

Problem

Let $CNF_H = \{ \langle \phi \rangle \mid \phi \text{ is a satisfiable cnf-formula where each clause contains any number of literals, but at most one negated literal} \}$. Show that $CNF_H \in P$.

Step-by-step solution

Step 1 of 5

$CNF_H = \{ \langle \phi \rangle \mid \phi \text{ is a satisfiable cnf-formula where each variable appears in at most } k \text{ places} \}$ Hence, $CNF_H \in P$ can be proved by using following approach:

Situation is quite clear as all user needs to find the **dependability** of CNF on P and NP .

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Step 2 of 5

Consider the following algorithm which can be used for this language:

$N = \text{"On input } \langle \phi \rangle \text{ where } \phi \text{ is a boolean formula in cnf"}$

1. If ϕ don't consists a unit clause $(\sim x)$, assume every literals x will be 1 and $(\sim x)$ will be 0 and accept.
2. Repetition performed until these exists no new $(\sim x)$ unit clause:
3. If ϕ consist a unit clause $(\sim x)$, remove each clauses that contains $(\sim x)$ from ϕ and remove every occurrences of x from the clause in ϕ .
4. If an empty clause is exists in ϕ , reject.
5. Let every literals x in ϕ be 1, $(\sim x)$ be 0 and accept.

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Step 3 of 5

Dependability can be viewed as:

1. Consider that $CNF_2 \in P$

Consider first situation of ϕ and consider it belongs to some x and if there is any $\neg x$ then reject. Consider one more situation of ϕ that will be belonging to some other variable let's say y and here situation will rejected if there is any $\neg y$ otherwise accepted.

• **Two situations are discussed here remove those situation from ϕ and relate those two situations, let's say M and N, to ϕ and call the result.**
This way it is proved that $CNF_2 \in P$.

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Step 4 of 5

2. Consider another situation $CNF_3 \in P$

Consider first situation of ϕ and consider it belongs to some p and if there is any $\neg p$ then reject. Consider one more situation of ϕ that will be belonging to some other variable, let's say q and r here situation will rejected if there is any $\neg q$ otherwise accepted.

• Two situations are discussed here remove those situation from ϕ and relate those two situations, let's say A and B, to ϕ and call the result.
This way it is proved that $\text{CNF}_3 \in \mathbf{P}$.

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Step 5 of 5

Similarly, this situation will be held true for $\text{CNF}_n \in \mathbf{P}$.

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