

Lecture 20

Compensation and stabilization

Example: telescopic, 2-stage Op-Amp

- What are gain, poles?

Gain:

$$A_o = g_{mn} (g_{mn} r_{on}^2 \parallel g_{mp} r_{op}^2) g_{mp} (r_{on} \parallel r_{op})$$

1st stage output pole (dominant):

$$p_1 = \frac{1}{(g_{mn} r_{on}^2 \parallel g_{mp} r_{op}^2) (C_{gs} + 2C_{db})}$$

2nd stage output pole (depends on load):

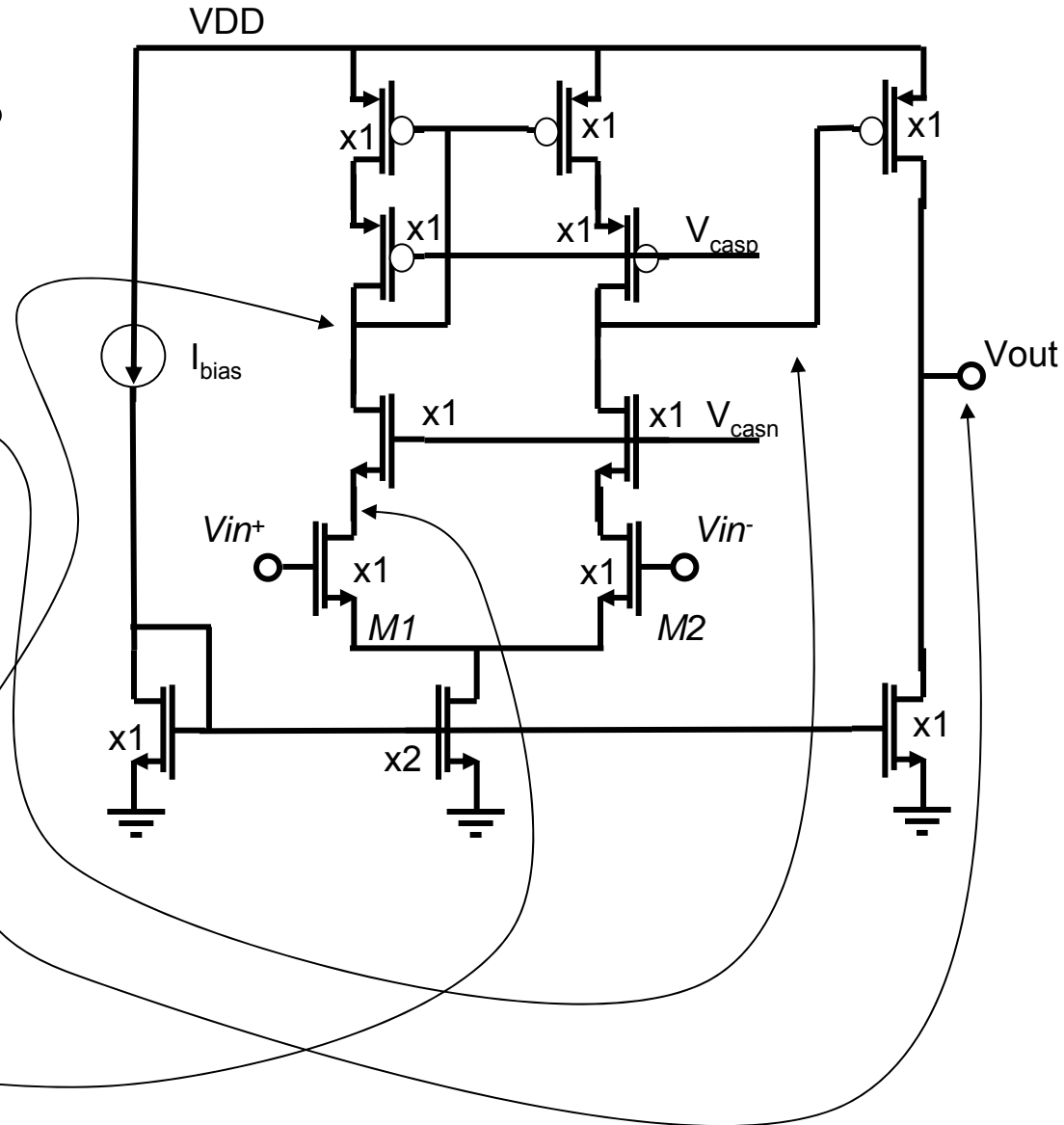
$$p_2 = \frac{1}{(r_{on} \parallel r_{op} \parallel R_L) (C_L + 2C_{db})}$$

