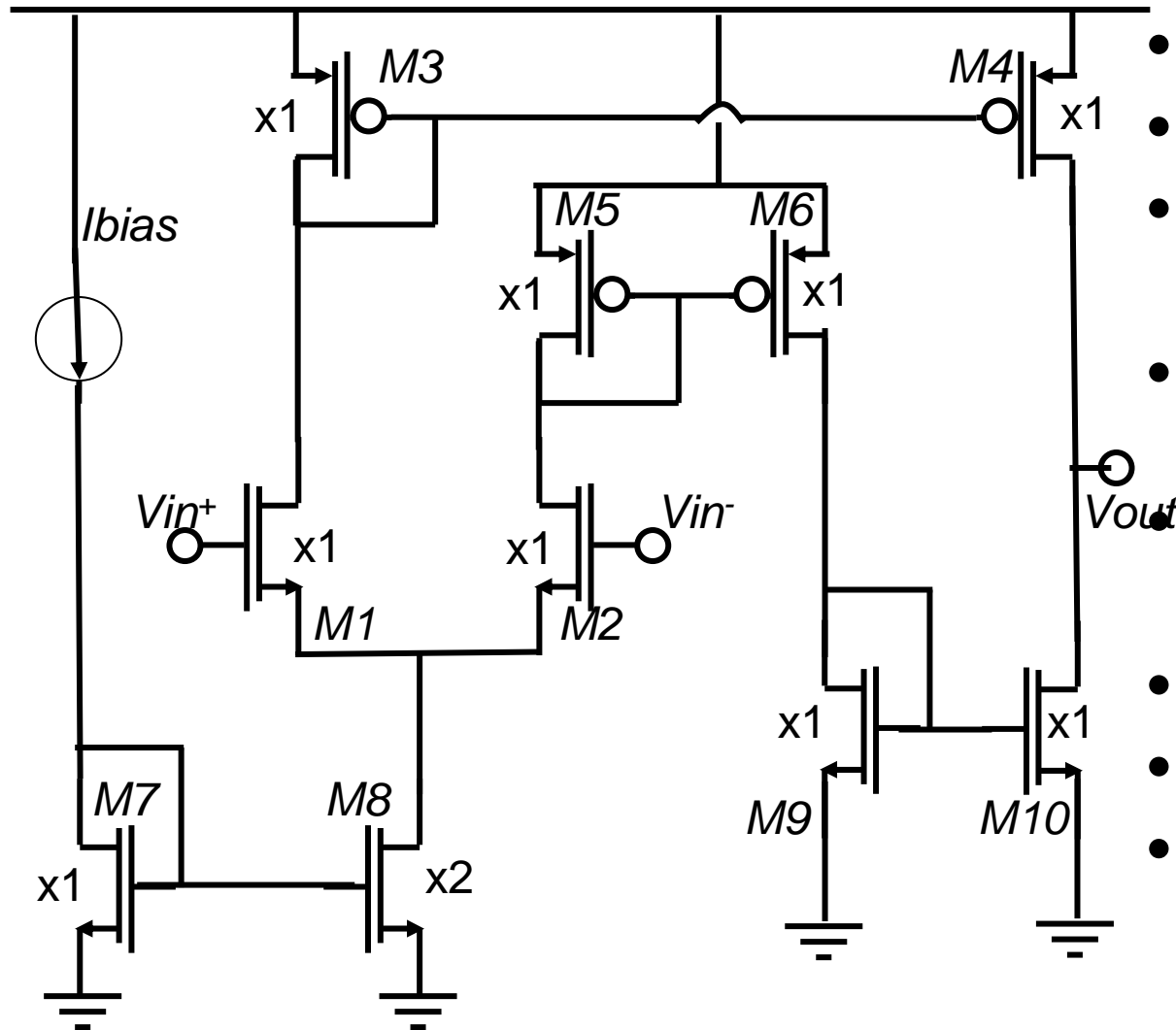


# Lecture 15

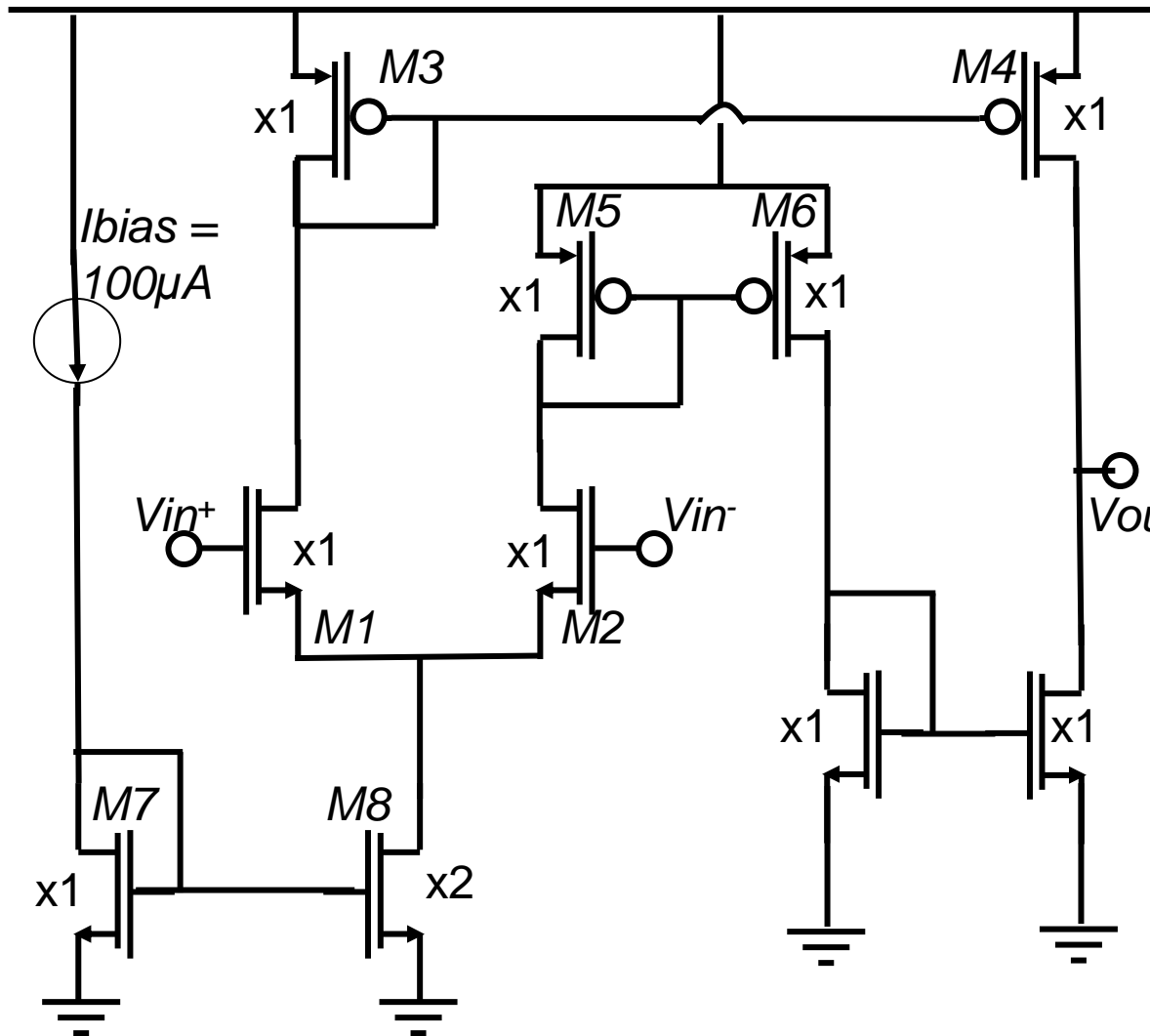
more op-amps

# mirrored = similar gain



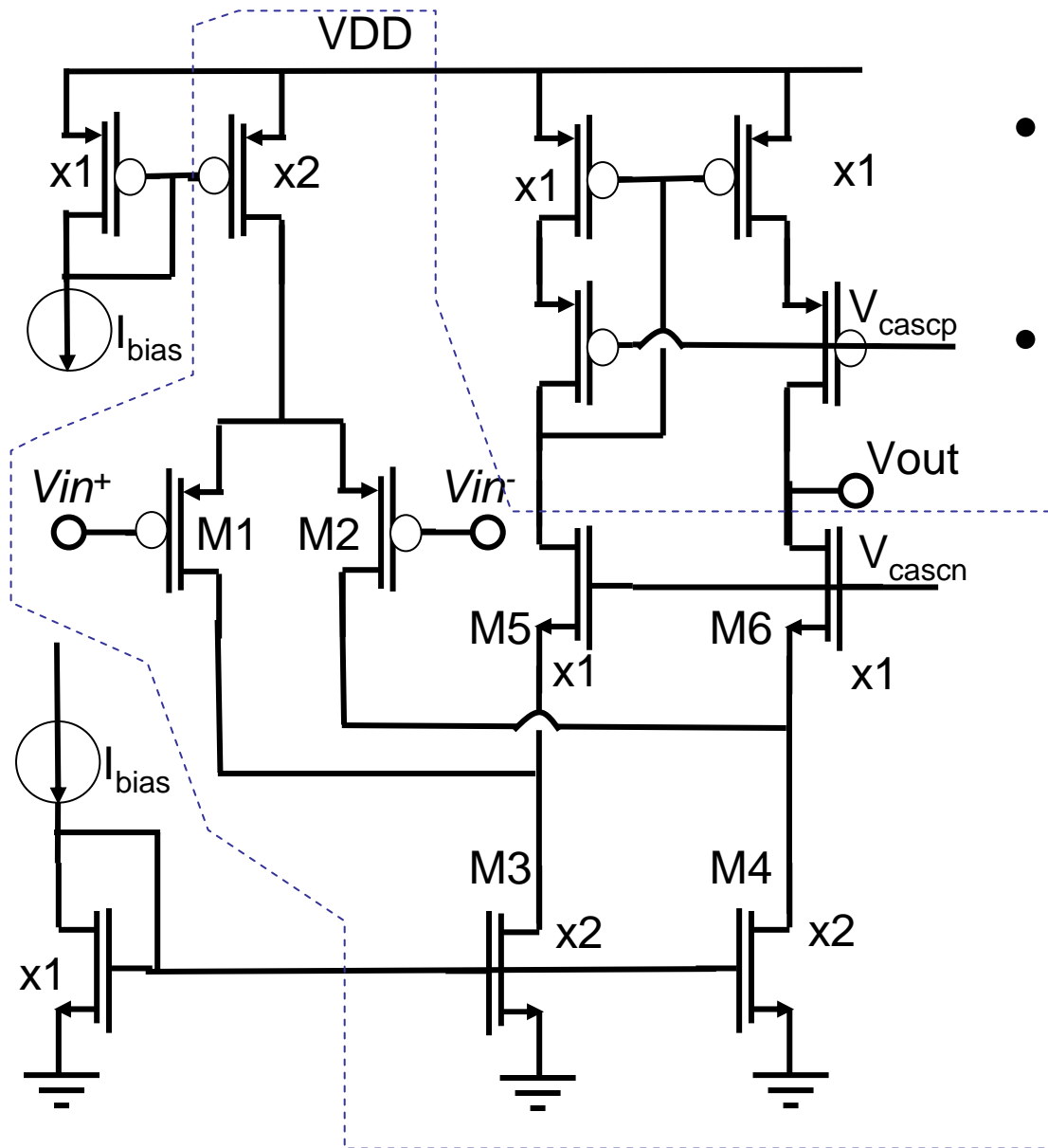
- If  $V_{in}^+ = -V_{in}^- = V_d/2$
- $I_{d1} = I_{bias} + g_{m_n} V_d/2$
- $I_{d2} = I_{bias} - g_{m_n} V_d/2$
- $I_{d4} = I_{d3} = I_{d1}$   
 $= I_{bias} + g_{m_n} V_d/2$
- $I_{d10} = I_{d9} = I_{d6} = I_{d5} = I_{d2}$   
 $= I_{bias} - g_{m_n} V_d/2$
- $I_{out} = I_{d4} - I_{d10}$   
 $= g_{m_n} V_d$
- $V_{out} = I_{out} \cdot R_{out}$
- $R_{out} = r_{on} \parallel r_{op}$
- $\text{Gain} = g_{m_n} (r_{on} \parallel r_{op})$

