

## Problem

The proof of Lemma 2.41 says that  $(q, x)$  is a *looping situation* for a DPDA  $P$  if when  $P$  is started in state  $q$  with  $x$  ?

$\Gamma$

## Step-by-step solution

### Step 1 of 4

A language  $Q$  is said to be **decidable** if a Turing machine (which is also called as decider)  $M$  exists in which  $Q$  is **accepted** and **halts on every string input**. A language, that is decidable, is also known as a recursive language.

• Now, consider a string  $l$ , then for any string  $l$ , there exist the following condition:

- $l \in Q \Rightarrow M$ , **Halts in a state of accepting**.
- $l \notin Q \Rightarrow M$ , **halts in a state of non-accepting**.

It is also known that “each language which is decidable is also **Turing-acceptable**”.

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### Step 2 of 4

It is already known that “A looping condition for a DPDA (Deterministic Push Down Automata)  $P$  is  $(q, x)$  if state  $q$  is the starting point of  $P$  with  $x \in \Gamma$  which exists on the stack's top and everything under  $x$  is never popped. Also, an input symbol is never be read”.

• The above given problem of looping can be solved by identifying the looping situation. In other words, “only in which no further inserted symbol is ever read and re-programming DPDA. Therefore, instead of looping, it rejects and reads the input.

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### Step 3 of 4

The situation arises above, produces a halt situation. The following algorithm explained it more carefully:

$T =$  “On input  $\langle B \rangle$ , where  $B$  is DFA:

1. Initial state of  $B$  is marked.
2. Repeat this till a marked on new state:
3. Mark a position on which a **transition exists** in to it from any other state which is marked already.
4. If none of the state is marked as accepted state, it will be **accepted**; otherwise, **rejected**”

The above algorithm produces a halt situation for accept and non-accept state.

[Comments \(3\)](#)

### Step 4 of 4

Now consider a language  $F$ , which is defined as  $F = \{ \langle P, q, x \rangle \mid (q, x) \text{ is a situation of looping for } P \}$ . Therefore, from the above discussion it can be said that “the above given language  $F$  is a decidable language”.

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