mirror pole:

$$p_3 = \frac{g_{mp}}{(2C_{gs} + 2C_{db})}$$

cascode pole:

$$p_4 = \frac{g_{mn}}{(C_{gs} + C_{db} + C_{sb})}$$



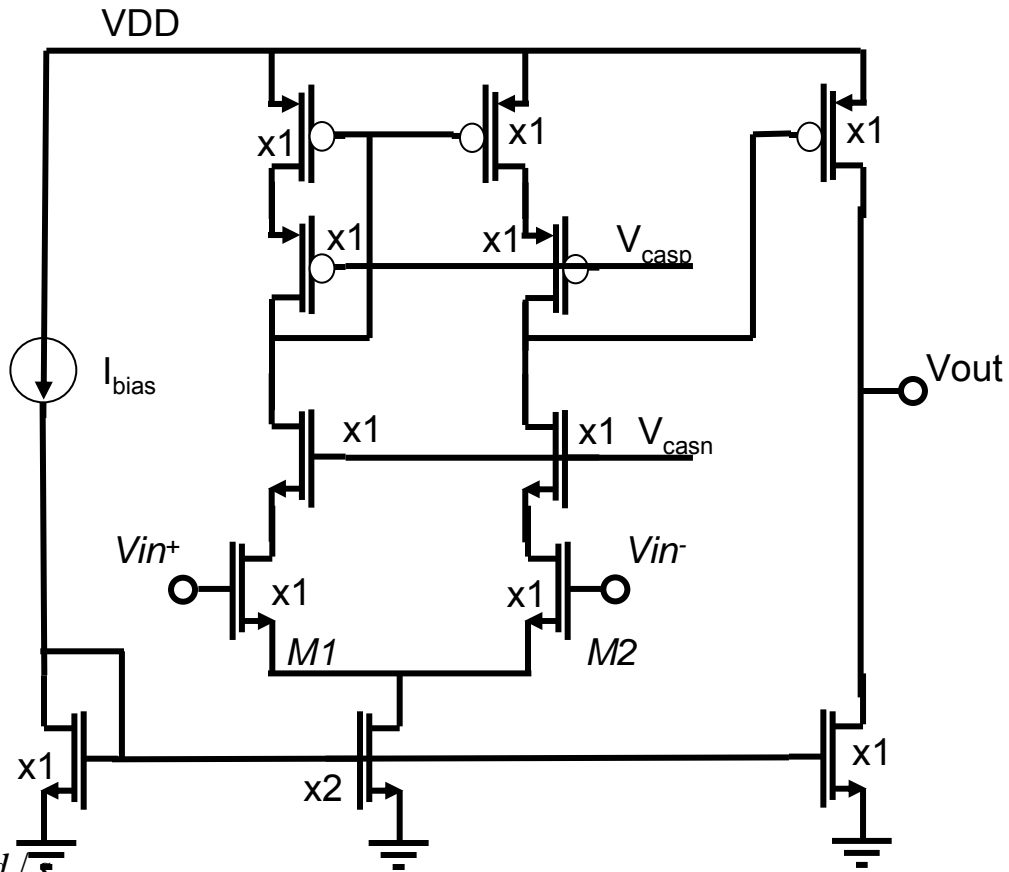
Example: telescopic, 2-stage Op-Amp

- Make up some reasonable numbers:
 - Set $g_m r_o = 10$
 - Set $\omega_T = 100 \text{ Grad/s}$ (16GHz): $\omega_T \sim g_m / C_{gs}$
(note, in real life n- and p-fets have different ω_T 's)
 - Set $C_{db} = C_{gs} / 2$
- Set $R_L = \infty$, $C_L = 0$
- Now:

