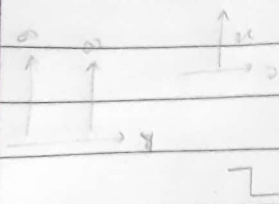


$$\lambda(\mu\text{m}) = \frac{1.24}{E_g(\text{eV})}$$

Quantum Wire



5nm ← for energy discretization

2D confinement → Q. wire

Quantum Dots - 3D confinement

0-D system

from thermodynamics ΔF GaN

minimizing surface energy

ΔE_c = Conduction band offset ΔE_v = valence band offset

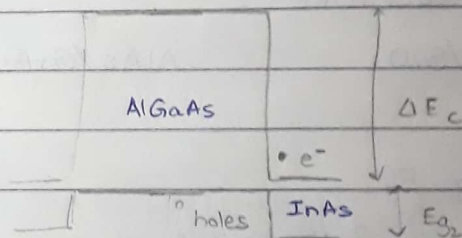
$$\Delta E_g = E_{g1} - E_{g2} = \Delta E_c + \Delta E_v$$



Type I

$$\Delta E_c = 0.6 \Delta E_g$$

$$\Delta E_v = 0.4 \Delta E_g$$

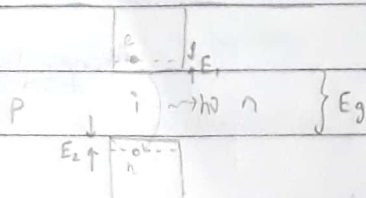


Type II (staggered)

• e^- and holes are physically separated
• give very good high performance photodiodes

LED

pn



flatband diagram

AlGaIn - GaN - AlGaIn

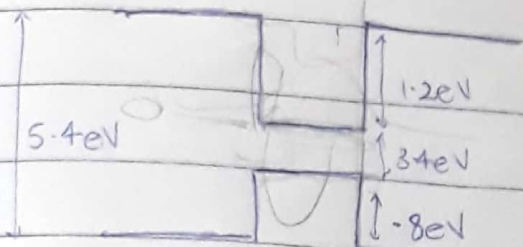
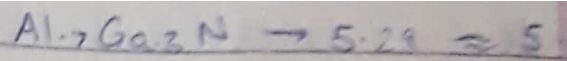
$E_1 \neq E_2$ (due to m^*)

GaN - InGaIn - GaN

$$E_g' = E_g + E_1 + E_2 = hc/\lambda$$

$$\lambda = 300 \text{ nm}, \text{ Al}_{1-x}\text{Ga}_x\text{N} - \text{GaN} - \text{Al}_{1-x}\text{Ga}_x\text{N} \quad W = ?, x = ?$$

$$m_e = m_p = m_0$$



$$E_1 = \frac{n^2 h^2}{8 m_l^2} \quad \text{Ad-hoc} \quad E_1 = \frac{h^2}{10 m_l^2}$$

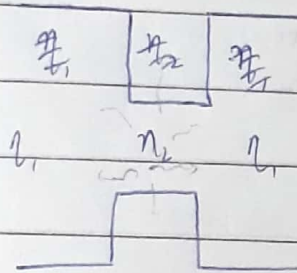
$$E_2 = \frac{h^2}{10 m_l^2}$$

$$3.4 + E_1 + E_2 = \frac{1.25}{.3} \approx 4.1 \Rightarrow$$

choosing x : lattice constant \rightarrow we have to grow the material (minimize defects)

$x a_1 + (1-x) a_2$: large $x \rightarrow$ low defects but no quantum
low $x \rightarrow$ trade-off

- carriers can't leave well \rightarrow greater recombination rate \Rightarrow more



AlGaIn
GaIn
AlGaIn

most light travels in p

* photon 'trapping' is due to refractive indices NOT potential well (electric)

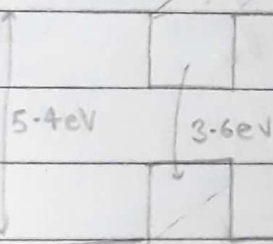
DIELECTRIC WAVEGUIDE

\hookrightarrow for monolithic circuits

to 1st order p
are not a
electric p

* Quantum efficiency : $\frac{\# \text{ of photons generated}}{\# \text{ of EHP injected}} = \eta_i \times \eta_e$