# mirrored = higher output range



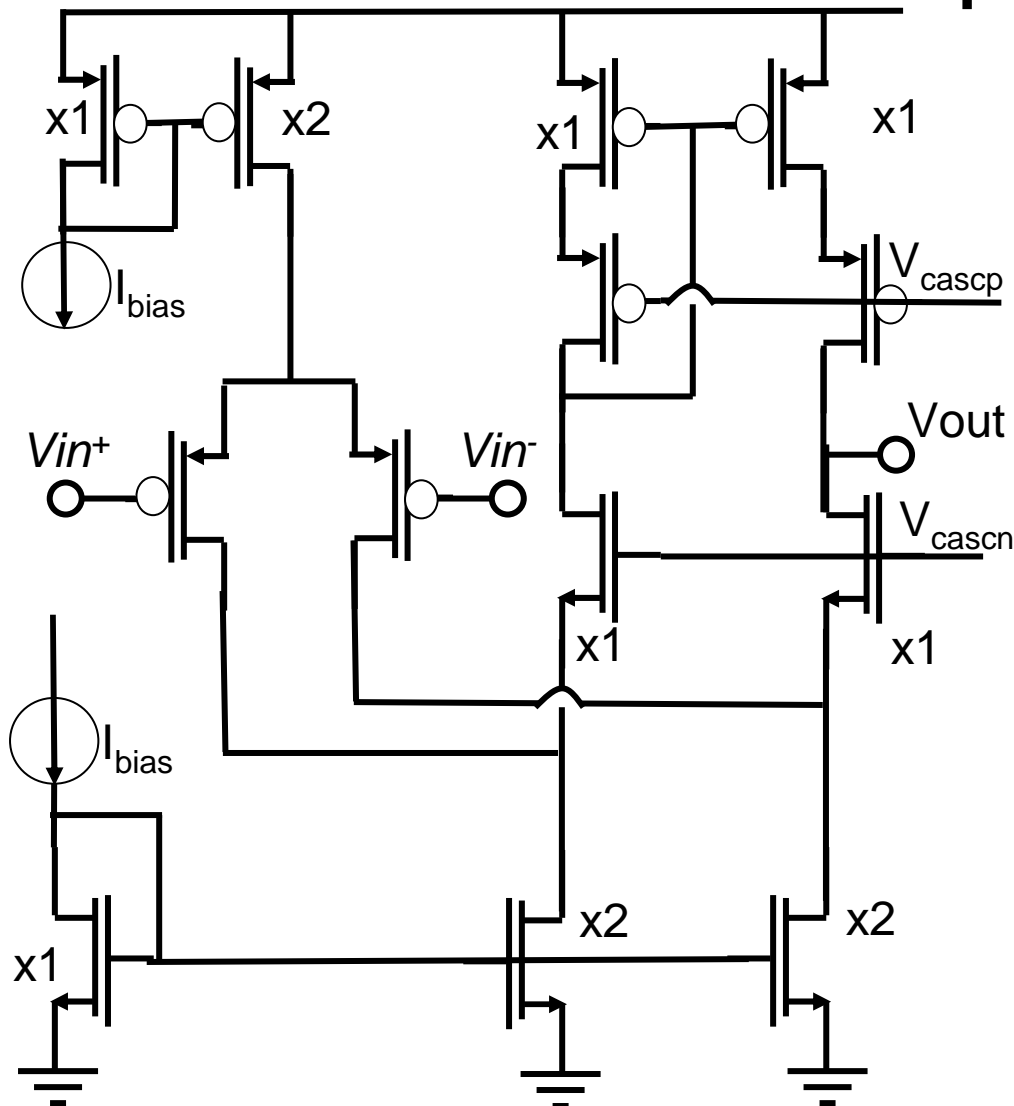
- Compared to basic op-amp, adding mirrors on output
- same gain
  - $\sim gm(r_{on} || r_{op})$
- same  $r_{out}$  (not so good)
  - $\sim r_{on} || r_{op}$
- Same max output current
- $\sim$ same added mirror pole
  - At  $gm/2C_{gs}$
  - Not too bad
- $\sim$ same CMRR
- same input range
- better output range
  - $V_{out} < V_{DD} - V_{ODP}$
  - $V_{out} > V_{ODN}$
- More dc current consumed
- Can increase gain w/cascodes at output (costs some output range)

