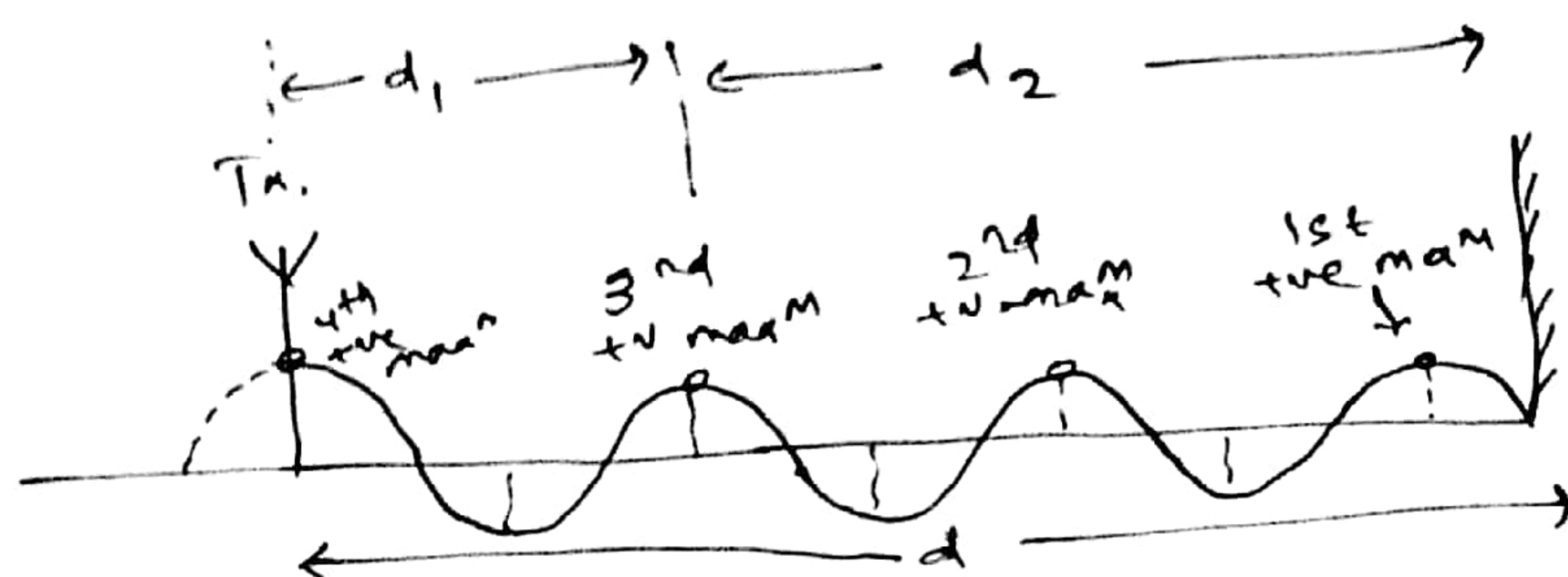


1. From the eqn of Electric field

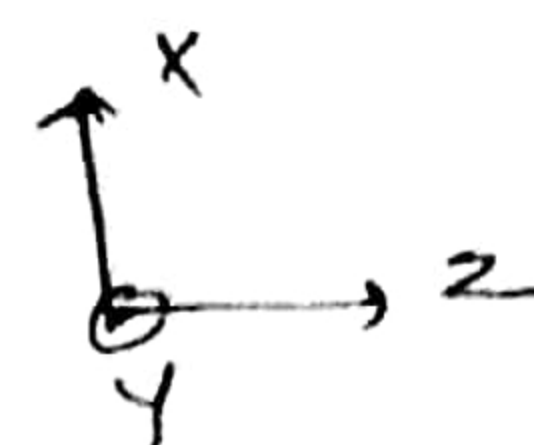
$$E(z,t) = \hat{y} 2E_0 \sin(\beta z) \cdot \sin(\omega t) \quad \text{V/m.} \quad (1)$$

(Please follow the tutorial-3 material for the derivation of above eqn.)

According to the eqn ^{and equation given.} the standing wave pattern



perfectly
conductive
wall (PCW).



(a) $E(z) = \hat{y} 2E_0 \sin(\beta z)$

$E(z) \rightarrow \text{max. for}$

$$\beta z = n\pi + \pi/2$$

$$\beta = \omega \sqrt{\mu_0 \epsilon_0} = 2\pi/\lambda_0$$

$$z = \frac{(n\pi + \pi/2) \lambda_0}{2\pi}$$

for, $n=6$, the 4th (+ve) max will at the posⁿ ob antenna.

$$z = \frac{(6\pi + \pi/2) \lambda_0}{2\pi} = \frac{13 \times 12}{4} = 3.25 (12) = 39 \text{ m.}$$

(b) $\beta z = n\pi$

$$z = \frac{n\pi}{2\pi} \lambda_0 = \frac{12n}{2} = 6n \quad \forall \quad n = 1, 2, \dots, 6$$

where the E-field is zero. [Hence, placing

a conducting surface will not affect the wave propagation.

