UDAAN 2025

TRIGONOMETRY (Level - 01)

Practice Sheet

Prove the following trigonometric identities:

$$(1-\cos^2 A)\csc^2 A = 1$$

$$2 \tan^2 \theta \cos^2 \theta = 1 - \cos^2 \theta$$

$$\cos \theta \sqrt{1 - \cos^2 \theta} = 1$$

$$(\sec^2 \theta - 1)(\csc^2 \theta - 1) = 1$$

$$\tan \theta + \frac{1}{\tan \theta} = \sec \theta \csc \theta$$

$$\frac{\cos \theta}{1 - \sin \theta} = \frac{1 + \sin \theta}{\cos \theta}$$

$$\sqrt{1}$$
. $\sin^2 A + \frac{1}{1 + \tan^2 A} = 1$

$$\sqrt{\frac{1-\cos\theta}{1+\cos\theta}} = \csc\theta - \cot\theta$$

$$\frac{1-\cos\theta}{\sin\theta} = \frac{\sin\theta}{1+\cos\theta}$$

$$\sqrt{10} \cdot \frac{1 - \sin \theta}{1 + \sin \theta} = \left(\sec \theta - \tan \theta\right)^2$$

11.
$$\frac{\left(1+\cot^2\theta\right)\tan\theta}{\sec^2\theta}=\cot\theta$$

12.
$$\tan^2 \theta - \sin^2 \theta = \tan^2 \theta \sin^2 \theta$$

13.
$$(\sec \theta + \cos \theta)(\sec \theta - \cos \theta) = \tan^2 \theta + \sin^2 \theta$$

$$\mathbf{14.} \quad \sec A (1 - \sin A) (\sec A + \tan A) = 1$$

15.
$$(\cos A - \sin A)(\sec A - \cos A)(\tan A + \cot A) = 1$$

16.
$$\sin^2 A \cot^2 A + \cos^2 A \tan^2 A = 1$$

17.
$$\cot \theta - \tan \theta = \frac{2\cos^2 \theta - 1}{\sin \theta \cos \theta}$$

18.
$$\frac{\cos^2 \theta}{\sin \theta} - \csc \theta + \sin \theta = 0$$

19.
$$\frac{1}{1+\sin A} + \frac{1}{1-\sin A} = 2\sec^2 A$$

20.
$$\frac{1+\sin\theta}{\cos\theta} + \frac{\cos\theta}{1+\sin\theta} = 2\sec\theta$$
 [NCERT]

21.
$$\frac{(1+\sin\theta)^2 + (1-\sin\theta)^2}{2\cos^2\theta} = \frac{1+\sin^2\theta}{1-\sin^2\theta}$$

22.
$$\frac{1+\tan^2\theta}{1+\cot^2\theta} = \left(\frac{1-\tan\theta}{1-\cot\theta}\right)^2 = \tan^2\theta$$
 [NCERT]

23.
$$\frac{1+\sec\theta}{\sec\theta} = \frac{\sin^2\theta}{1-\cos\theta}$$
 [NCERT]

$$\sqrt{24.} \qquad \frac{\left(1 + \tan^2 \theta\right) \cot \theta}{\csc^2 \theta} = \tan \theta$$

$$25. \quad \frac{1 + \cos A}{\sin^2 A} = \frac{1}{1 - \cos A}$$

26.
$$\frac{\sec A - \tan A}{\sec A + \tan A} = \frac{\cos^2 A}{\left(1 + \sin A\right)^2}$$

$$27. \qquad \frac{1+\cos A}{\sin A} = \frac{\sin A}{1-\cos A}$$

$$\sqrt{\frac{1+\sin A}{1-\sin A}} = \sec A + \tan A$$



$$\sqrt{\frac{1 - \cos A}{1 + \cos A}} + \sqrt{\frac{1 + \cos A}{1 - \cos A}} = 2 \csc A$$

30.
$$(\sec A - \tan A)^2 = \frac{1 - \sin A}{1 + \sin A}$$

31/.
$$\frac{1}{\sec A - 1} + \frac{1}{\sec A + 1} = 2 \csc A \cot A$$

32.
$$\frac{\tan A + \tan B}{\cot A + \cot B} = \tan A \tan B$$

33.
$$\tan^2 A \sec^2 B - \sec^2 A \tan^2 B = \tan^2 A - \tan^2 B$$



Answer Key

- 1. (Prove)
- **2.** (**Prove**)
- **3.** (**Prove**)
- **4.** (**Prove**)
- 5. (Prove)
- 6. (Prove)
- **7.** (**Prove**)
- **8.** (**Prove**)
- **9.** (**Prove**)
- **10.** (Prove)

- 11. (**Prove**)
- **12.** (**Prove**)
- **13.** (**Prove**)
- **14.** (**Prove**)
- **15.** (**Prove**)
- **16.** (**Prove**)
- **17.** (**Prove**)
- **18.** (**Prove**)
- **19.** (**Prove**)
- **20.** (**Prove**)
- **21.** (Prove)
- **22.** (Prove)
- **23.** (Prove)
- **24.** (Prove)
- **25.** (Prove)
- **26.** (Prove)
- **27.** (Prove)
- 28. (Prove)
- **29.** (Prove)
- **30.** (Prove)
- **31.** (Prove)
- **32.** (Prove)
- **33.** (Prove)