$$A_o = (g_m r_o)^3 / 4$$

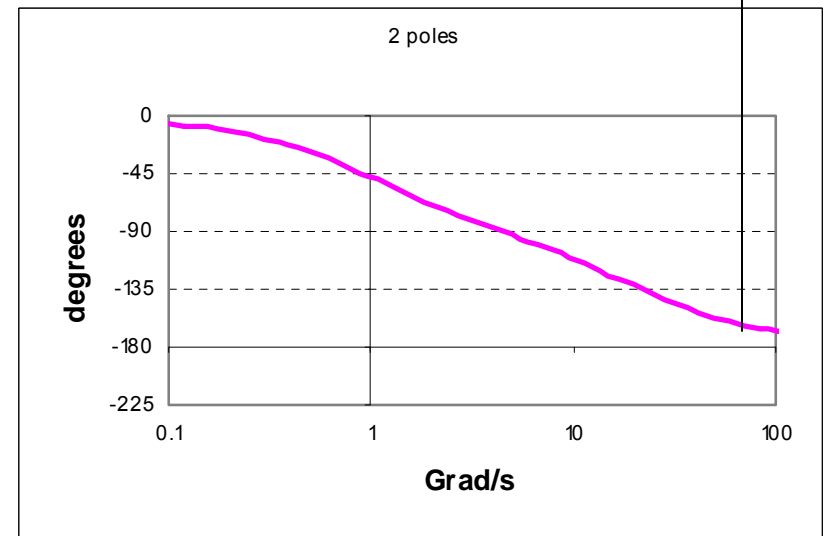
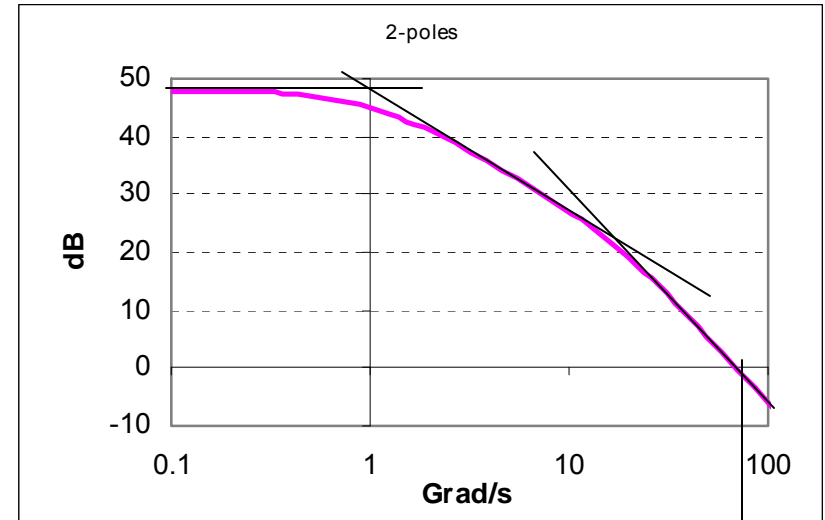
$$p_1 = \frac{1}{(g_m r_o)^2 / 2 (2C_{gs})} = \frac{g_m}{(g_m r_o)^2 C_{gs}} = \frac{\omega_T}{100}$$

$$p_2 = \frac{1}{r_o C_{db}} = \frac{2g_m}{(g_m r_o) C_{gs}} = \frac{\omega_T}{5} = 20 \text{ Grad} / s$$



Example: telescopic, 2-stage Op-Amp

- Find UGBW in this case (just looking at 2 poles)
- For $p_1 < \omega < p_2$,
 - $A(\omega) = A_o * p_1 / \omega$
 - So at $\omega = p_2$, $A(p_2) \sim A_o * p_1 / p_2$
 - In this case, $A(p_2) \sim 250 * 1G / 20G = 12.5$ (22dB)
- For $\omega > p_2$,
 - $A(\omega) = A(p_2) * p_2^2 / \omega^2$
- UGBW where $A(\omega) = 1$
 - $A(p_2) * p_2^2 / \omega^2 = 1$
 - $\omega_{UG} = (A(p_2) * p_2^2)^{1/2}$
 - In this case:
 - $\omega_{UG} = 20 \text{ Grad/s} * (12.5)^{1/2}$
 - UGBW = 70 Grad/s