(2)

(c) from equn.
for propagation in a low-loss medium.
i.e. $\frac{\sigma}{\omega\epsilon} \ll 1$

$$\epsilon_1 = 4\epsilon_0, \epsilon_r = 4$$

$$\mu_1 = \mu_0, \mu_r = 1.$$

$$\sigma = 10^{-5} \text{ S/m}.$$

$$\alpha = \frac{\sigma}{2} \sqrt{\frac{\mu}{\epsilon}} = 30\pi \times 10^{-5} \text{ Np/m}.$$

The first ^{the} maxm. of the E-field to the right
of the antenna.

$$E = E_0 e^{-\alpha d_1} + E_0 e^{-\alpha(d+d_2)}$$

$$= 100 \left[e^{-\alpha d_1} + e^{-\alpha(d+d_2)} \right]$$

$$d_1 = \lambda = 12 \text{ m}.$$

$$d = 3.25\lambda = 39 \text{ m}.$$

$$d_2 = 2.25\lambda = 27 \text{ m}.$$

$$\Rightarrow E = 100 \left[e^{-30\pi \times 10^{-5} \times 12} + e^{-30\pi \times 10^{-5} (39+27)} \right]$$

$$= 192.84 \text{ V/m}.$$

$$2. P_r = 10 \text{ mW/m}^2.$$

$$f = 10 \text{ GHz}.$$

$$\text{body property } \sigma = 0.01 \text{ S/m}.$$

$$\mu = \mu_0.$$

$$\epsilon = 24\epsilon_0.$$

$$\text{body impedance } \eta_b = \sqrt{\frac{j\omega\mu}{\sigma + j\omega\epsilon}}.$$

$$\frac{\sigma}{\omega\epsilon} \ll 1, \quad \eta_b = \sqrt{\mu/\epsilon}.$$

Reflection from body.

$$\Gamma_b = \frac{\eta_b - \eta_0}{\eta_b + \eta_0} = \frac{1 - \sqrt{24}}{1 + \sqrt{24}} = -0.66$$

Total power absorbed by the body.

$$= P_r (1 - |\Gamma|^2) \cdot \text{effective area}$$

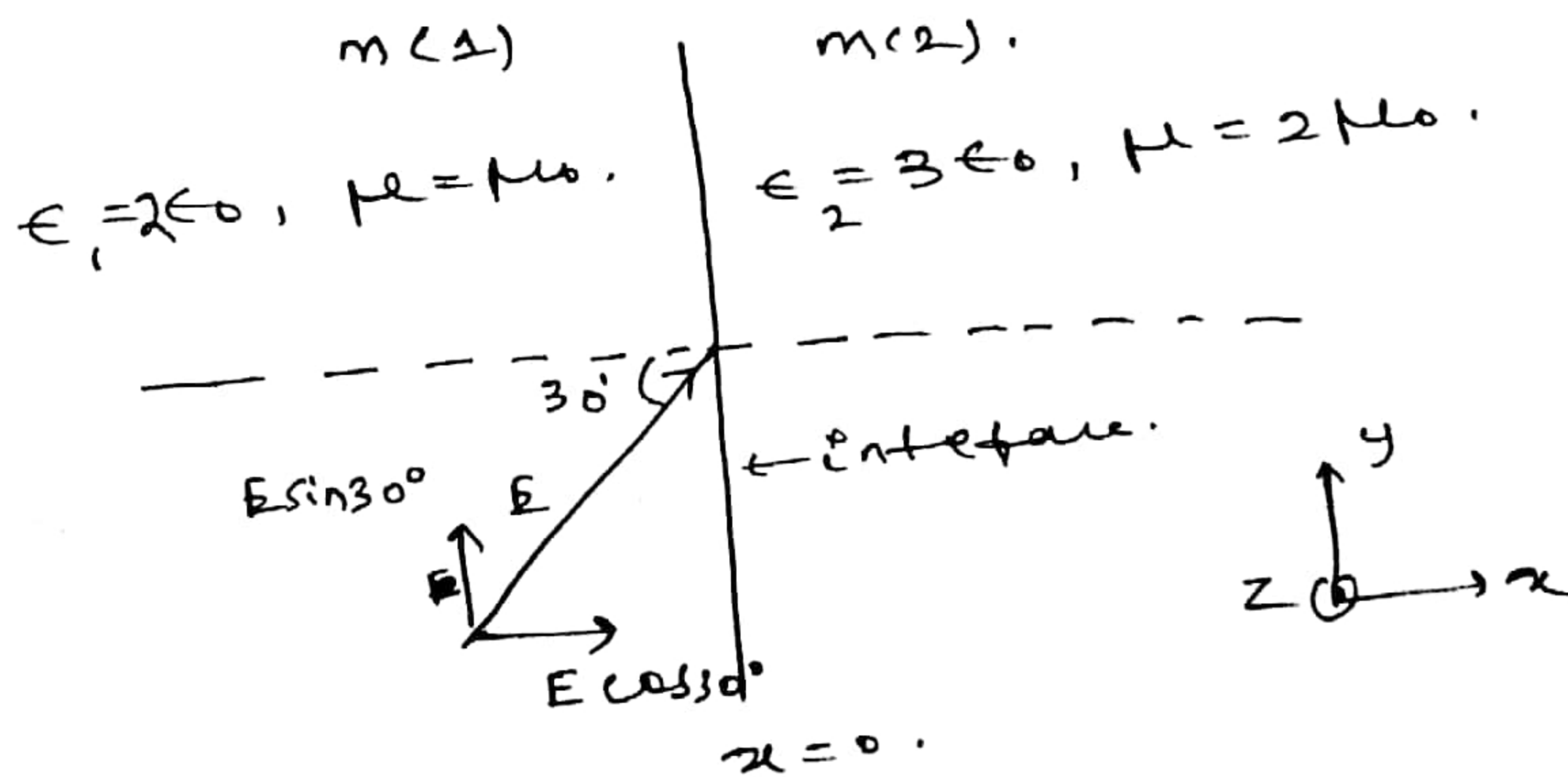
$$= 10 \frac{\text{mW}}{\text{cm}^2} (1 - 0.66^2) \cdot 1.5 \times 100^2 \text{ cm}^2$$

