

### Problem

Read the informal definition of the finite state transducer given in Exercise 1.24. Give a formal definition of this model, following the pattern in Definition 1.5 (page 35). Assume that an FST has an input alphabet  $\Sigma$  and an output alphabet  $\Gamma$  but not a set of accept states. Include a formal definition of the computation of an FST.

(Hint: An FST is a 5-tuple. Its transition function is of the form  $\delta: Q \times \Sigma \longrightarrow Q \times \Gamma$ .)

### Step-by-step solution

#### Step 1 of 2

##### Finite State Transducer:

- A finite state transducer is a kind of deterministic finite state automaton which consists of both the input string and the output string.
- It converts the input string into an output string.

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#### Step 2 of 2

##### The formal definition of Finite State Transducer (FST) is as follows:

A Finite State Transducer is a 6-tuple machine and is represented as  $M = (Q, \Sigma, \Gamma, \delta, q_0)$  where

- $Q$  is a finite set of states.
- $\Sigma$  is a finite set of input alphabets.
- $\Gamma$  is a finite set of output alphabets.
- $\delta: Q \times \Sigma \rightarrow Q \times \Gamma$  is the transition function that defines rules.
- $q_0 \in Q$ , is the start state.

##### The formal definition of the computation of Finite State Transducer (FST) is as follows:

- The computation of the finite state machine is carried out by translating the input string into output string.
- Assume that  $w$  is an input string over the input alphabet  $\Sigma$  and  $x$  is an output string consisting of alphabet of  $\Gamma$ .
- The transition is carried out over a sequence of states  $q_0', q_1', \dots, q_n'$  in  $Q'$  such that
  - $q_0' = q_0$
- The transition of  $\delta(q_{i+1}', w_{i+1}) = (q_{i+1}', x_{i+1})$  for  $0 \leq i < n$ .

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