# Folded cascode



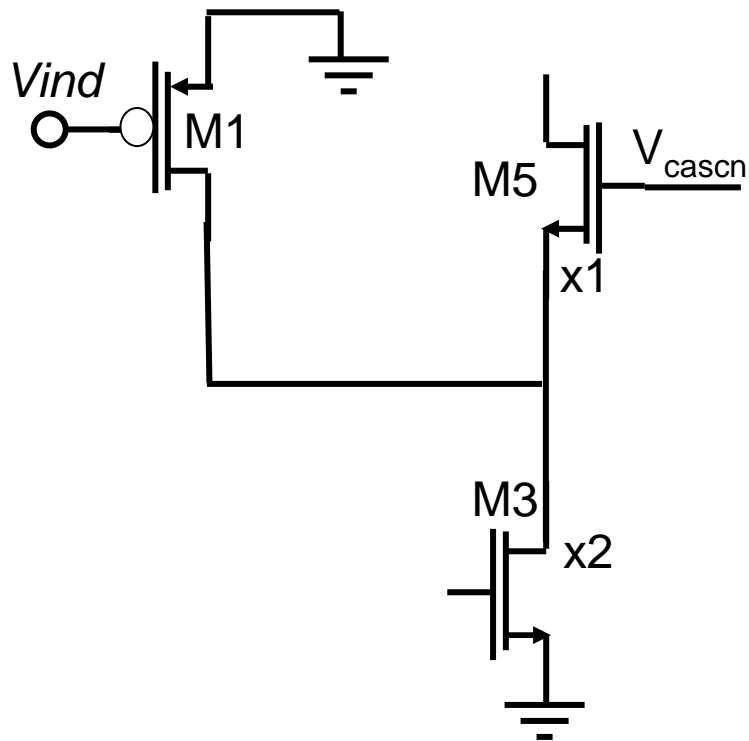
- “bottom part” (inside dashed line) of interest:
  - top part same as telescopic
- DC analysis
  - $I_{D1} = I_{bias} - gmV_{din}/2$
  - $I_{D2} = I_{bias} + gmV_{din}/2$
  - $I_{D3} = I_{D4} = 2I_{bias}$
  - KCL:  $I_{D5} = I_{D3} - I_{D1}$
  - KCL:  $I_{D6} = I_{D4} - I_{D2}$
  - $I_{D5} = I_{bias} + gmV_{din}/2$
  - $I_{D6} = I_{bias} - gmV_{din}/2$

