Problem 5.5

Specify the Nyquist rate and the Nyquist interval for each of the following signals:

(a)
$$g(t) = \operatorname{sinc}(200t)$$

(b)
$$g(t) = \text{sinc}^2(200t)$$

(c)
$$g(t) = \operatorname{sinc}(200t) + \operatorname{sinc}^2(200t)$$

Solution

(a) The highest frequency component of

$$g(t) = \operatorname{sinc}(200t)$$
$$= \frac{\sin(200\pi t)}{200\pi t}$$

is 100 Hz. Hence, the Nyquist rate is 200 Hz and the Nyquist interval is 5 ms.

(b) The highest frequency component of

$$g(t) = \operatorname{sinc}^2(200t)$$

is twice that of g(t) in part (a); it is so because squaring a band-limited single has the effect of doubling its highest frequency component. Hence, the Nyquist rate of

$$g(t) = \operatorname{sinc}^2(2Wt)$$

is 400 Hz and the Nyquist interval is 2.5 ms.

(c) The highest frequency component of the composite signal

$$g(t) = \operatorname{sinc}(200t) + \operatorname{sinc}^{2}(200t)$$

is determined by the component $sinc^2(200t)$. Hence, the Nyquist rate of this third signal is 400 Hz and the Nyquist interval is 2.5 ms.