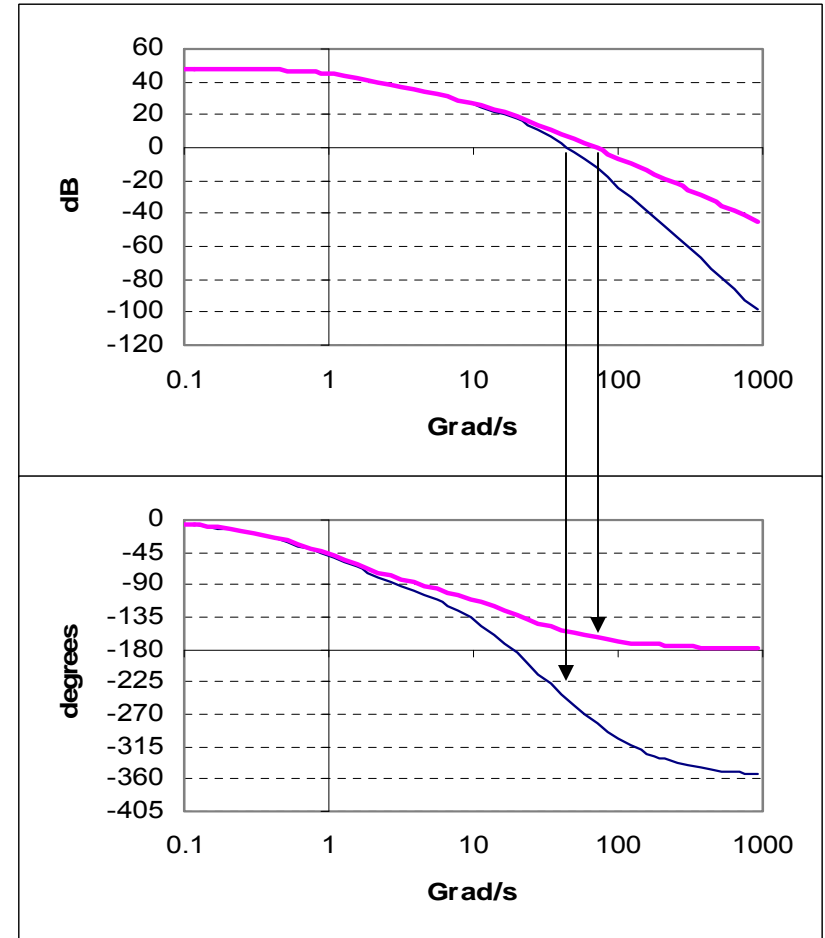
Example: telescopic, 2-stage Op-Amp

- So make a Bode plot:
 - PM is $\sim 17^\circ$
- But we *know* there are more poles:

$$p_3 = \frac{g_m}{(2C_{gs} + 2C_{db})} = \frac{\omega_T}{3} = 33 \text{ Grad} / s$$

$$p_4 = \frac{g_{mn}}{(C_{gs} + 2C_{db})} = \frac{\omega_T}{2} = 50 \text{ Grad} / s$$