# Folded cascode = high gain, different input range

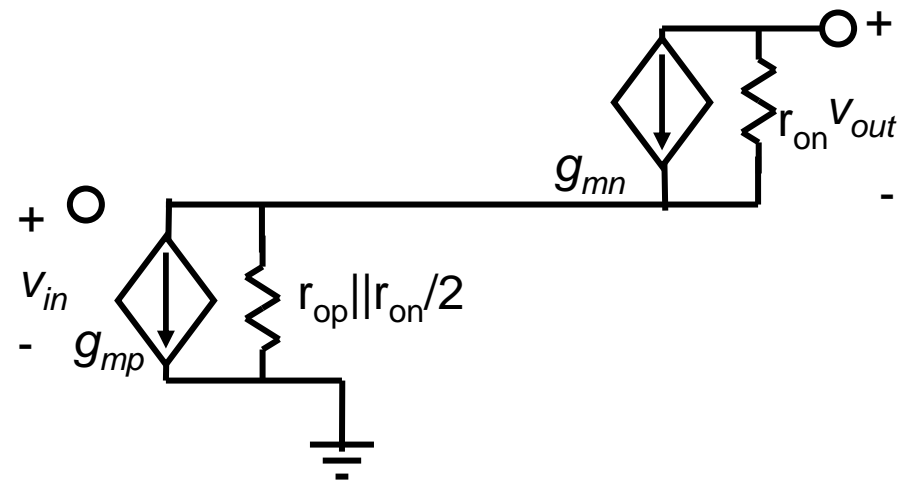
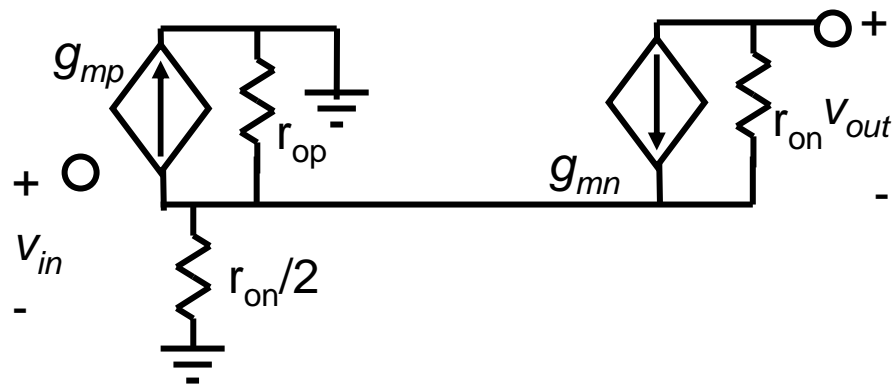


- Compared to telescopic op-amp, folded cascodes
- similar gain (good)
  - $\sim (g_m r_o)^2$  vs  $g_m r_o$
  - Really slightly lower:
    - $g_{mp}((r_{op} || r_{ob}) g_{mn} r_{on}) || (g_{mp} r_{op}^2)$
    - $r_{ob} \sim r_{on}/2$
- similar rout (not so good)
  - $((r_{op} || r_{ob}) g_{mn} r_{on}) || (g_{mp} r_{op}^2) \sim g_m r_o^2$
- Same max output current
- ~same BW besides output pole
- ~same CMRR
- Better input range
  - $V_{in} > V_{ODn} - V_{THp} < 0$  !!!!
  - $V_{in} < V_{DD} - 2V_{OD} - V_{THp}$
  - Can go below ground!
- Better output range ( $V_{cascn}$  can be low)
  - $V_{out} < V_{cascp} + |V_{THp}|$
  - $V_{out} > V_{cascn} - |V_{THN}|$

