

# 1. Interpretation of Divergence.

EX:  $\nabla \cdot D = \rho_v$

Consider  $D = k(xa_x + ya_y)$ .

Calculate the value of charge ~~that originates~~ from which the field originates for

a)  $k = 1$

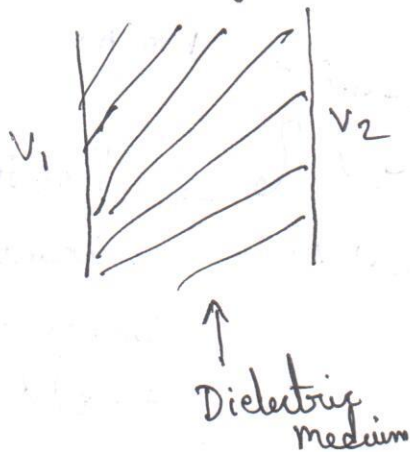
$$\nabla \cdot D = 2$$

b)  $k = 2$

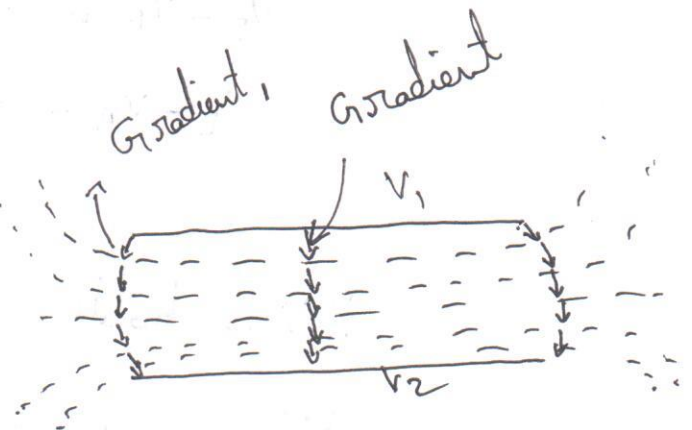
$$\nabla \cdot D = 4.$$

# 2. Interpretation of ~~divergen~~ gradient and significance of -ve sign.

EX: Calculate the value of E-field inside the region bounded by  $V_1, V_2$



$$\Rightarrow E = -\nabla V$$



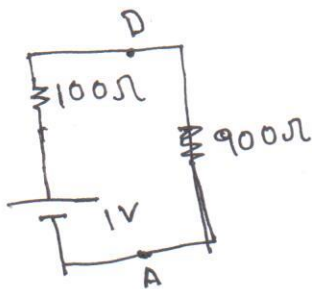
3. Calculate the value of  $\nabla \times \mathbf{H}$  at the two points given in the figure

at 'a'  $\nabla \times \mathbf{H} = \mathbf{J}$

at 'b'  $\nabla \times \mathbf{H} = 0$



4.

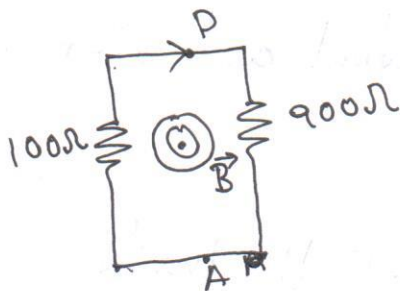


find  $V_D - V_A$

$$E = IR \Rightarrow I = \frac{1}{1000} = 1 \text{ mA}$$

$$V_D - V_A = 0.9 \text{ V}$$

$\nabla \times \mathbf{E} = 0$   
Conservative field.



find  $V_D - V_A$

$\vec{B}$  is increasing magnetic field

Consider  $E_{\text{induced}} = 1 \text{ V}$ .

$$\text{Current} = \frac{1}{100 + 900} = 1 \text{ mA}$$

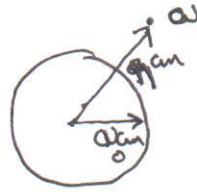
$$\left. \begin{aligned} V_D - V_A &= 0.9 \text{ V} \\ V_D - V_A &= -0.1 \text{ V} \end{aligned} \right\} \rightarrow \text{Difference is because of non conservative field.}$$

KVL holds for conservative fields.

KVL is a special case of Faraday's law.

5. Consider a flux tube that carries Magnetic field intensity of  $H = \sin(\omega t)$ . Find the value of  $E$  at point 'a' ~~as~~ shown in figure

$$\nabla \times E = -\frac{d}{dt} \mu_0 \sin(\omega t)$$



$$\nabla \times E = -\mu_0 \omega \cos(\omega t)$$

apply Stokes theorem

~~$$\oint (\nabla \times E) \cdot d\mathbf{s}$$~~

$$\iint (\nabla \times E) \cdot d\mathbf{s} = - \iint \mu_0 \omega \cos(\omega t) d\mathbf{s}$$

$$\oint E \cdot d\mathbf{l} = -\mu_0 (\pi a_0^2) \cos \omega t$$

$$E (2\pi a) = -\mu_0 (\pi a_0^2) \cos \omega t$$

$$E = \frac{-\mu_0 \pi a_0^2 \cos(\omega t)}{2\pi a}$$

$$E = \frac{-\mu_0 \cos(\omega t) a_0^2}{2a}$$