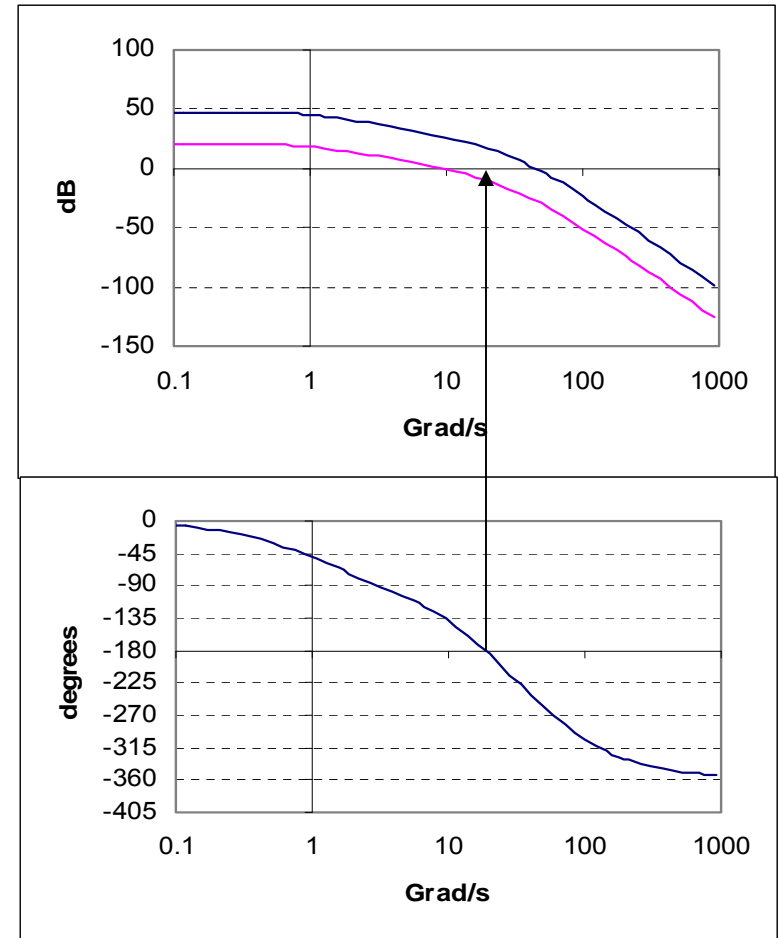
- These will have marginal effects on UGBW,
 - From 70 Grad/s to 45 Grad/s
- But big effect on PM
 - 17° shifts to -70°



This is $A(s)$... if we set $B_o = 1$ (unity gain) this will NOT be STABLE!

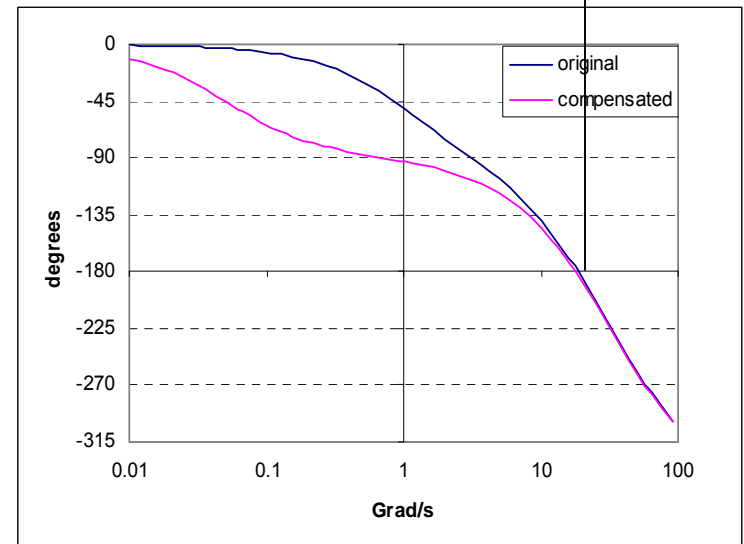
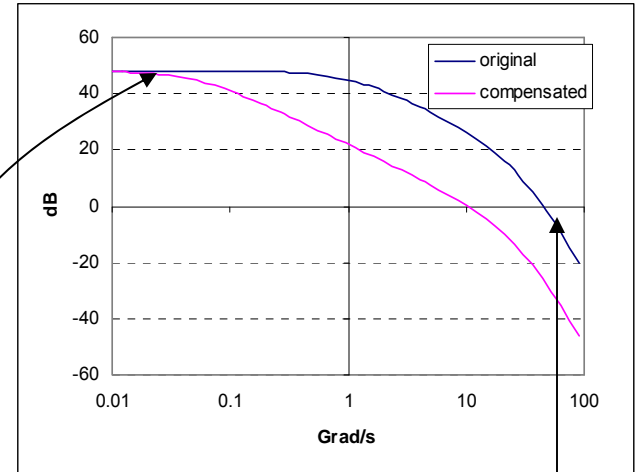
How stabilize?