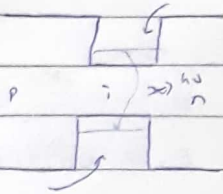
(less recombination)



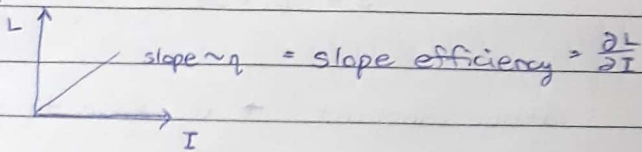
$$\eta_i = \frac{\# \text{ of photons generated}}{\# \text{ of EHP}}$$

$$\eta_e = \frac{\# \text{ of photons emitted}}{\# \text{ of photons generated}}$$

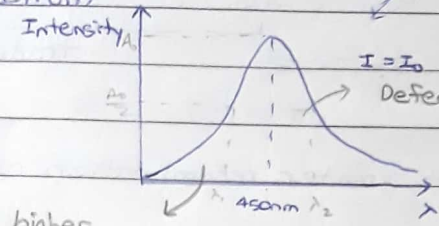
LED : $\rightarrow I$



① L-I



② Spectrum



ELECTROLUMINESCENCE

Full width $\lambda_2 - \lambda_1$ half maxima

\rightarrow Broadband emission

\rightarrow Narrowband emission

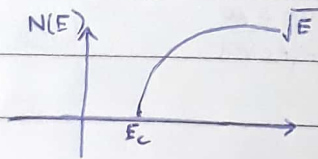
Power spectral Density

③ PHOTOLUMINESCENCE

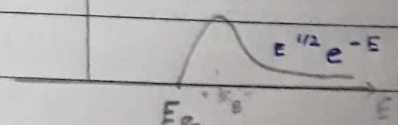
'Optical generation of carriers

Density of States

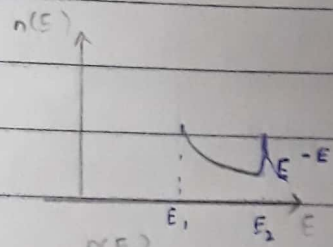
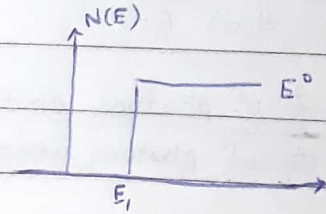
Bulk



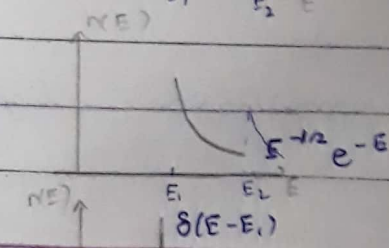
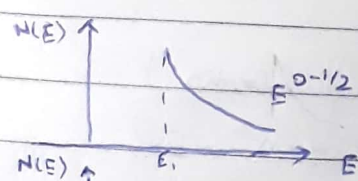
$$n(E) = f(E) N(E)$$



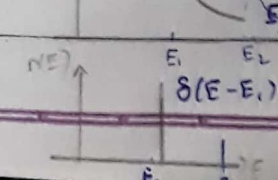
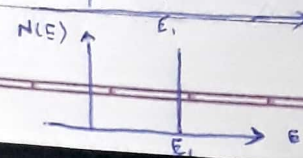
Q. Well



Q. Wire



Q. Dot



- p-i-n diode has greater breakdown voltage than p-n
- For LED and LASER p-i-n ensures radiative recomb. (defect free :)

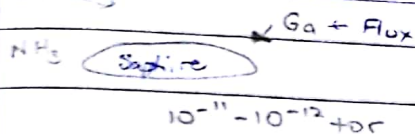
Page No.: 29

Date: 29/9/17

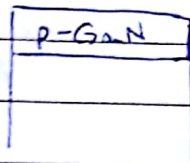
- Fermi-Dirac Statistics is from maximizing entropy
- Quantum Dot enables extremely narrow band emissions
- = For Quantum Well : \geq atleast one bound state
- Wire/Dot : not necessary.

