

Math MTRV - 2

1. Let first term =  $a$  and common difference = ' $d$ '

$$a_1 = \frac{1}{2} \Rightarrow a = \frac{1}{2} \quad \text{--- (i)}$$

$$a_8 = \frac{17}{6} \Rightarrow a + 7d = \frac{17}{6} \quad \text{--- (ii)}$$

$$\text{(ii)} - \text{(i)}$$

$$a + 7d - a = \frac{17}{6} - \frac{1}{2}$$

$$\Rightarrow 7d = \frac{28}{12} \Rightarrow d = \frac{1}{3}$$

$$\therefore \text{common difference} = \frac{1}{3}$$

$$\begin{aligned} \text{Fourth term} \Rightarrow a_4 &= a + 3d \\ &= \frac{1}{2} + 3 \times \frac{1}{3} \\ &= \frac{1}{2} + 1 \\ &= \frac{3}{2} \end{aligned}$$

$$\therefore \text{common difference} = \frac{1}{3} \text{ and } a_4 = \frac{3}{2}$$

2. a

$$a = 11$$

$$\text{common difference} = -3$$

$$\therefore \text{let } n^{\text{th}} \text{ term} = -150$$

$$\therefore a + (n-1)d = -150$$

$$11 + (n-1)(-3) = -150$$

$$11 - 3n + 3 = -150$$

$$\therefore -3n + 14 = -150$$

$$\therefore -3n = -164$$

$$\therefore 3n = 164$$

$\therefore$  as  $n$  is a fraction here,  $-150$  is not a term of this AP

3.

$$S_7 = 119$$

$$\left[ S_n = \frac{n}{2} (2a + (n-1)d) \right]$$

$$\frac{7}{2} (2a + 6d) = 119 \Rightarrow a + 3d = 17 - \textcircled{1}$$

$$\text{We know, } S_{17} = 714$$

$$\therefore \frac{17}{2} (2a + 16d) = 714$$

$$a + 8d = 402 - \textcircled{2}$$

Subtracting  $\textcircled{1}$  from  $\textcircled{2}$

$$42 - 17 = a + 3d - a - 8d$$

$$\Rightarrow 25 = -5d$$

$$\Rightarrow d = -5$$

putting  $d = -5$  in  $\textcircled{1}$

$$17 = a + 3(-5)$$



$$\Rightarrow 17 = a - 15$$

$$\Rightarrow 15 + 15 = a$$

$$\Rightarrow a = 32 ; d = -5$$

$$S_n = \frac{n}{2} (2 \cdot 32 + (n-1)(-5))$$

$$\Rightarrow S_n = \frac{n}{2} (64 - 5n + 5)$$

$$\therefore S_n = \frac{69n}{2} - \frac{5n^2}{2}$$

$$\therefore S_n = \frac{69n - 5n^2}{2} \text{ and } a = 32 ; d = -5$$