

## Problem

Give an informal description of a pushdown automaton that recognizes the language  $A$  in Exercise 2.9.

## Step-by-step solution

### Step 1 of 1

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Given language is

$$A = \{a^i b^j c^k \mid i = j \text{ or } j = k \text{ where } i, j, k \geq 0\}$$

The language is union of two languages  $\{a^i b^j c^k \mid i, k \geq 0\}$  and  $\{a^i b^k c^k \mid i, k \geq 0\}$ .

$$\text{Let } A_1 = \{a^i b^j c^k \mid i, k \geq 0\} \text{ and } A_2 = \{a^i b^k c^k \mid i, k \geq 0\}.$$

The informal description of the PDA that recognizes the language  $A_1$ .

In more detail, it operates as follows:

- Read and push  $a$ 's.
- Read  $b$ 's, while popping  $a$ 's.
- If  $b$ 's finish when stack is empty, skip  $c$ 's on input and accept.

The informal description of the PDA that recognizes the language  $A_2$ .

In more detail, it operates as follows:

- Skip  $a$ 's on input.
- Read and push  $b$ 's.
- Read  $c$ 's, while popping  $b$ 's.
- If  $c$ 's finish when stack is empty, accept.

The informal description of the PDA that recognizes the language  $A$  is the combination of both the languages  $A_1$  and  $A_2$ .

In more detail, it operates as follows:

1. Nondeterministically branch to either step 2 or step 6.
2. Read and push  $a$ 's.
3. Read  $b$ 's, while popping  $a$ 's.
4. If  $b$ 's finish when stack is empty, skip  $c$ 's on input and accept.
5. Skip  $a$ 's on input.
6. Read and push  $b$ 's.
7. Read  $c$ 's, while popping  $b$ 's.
8. If  $c$ 's finish when stack is empty, accept.

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