

PCA (Principal Component Analysis).

* Data preprocessing, Dimensionality Reduction
Alternative - LDA, TSME.

$x_1, x_2, x_3, x_4, \dots, x_{100}$

- Time complexity
- Difficult to generalise a data/relation.
- All the time all features aren't going to contribute.
- Hard to find shape of data.

Solⁿ - Dimensionality Reduction.

DR:- Trying to convert dataset in another axis such that it retains original meaning of data.

Step-1 take dataset $x_1, x_2 \rightarrow C$
 $\mu=0, \sigma=1$

$$Z = \frac{x - \mu}{SD} \quad (\text{Standard normal dist.})$$

Step-2 Draw single straight line explaining data.

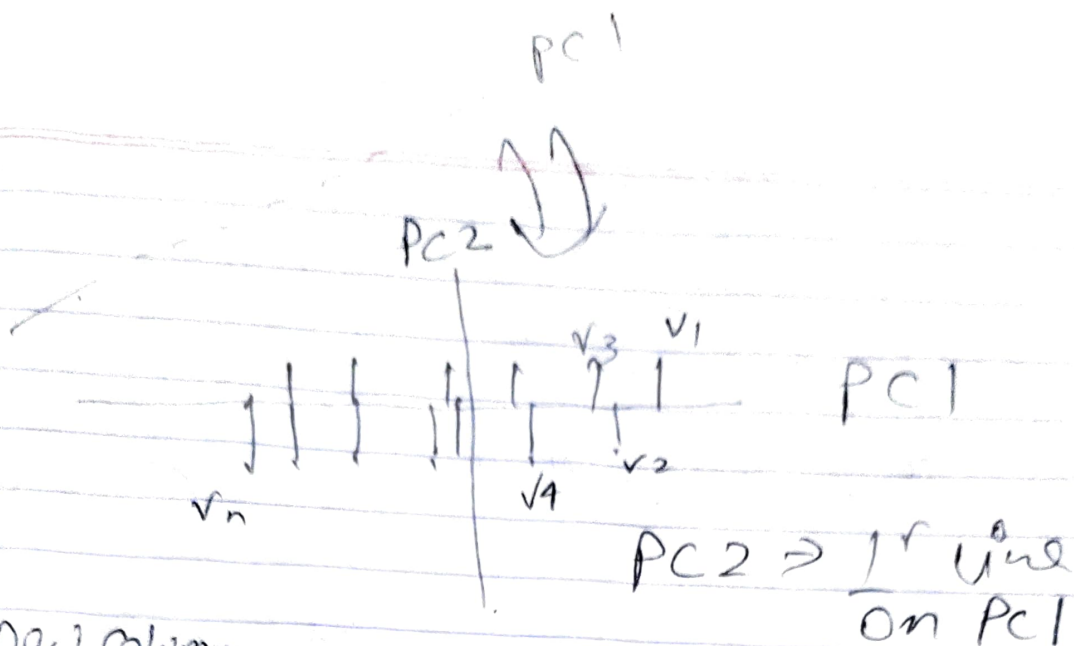
(Implement Linear regression such that residual minimum).

$$x_2 = mx_1 + c$$

or $x_1 = mx_2 + c$

(Principal component 1)
Line ϕ ?

Step-3



New Column

v_1
 v_2
 \vdots
 v_n

\Rightarrow Combination of x_1 & x_2

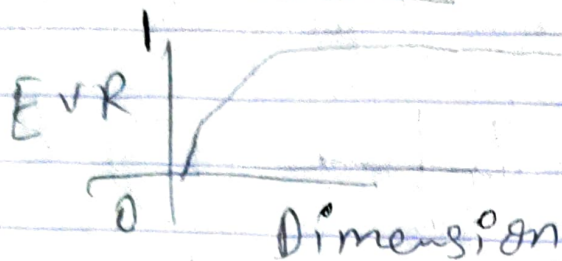
PC1 (High Priority)

How many ~~PCR~~ lines \Rightarrow EVR (Explained Variance Ratio)

EVR = How many features one PC1 line can explain?

$$EVR(PC1) = \frac{\text{Distance of PC1 Points}}{\text{Distance of PC1} + \text{Distance of PC2}}$$

Screen plot



$$\text{Cov}_{C_1, C_2} = \sum_{k=0}^{m-1} (C_1 - \bar{C}_1) (C_2 - \bar{C}_2)$$

$m-1$

$$\frac{A^T A}{m-1} = \text{Cov}$$

$$T(V) = \lambda V$$

\downarrow
Eigen value

\rightarrow Eigen vector

$$\lambda \uparrow \Rightarrow PC1$$
$$=$$

$$1^{\text{st}} \text{ P. Analg. Eig (Cov)}$$

Rotation
when multiplied
by λ .