- 1st way: reduce gain:
- If know can use $B_o < 1$, do so
 - remember $H_o \sim 1/B_o$
- If don't need large A_o , reduce gain other ways: lower g_m of diff pair, etc.
- Try to get $UGBW < p_2$:
 - $A(p_2) = 22\text{dB}$
 - So reduce gain by at least 22dB
- Alternately reduce $A_o B_o$ to get 10dB gain margin
 - Here, $GM = -17\text{dB}$
 - So reduce $A_o B_o$ by 27dB
- Problem is, of course, that this kills your gain!



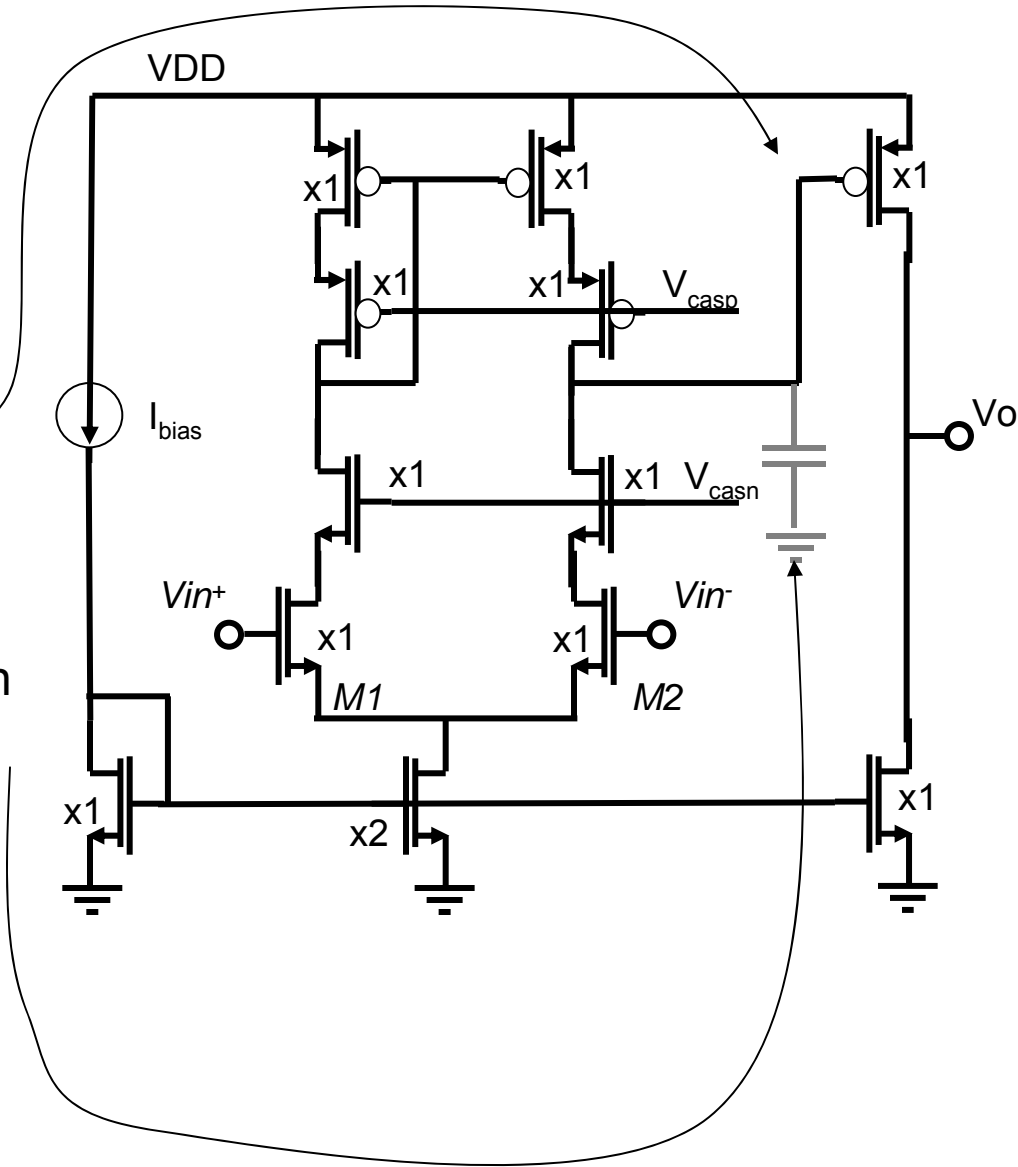
Compensation

- 2nd way: reduce dominant pole location:
- Every factor of ten lower is 20dB less gain at high frequencies
 - Reduce $A(p_2)$ by 22dB:
 - implies lower p_1 by 22dB (12.5)
- Or reduce pole for a 10dB GM:
 - Here GM = -17
 - So reduce by 27dB: a factor of ~20
 - Move p_1 to 50Mrad/s
 - Note HF phase barely changes, but gain drops



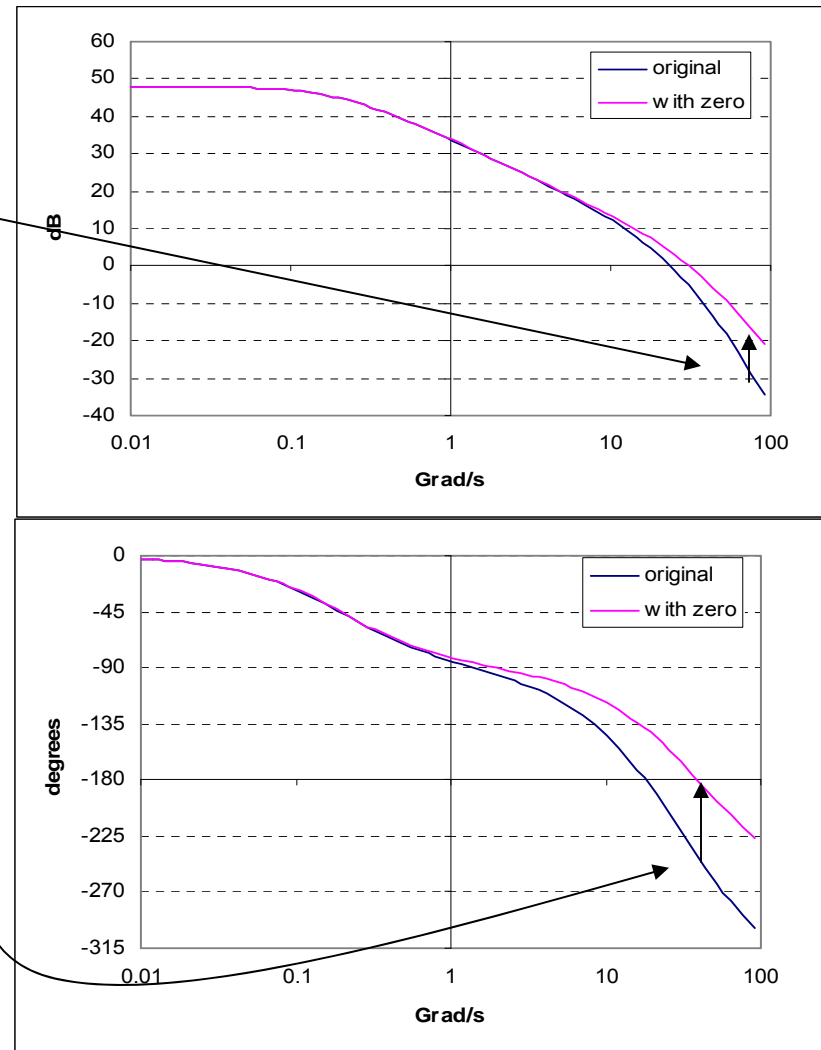
Compensation: how?

