

## Department of Aerospace Engineering IIST, Thiruvananthapuram Multi-disciplinary Optimisation (AE 496)

9:00-10:00AM 05/09/2017 (D4)

Maximum Marks: 15

## Note:

- 1. All questions are compulsory.
- 2. Clearly state all the assumptions/approximations in the derivations/answers.
- 1. Write a short note comparing the relative strengths and weaknesses of gradient and non-gradient optimisation algorithms.
- 2. State and prove the first order necessary optimality condition for unconstrained optimisation problem over a continuous domain.
- 3. Write a short note on various numerical step-size calculation methods by clearly outlining their relative advantages and disadvantages.
- 4. Write down the complete algorithm for Marquardt's method, either using a flowchart, or a pseudo-code. Please add extra text at the bottom of the algorithm to further clarify each step (if needed). Do not neglect to mention even simple (obvious) steps like "Calculate the gradient c".
- 5. Show that the BFGS formula given below is symmetric and satisfies the secant condition,

$$B^{(k+1)} = B^{(k)} + \frac{y^{(k)}y^{(k)^T}}{y^{(k)^T}s^{(k)}} + \frac{c^{(k)}c^{(k)^T}}{c^{(k)^T}d^{(k)}}$$

where, c is the gradient vector, d is the descent direction,  $y^{(k)} = c^{(k+1)} - c^{(k)}$ ,  $s^{(k)} = x^{(k+1)} - x^{(k)}$  and B is an approximation of the Hessian matrix H.

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Student's name: End of exam