$$= 84.66 \text{ W}$$

Energy absorbed during maximum exposure.

$$= 84.66 \times 6 \text{ hr.} = 507.96 \text{ W.h.}$$

4.



(a) $E_{n1} = E \cos 30^\circ$

$E_{t1} = E \sin 30^\circ = E_{t2}$

$$D_{n1} = D_{n2}$$

$$\Rightarrow \epsilon_1 E_{n1} = \epsilon_2 E_{n2}$$

$$\Rightarrow E_{n2} = \frac{\epsilon_1}{\epsilon_2} E_{n1} = \frac{2}{3} E \cos 30^\circ$$

$$\vec{E}_2 = \vec{E}_{t1} + \vec{E}_{n1} = E \sin 30^\circ \hat{y} + \frac{2}{3} E \cos 30^\circ \hat{x}$$

$$= \frac{5}{2} \hat{y} + \frac{10}{3} \hat{x} \cdot \frac{5\sqrt{3}}{2}$$

$$|\vec{E}_2| = \sqrt{\left(\frac{5}{2}\right)^2 + \left(\frac{5\sqrt{3}}{2}\right)^2} = 5 \text{ V/m}$$

$$|\vec{D}_1| = 2|\vec{E}| = 10 \text{ C/m}^2.$$

$$\vec{E}_2 = \vec{E}_{t2} + \vec{E}_{r2}.$$

$$= E \sin 30^\circ \hat{y} + \frac{2}{3} E \cos 30^\circ \hat{x}.$$

$$= \frac{5}{2} \hat{y} + \frac{2}{3} \times 5 \cdot \frac{\sqrt{3}}{2} \hat{x}$$

$$|\vec{E}_2| = 3.81 \text{ V/m}.$$

$$|\vec{D}_2| = 3 \times (3.81) = 11.45 \text{ C/m}^2.$$

(b) The wave is LP on each side of interface.

5. $\omega = 6 \times 10^8 \text{ rad/s}.$

$$L = 0.35 \mu\text{H/m}$$

$$C = 40 \text{ pF/m}.$$

$$G = 75 \mu\text{S/m}.$$

$$R = 17 \Omega/\text{m}.$$

$$Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}} = \left(\frac{17 + j 6 \times 10^8 \times 0.35 \times 10^{-6}}{75 \times 10^{-6} + j \times 6 \times 10^8 \times 40 \times 10^{-12}} \right)^{1/2}$$

$$= 93.623 - j 3.63 \text{ or } 93.694 \angle -2.224^\circ \Omega.$$

$$\Gamma = \left[(R + j\omega L)(G + j\omega C) \right]^{1/2}$$

$$= 0.094 + j 2.246 \text{ or } 2.248 \angle 87.596^\circ.$$

$$v_p = \frac{\omega}{\beta} = \frac{6 \times 10^8}{2.246} = 2.671 \text{ m/s}.$$

$$\lambda = \frac{2\pi}{\beta} = 2.797 \text{ m}.$$

to

(+)

$$10 \log(A) = -20$$

$$\Rightarrow A = 10^{-2}$$

$$e^{-2\alpha d} = 10^{-2}$$

$$\Rightarrow 2\alpha d = 4.605$$

$$\Rightarrow d = \frac{4.605}{2 \times 0.094} \approx 24.5 \text{ m.}$$

3.