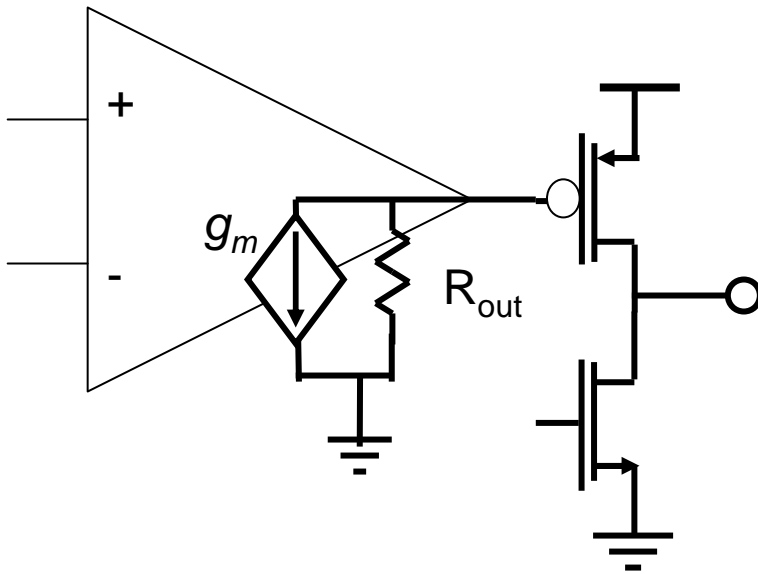
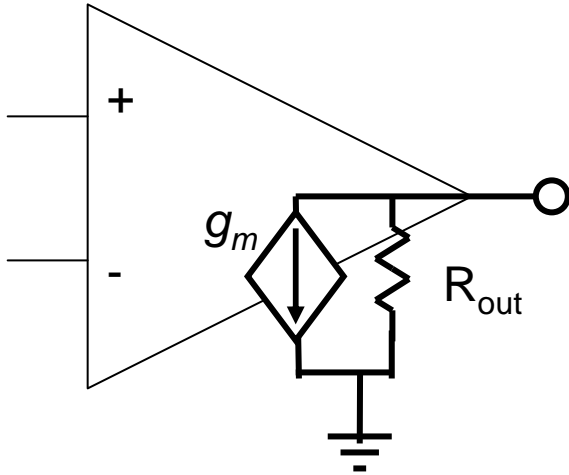
# Folded cascode: half circuit



- SS analysis
- Ss half circuit:
  - Same as cascode, except
  - Input pfet, cascode nfet
  - Mirror (m3) rout in parallel with CS output
- So  $R_{out} = g_{mn} \cdot r_{on} \cdot (r_{op} \parallel r_{on}/2)$

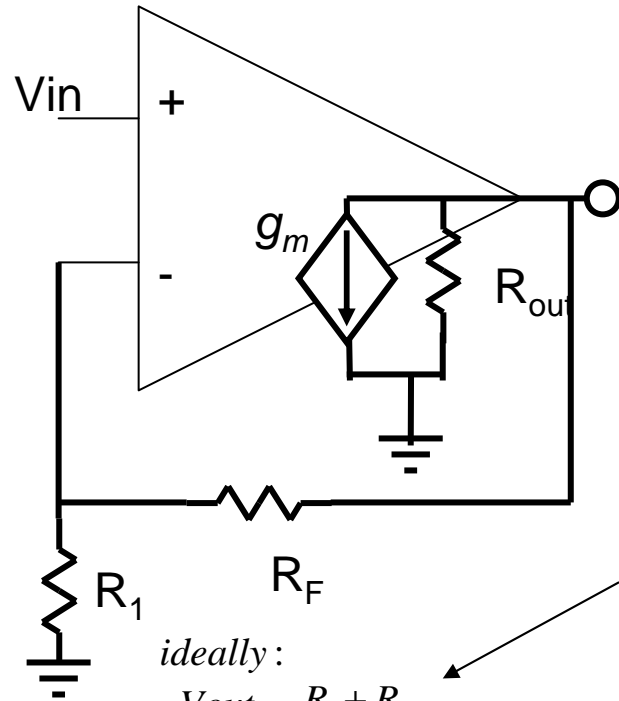


# 1 vs 2-stage OP-Amps



- 1-stage Op-Amps (OTAs)
  - Simple
  - Telescopic
  - Mirrored
  - Folded cascode
- All OTAs Have  $A = g_m R_{out}$ 
  - Where  $g_m$  is that of a single transistor ( $2I_d/V_{od}$ )
  - Get more gain with bigger  $R_{out}$  (cascode, etc)
  - Dominant pole on output:
  - $\omega_p = 1/((R_{out} || R_L)(C_L + 2C_{db}))$
- 2-stage: take OTA, add 2<sup>nd</sup> stage: usually CS
- Get  $A = A_{OTA} * g_m R_{out}$
- So separate gain from  $R_{out}$
- Can separately design input/output
- Get output pole, plus intermediate pole at OTA output:
  - $\omega_p = 1/((R_{outOTA})(C_{GS} + 2C_{db}))$

