

Greedy Method:

The greedy method is perhaps (maybe or possible) the most straight forward design technique, used to determine a feasible solution that may or may not be optimal.

Feasible solution:- Most problems have n inputs and its solution contains a subset of inputs that satisfies a given constraint(condition). Any subset that satisfies the constraint is called feasible solution.

Optimal solution: To find a feasible solution that either maximizes or minimizes a given objective function. A feasible solution that does this is called optimal solution.

The greedy method suggests that an algorithm works in stages, considering one input at a time. At each stage, a decision is made regarding whether a particular input is in an optimal solution.

Greedy algorithms neither postpone nor revise the decisions (ie., no back tracking).

Example: Kruskal's minimal spanning tree. Select an edge from a sorted list, check, decide, and never visit it again.

Application of Greedy Method:

1. Job sequencing with deadline
2. 0/1 knapsack problem
3. Minimum cost spanning trees
4. source shortest path problem

Algorithm for Greedy method

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Algorithm Greedy(a,n)

//a[1:n] contains the n inputs.

{

Solution :=0;

For $i=1$ to n do

{

$X:=\text{select}(a);$

If Feasible(solution, x) then

Solution :=Union(solution, x);

}

Return solution;

}

...

Selection Function, that selects an input from $a[]$ and removes it. The selected input's value is assigned to x .

Feasible Boolean-valued function that determines whether x can be included into the solution vector.

Union function that combines x with solution and updates the objective function.

Knapsack problem:

The knapsack problem or rucksack (bag) problem is a problem in combinatorial optimization: Given a set of items, each with a mass and a value, determine the number of each item to include in a collection so that the total weight is less than or equal to a given limit and the total value is as large as possible.

There are two versions of the problems

1. 0/1 knapsack problem
2. Fractional Knapsack problem
 - a. Bounded Knapsack problem.
 - b. Unbounded Knapsack problem

Solutions to knapsack problems

Brute-force approach:-Solve the problem with a straight forward algorithm

Greedy Algorithm:- Keep taking most valuable items until maximum weight is reached or taking the largest value of eac item by calculating $v_i = \text{value}_i / \text{Size}_i$

Dynamic Programming:- Solve each sub problem once and store their solutions in an array.

Greedy algorithm for knapsack.

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Algorithm GreedyKnapsack(m,n)

// p[1:n] and [1:n] contain the profits and weights respectively

// if the n-objects ordered such that $p[i]/w[i] \geq p[i+1]/w[i+1]$, m size of knapsack and x[1:n] the solution vector

{

For i:=1 to n do x[i]:=0.0

U:=m;

For i:=1 to n do

{

if($w[i] > U$) then break;

x[i]:=1.0;

U:=U-w[i];

}

If($i \leq n$) then x[i]:=U/w[i];

}

...