$$J_0 = 1 \text{ A/m.}$$

$$f = 100 \text{ MHz}$$

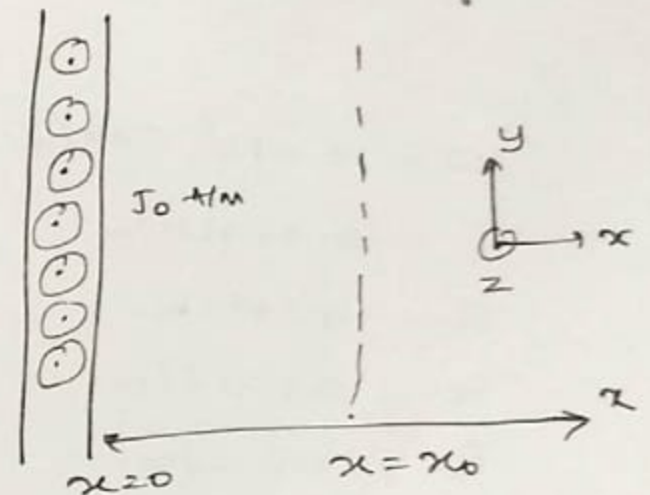
$$\sigma = 4 \text{ S/m.}$$

$$\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m.}$$

$$\epsilon_r = 80$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ H/m.}$$

$$x_0 = 1 \text{ m.}$$



$$\gamma = \sqrt{j\omega\mu(\sigma + j\omega\epsilon)}$$

$$= \left\{ j \times 2\pi \times 10^8 \times 4\pi \times 10^{-7} \left[4 + (j \times 2\pi \times 10^8 \times 80 \times 8.854 \times 10^{-12}) \right] \right\}^{1/2}$$

$$= 37.592 + j 42.006$$

$$\alpha = 37.592 \text{ NP/m.}$$

$$\beta = 42.006 \text{ rad/m.}$$

$$\vec{J} = \hat{z} 1 \text{ A/m.}$$

$$\vec{H} = \hat{y} \frac{J_s}{2} e^{-\gamma x}$$

$$= \hat{y} \frac{1}{2} e^{-\alpha x} e^{-j\beta x}$$

$$\vec{H}|_{x=1 \text{ m}} = \hat{y} 0.5 \times e^{-37.592} e^{-j42.006}$$

$$= \hat{y} 2.36 \times 10^{-17} e^{-j42.006} \text{ A/m.}$$

From Ampere's law

$$\oint \vec{H} \cdot d\vec{l} = I_{enc} = J_0 b$$

$$H = \begin{cases} H_0 \hat{a}_y & x > 0 \\ -H_0 \hat{a}_y & x < 0 \end{cases}$$

$$\oint \vec{H} \cdot d\vec{l} = \left(\int_1^2 + \int_2^3 + \int_3^4 + \int_4^1 \right) H \cdot dl$$

$$= 0(-a) + (-H_0)(-b) + 0(a) + H_0(b)$$

$$= 2H_0 b$$

from ① & ② $H_0 = \frac{1}{2} J_0$

$$H = \begin{cases} \frac{J_0}{2} \hat{a}_y & x > 0 \\ -\frac{J_0}{2} \hat{a}_y & x < 0 \end{cases}$$

$$\vec{E} = -\hat{z} \eta |H| e^{-\gamma x}$$

$$\eta = \sqrt{\frac{j\omega\mu}{\sigma + j\omega\epsilon}}$$

$$= \left[\frac{j 2\pi \times 10^8 \times 4\pi \times 10^{-7}}{4 + j 2\pi \times 10^8 \times 80 \times 8.854 \times 10^{-12}} \right]^{1/2}$$

$$= \Omega \cdot 10.437 + j9.34 \quad \text{or} \quad 14.006 \angle 41.825^\circ \Omega$$

$$\vec{E} = -\hat{z} \quad 3.3 \angle 41.82^\circ \times 10^{-16} e^{j42} \text{ V/m}$$

$$\text{or } (24.631 + j22.042) \times 10^{-17} e^{j42} \text{ V/m}$$