EE-IITB EE301-TUTORIAL 3

1. Region 1, z < 0, and region 2, z > 0, are both perfect dielectrics ($\mu = \mu_0$, ε and loss less). A uniform plane wave traveling in the \mathbf{a}_z direction has a radian frequency of 3×10^{10} rad/s. Its wavelengths in the two regions are $\lambda_1 = 5$ cm and $\lambda_2 = 3$ cm. What percentage of the energy incident on the boundary is (a) reflected; (b) transmitted? (c) What is the standing wave ratio in region 1?

2. A plane wave propagates in free space and encounters a perfect conductor. The frequency of the wave is 1 GHz and its amplitude is 1 V/m. The electric field intensity is directed in the x direction and the wave propagates in the z direction, as shown in Figure 1.

Calculate the electric and magnetic field intensities everywhere to the

left of the conductor's surface.

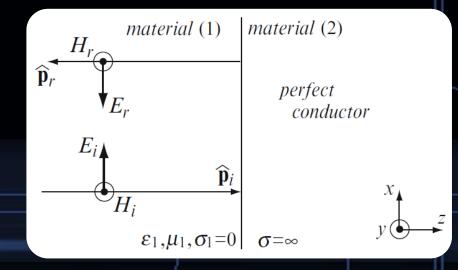


Figure 1.

3. A plane wave with parallel polarization is incident on the interface between a perfect dielectric and free space, at 28° from within the dielectric. The dielectric has permeability of free space and relative permittivity $\epsilon_r = 4$.

Calculate:

- (a) The reflection and transmission coefficients at the interface.
- (b) The critical angle.
- (c) The Brewster's angle if $\varepsilon_{r1} = \varepsilon_{r2}$

4. A uniform plane wave travelling (With $|E| = 10^{-3}$ V/m) in free space is incident on a semi-infinite lossless medium with a dielectric constant of 1.44. Determine the values of the reflection coefficient, transmission coefficient, incident and transmitted power, and travelling wave and standing wave parts in the incident medium.

5. A uniform plane wave with perpendicular polarization travelling in free space having a power density of 10 W/m² is incident at an air-dielectric (ε_r = 25) interface with an incident angle of 45°. Find the amplitude of the electric field, the magnetic field at a distance of 1 m on either side of the interface. Consider the frequency of wave as 100 MHz.

- 6. Consider a parallel polarized electromagnetic wave radiated from a submerged submarine impinges on a water-air interface. Assuming the zero conductivity for water and $\epsilon_r = 81$. Calculate the value of the incidence angle for which reflected power is zero
- (a) Repeat the above problem considering the wave radiated from an aircraft impinges on an air-water interface. Also, assume that the conductivity of air is zero.

7. A perpendicularly polarized plane wave at 100 GHz impinges on a flat metallic reflector at an angle of incidence α . The incident electric field intensity is in the positive x direction, has amplitude 100 V/m, and propagates in free space. Assume the incident magnetic field intensity has components in the positive y and negative z directions and that the interface coincides with the x-y plane.

Calculate: The surface current density as a function of the incidence angle α on the surface of the conductor. Plot its magnitude and show for what values of the incidence angle the current density is maximum and for what values it is minimum.