

Problem

Recall the CFG G_4 that we gave in Example 2.4. For convenience, let's rename its variables with single letters as follows.

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T \times F \mid F \\ F &\rightarrow (E) \mid a \end{aligned}$$

Give parse trees and derivations for each string.

- a. a
- b. a+a
- c. a+a+a
- d. ((a))

Step-by-step solution

Step 1 of 8

Given Grammar G_4 is

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T \times F \mid F$$

$$F \rightarrow (E) \mid a$$

Derivation: The sequence of substitutions to obtain a string is called a *derivation*.

Parse Tree: The pictorial representation of derivation of a string is a *parse tree*.

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Step 2 of 8

a)

The parse tree to generate string a is as follows:

$$\begin{array}{c} E \\ | \\ T \\ | \\ F \\ | \\ a \end{array}$$

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Step 3 of 8

The derivation for the string a is as follows:

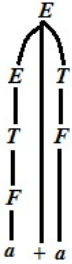
$E \Rightarrow T$
 $E \Rightarrow F$
 $E \Rightarrow a$

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Step 4 of 8

b)

The parse tree to generate string $a + a$ is as follows:



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The derivation for the string $a + a$ is as follows:

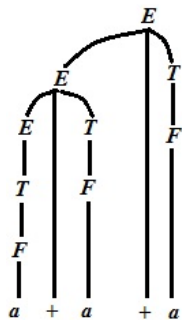
$E \Rightarrow E + T$
 $E \Rightarrow T + T$
 $E \Rightarrow F + T$
 $E \Rightarrow a + T$
 $E \Rightarrow a + F$
 $E \Rightarrow a + a$

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c)

The parse tree to generate string $a + a + a$ is as follows:



The derivation for the string $a + a + a$ is as follows:

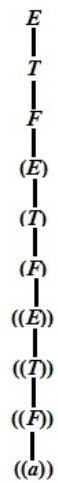
$E \Rightarrow E + T$
 $E \Rightarrow E + T + T$
 $E \Rightarrow T + T + T$
 $E \Rightarrow F + T + T$
 $E \Rightarrow a + T + T$
 $E \Rightarrow a + F + T$
 $E \Rightarrow a + a + T$
 $E \Rightarrow a + a + F$
 $E \Rightarrow a + a + a$

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Step 7 of 8

d)

The parse tree to generate string $((a))$ is as follows:



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Step 8 of 8

The derivation for the string $((a))$ is as follows:

$E \Rightarrow T$
 $E \Rightarrow F$
 $E \Rightarrow (E)$
 $E \Rightarrow (T)$
 $E \Rightarrow (F)$
 $E \Rightarrow ((E))$
 $E \Rightarrow ((T))$
 $E \Rightarrow ((F))$
 $E \Rightarrow ((a))$

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