   $\begin{bmatrix} F \\ F \end{bmatrix}$

$(A + (B * C - (D \vee E \wedge F) * G) * H)$

(	(	A
A	(	A
+	(+	A
B	(+	AB
*	(*	AB*
C	(*	AB*+
(	(+	A
B	(+	AB
*	(+*	AB
C	(*(*	ABC
-	(*(-	ABC*
(	(*(- (	ABC*
D	(*(- (	ABC* D
/	(*(- (/	ABC* D
E	(*(- (/	ABC* DE
↑	(*(- (/ ↑	ABC* DE

Q

$$((A+B) \times C) / D$$

	(	A
+	(+	A
B	(	AB
)	(	AB+
x	*	AB+
C	*	AB+C
/	(/	AB+C*
D	(/	AB+C*D
)		AB+C*D/

Q

$$((A+B) \times C) / D + (E \times F) / G$$

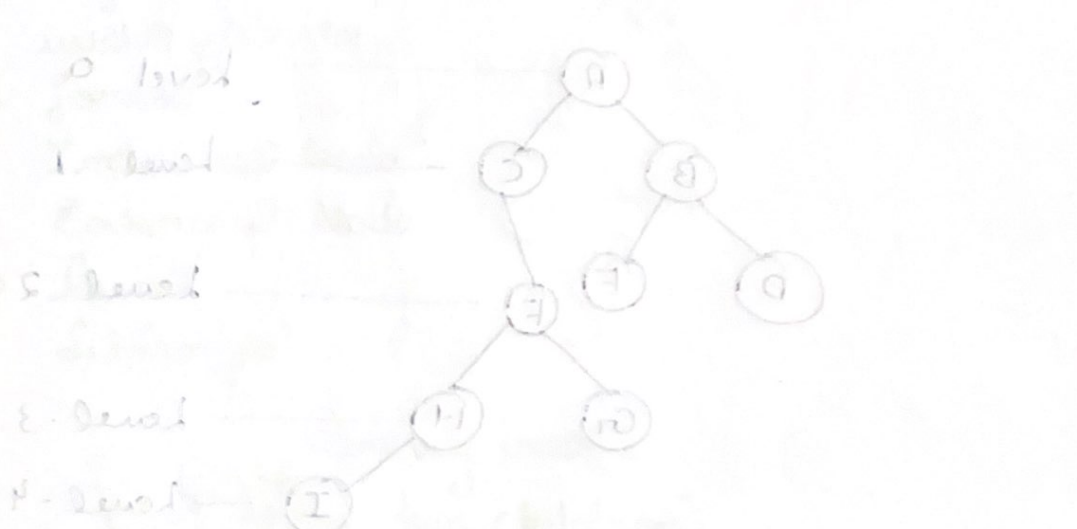
	(	A
+	(+	A
B	(	AB
)	(	AB+
C	*	AB+C
/	(/	AB+C
D	(/	AB+CD
+	+	AB+CD+
E	*	AB+CD+
F	*	AB+CD+
/	(/	AB+CD+
G	(/	AB+CD+
)		AB+CD+



$E$   $(+)$   $AB + C * D / E$   
 $\uparrow$   $C \uparrow$   $AB + C * D / E$   
 $F$   $AB + C * D / E$

A tree diagram is a hierarchical structure.

A tree diagram is a hierarchical structure.



A tree diagram is a hierarchical structure.