LED FABRICATION

- Molecular Beam Epitaxy



- MOCVD : metal organic chemical vapour deposition



ICP - RIE

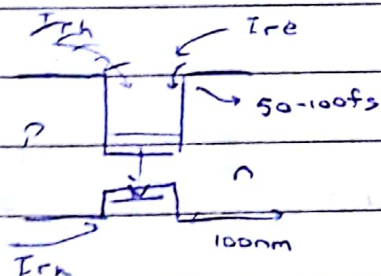
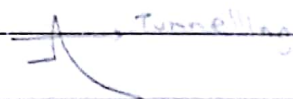
Inductive coupled plasma Reactive etching

(Ar/Cl)

n-dohmic

Ti/Al/Ni/Au

\rightarrow TiN



$$f = \frac{I_{rh} + I_{re}}{I_{rh} + I_{re} + I_r}$$

$$I_{re} = \frac{100 \text{ nm}}{v_e} \sim 1 \text{ ns}$$

$$I_{rh} \sim 1 \text{ ns}$$

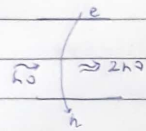
$$\tau_r \sim 5-10 \text{ ns}$$

- Mobility : Hall effect

Femtosecond Spectroscopy (can resolve any event $10-50 \text{ fs}$)

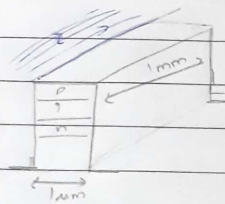
Time Resolved Photoluminescence

LASER



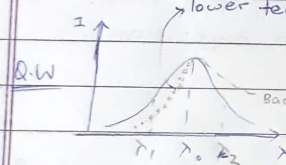
- phase coherence
- spectral purity (monochromatic light)
- spatial coherence

1.3 μm
1.55 μm Lasers
refractive index of quartz
s.t. transmission is high



Optical oscillator

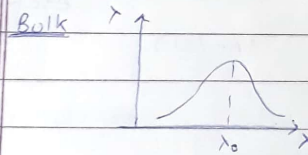
RECAP of LED



$$\lambda_0 = \frac{hc}{E_1 + E_2 + E_g}$$

$$E_1 + KE_1 + E_2 - KE_2 + E_g$$

mp mp



$$\lambda_0 = \frac{hc}{E_g + k_B T}$$

2 degree of confinement

$$E_x = \frac{\pi^2 \hbar^2 n_x^2}{2mL_x^2}$$

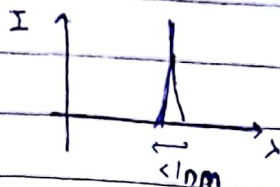
$$E_y = \frac{\pi^2 \hbar^2 n_y^2}{2mL_y^2}$$

$$E_z = \frac{\pi^2 \hbar^2 n_z^2}{2m}$$

Fermi's Golden Rule

↳ the emitted ~~was~~ photon ~~is~~ will have max. probability of having same phase as the

LASER



LED $\sim ns$

$\sim ps$ LASER

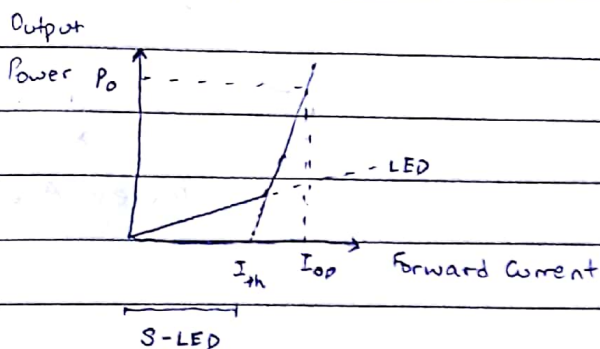
- higher power
- less time
also constructive interference
- more efficient
- Modulation bandwidth

