

* Sum of squares of n numbers should be also a square :-

$$n^2 = (n-2)^2 - 4 + 4n$$

$$n^2 = (n-2)^2 + 2^2(n-1)$$

$$(n)^2 = (n-2)^2 + [2]^2(n-1)$$

it means for any number n its square will be equal to $(n-1)$ times $2^2 + 1 \times (n-2)^2$

total are n number and their sum is a square

* if any number n is even then obviously $n-1$ is odd and it can be written as

$$n-1 = 2u+1 \Rightarrow n = \frac{n-2}{2}$$

add u^2 to both sides

$$n^2 + n-1 = n^2 + 2u+1$$

$$n^2 + n-1 = (u+1)^2$$

$$n^2 + 1^2(n-1) = (u+1)^2$$

if n is odd

$n-2$ also a odd number

and $n-2+4 \Rightarrow$ odd number

$$n-2+4 \neq 2u+1$$

$$\Rightarrow u = \frac{n+1}{2}$$

$$n-2+4 + u^2 = n^2 + 2u+1$$

$$n^2 + (n-2)+4 = (u+1)^2$$

$$n^2 + 1^2(n-2) + 2^2 = (u+1)^2$$