# 1 vs 2-stage OP-Amps: feedback effects



ideally:

$$\frac{V_{out}}{V_{in}} = \frac{R_1 + R_f}{R_1}$$

really

$$\frac{V_{out}}{V_{in}} = \frac{g_m R_{out} (R_1 + R_f)}{g_m R_{out} R_1 + R_1 + R_f + R_{out}}$$

$R_{out} \rightarrow \infty$

$$\frac{R_1 + R_f}{R_1 + \frac{1}{g_m}}$$

Resistive FB: Get gain error!

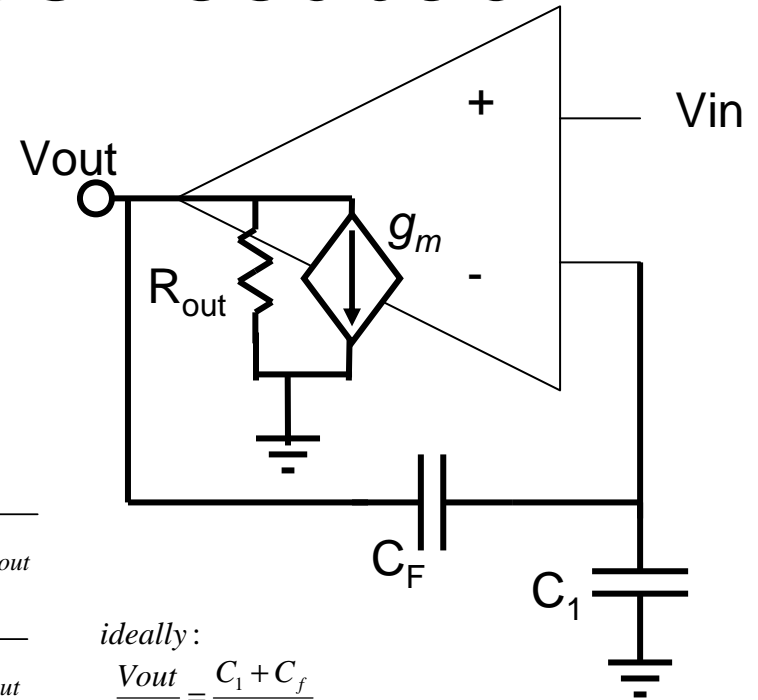
$V_{out}$  ideally:

$$\frac{V_{out}}{V_{in}} = \frac{Z_1 + Z_f}{Z_1}$$

really

$$\begin{aligned} \frac{V_{out}}{V_{in}} &= \frac{A(Z_1 + Z_f)}{AZ_1 + Z_1 + Z_f + R_{out}} \\ &= \frac{g_m R_{out} (Z_1 + Z_f)}{g_m R_{out} Z_1 + Z_1 + Z_f + R_{out}} \end{aligned}$$

As send  $R_{out} \rightarrow \infty$



ideally:

$$\frac{V_{out}}{V_{in}} = \frac{C_1 + C_f}{C_f}$$

really

$$\begin{aligned} \frac{V_{out}}{V_{in}} &= \frac{g_m R_{out} \left( \frac{1}{j\omega C_1} + \frac{1}{j\omega C_f} \right)}{g_m R_{out} \frac{1}{j\omega C_1} + \frac{1}{j\omega C_1} + \frac{1}{j\omega C_f} + R_{out}} \\ &= \frac{g_m R_{out} (j\omega C_f + j\omega C_1 + j\omega C_f j\omega C_1)}{g_m R_{out} j\omega C_f + j\omega C_1 + j\omega C_f + j\omega C_f j\omega C_1} \\ &\xrightarrow{R_{out} \rightarrow \infty} \frac{C_1 + C_f}{C_f} \frac{1}{1 + j\omega \frac{C_1}{g_m}} \end{aligned}$$

Capacitive FB: Get pole, but gain right