LED speed is limited by recombination process

(LED $\rightarrow ns \Rightarrow GHz$ LASER $\rightarrow ps \Rightarrow THz$)

LASER \Rightarrow Gaussian

LED \rightarrow Lambert's Cosine Law



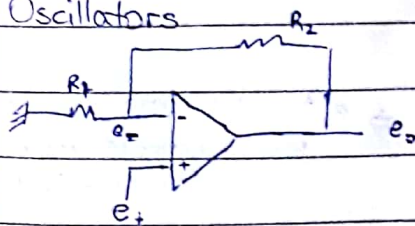
S-LED : superluminescent LED

\hookrightarrow same stimulated emission

but not enough for lasing action

Normalised Response : $\frac{\partial(L/L_o)}{\partial(I_{ac}/I_o)}$

Oscillators



$$e_o = A(e_+ - e_-)$$

$$\frac{0 - e_-}{R_1} = \frac{e_- - e_o}{R_2}$$

$$\Rightarrow \frac{e_o}{e_+} = \frac{A}{\frac{R_1}{R_1 + R_2} + 1} = \frac{A}{1 + AB}$$

$$\left(\frac{R_1}{R_1 + R_2} \right)$$

feedback factor

$$\frac{-ve}{1 + AB}$$

$$\frac{+ve}{1 - AB}$$

\hookrightarrow voltage could go to max \Rightarrow Saturation

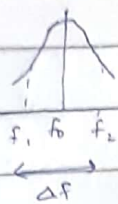
$|AB| > 1$ as circuit

will 'adjust' to

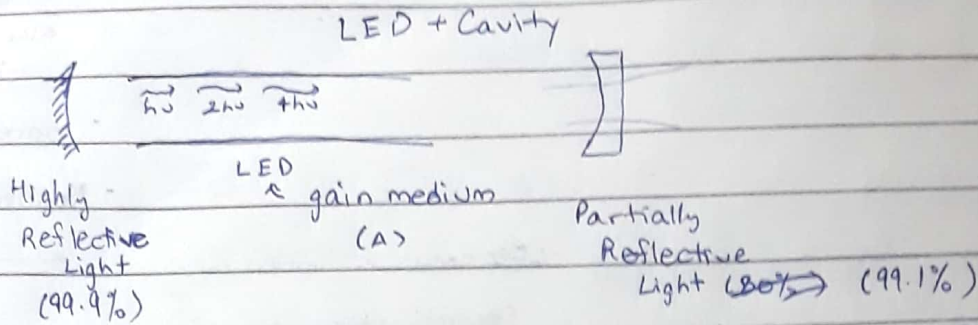
make $AB = 1$

$$\frac{A(\omega)}{1 - A(\omega)\beta(\omega)}$$

\hookrightarrow Amplifier becomes an oscillator

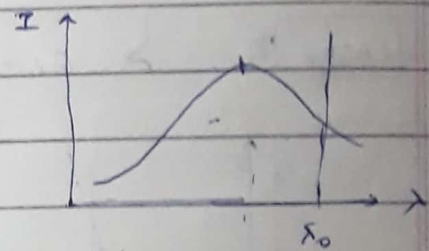
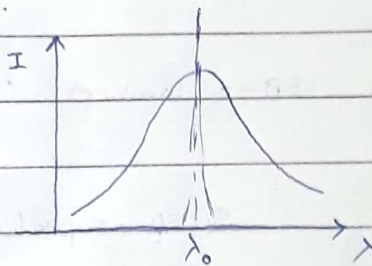


Quality Factor : $\frac{f_0}{\Delta f}$

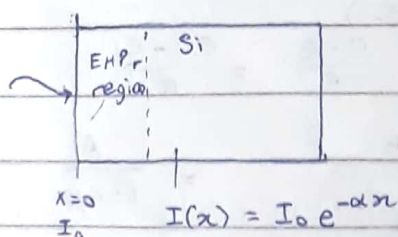
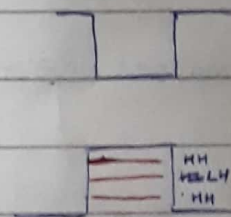
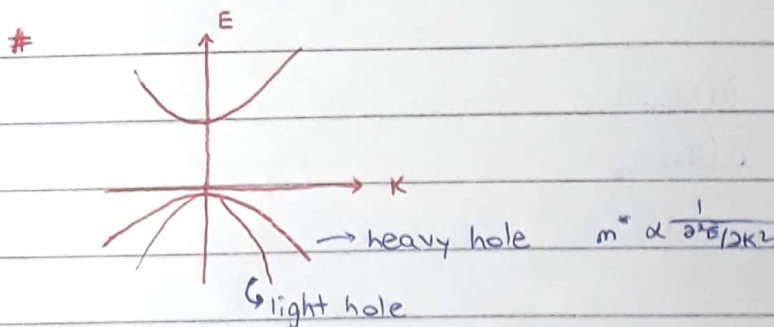


$\beta = \frac{L_{out}}{L_{reflect}}$ $\beta = \frac{\text{fraction of reflected}}{\text{fraction of input}}$

$L = \frac{\lambda_0}{2}$



lower A \Rightarrow need larger β



$\alpha = \alpha(\lambda, T)$ \Rightarrow Any wavelength longer than E_g , will penetrate more (material is more transparent)

$\frac{1}{\alpha}$ = penetration depth

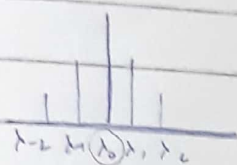
Min Pumping in more carriers

→ Gain increases due to greater recombination

→ Peak shifts to higher energy \Rightarrow wavelength shifts \Rightarrow CHIRP

- \hookleftarrow higher energy tail is also occupied
- temp increases \hookleftarrow

* for precision use, LASER is left on ~~for~~ (idle) to result in eq^m temp (no chirp)



Peak is due to maxima of gain

(λ_i satisfies boundary condition)

$$L = \frac{n\lambda_i}{2}$$

Multimode LASER

↓ optical filter

Singlemode LASER

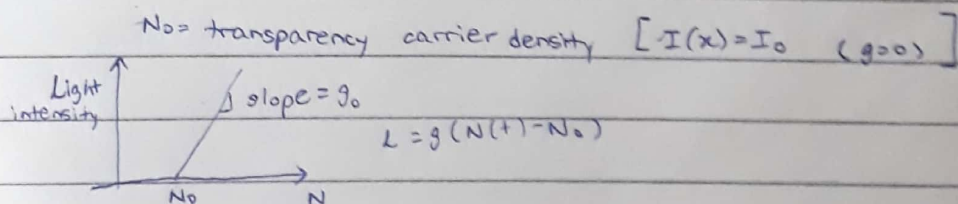
LASER RATE EQⁿ

$N = e^-$ density

$I(t) = \text{current}$

$V_a = \text{active volume of device}$

$$\frac{dN(t)}{dt} = \frac{I(t)}{qV_a} - \underbrace{g_0 \frac{[N(t) - N_0] \cdot S(t)}{1 + \epsilon \cdot S(t)}}_{\text{stimulated emission}} - \underbrace{\frac{N(t)}{\tau_0}}_{\text{spontaneous emission}}$$



$S(t) = \text{photon density}$

$\epsilon = \text{gain compression factor}$ (if too many photons, gain is slightly lesser)

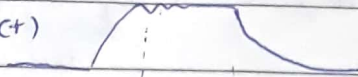
$$\frac{dS(t)}{dt} = \Gamma \cdot g_0 \frac{[N(t) - N_0] \cdot S(t)}{1 + \epsilon S(t)} - \underbrace{\frac{S(t)}{\tau_p} + \frac{\Gamma \cdot \beta}{\tau_0} N(t)}_{\text{rate at which photons leave the system}}$$

Γ : photon confinement factor

β : fraction of recombination that is radiative

Relaxation Oscillation

More e^- \rightarrow more photons \rightarrow stimulated emission \rightarrow e^- builds up
stops
photons decrease

 $I(t)$  $N(t)$  $S(t)$ 