- Need to reduce dominant pole frequency
 - In example by a factor of ~ 20
 - How?
- Easiest way: add capacitance to dominant pole node
 - R is highest here, so least C required.
 - Add a capacitor with $C = 19 \times$ the parasitic cap
 - Can do this with an PFET with large W, L to make a MOS Cap.
- This costs bandwidth.
- (Note, for better PSRR in this case, would tie cap to VDD)



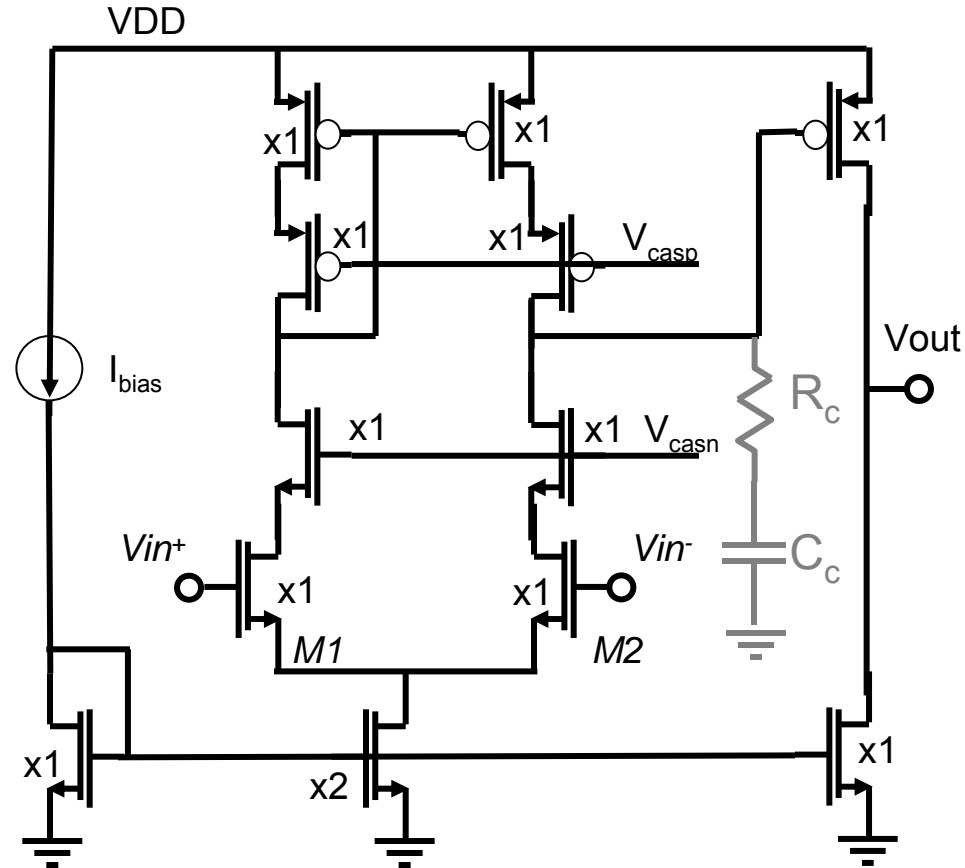
Adding a zero

- 3rd trick: add a zero:
 - Increases HF gain by 20dB/dec(Bad)
 - But also increases HF phase by up to 90° (good)
 - Can place zero near 2nd pole to cancel phase effects while still keeping 1 pole of roll-off
 - Usually have to combine with compensation (see next slide)
- Here,
 - move $p_1 \rightarrow 200\text{Mrad/s}$
 - Add zero at 20Grad/s
 - GM from -5dB to 4dB
 - PM from -20° to 15°
- Less of a BW hit.



Adding a zero: how?

- Put a resistor in series with dominant capacitor
 - Changes Z_C from $1/j\omega C_c$
 - To $(1+j\omega R_c C_c)/j\omega C_c$
- Pole at $2/(g_m r_o^2 C_c)$
- Zero at $1/R_c C_c$
- 2nd pole at $1/R_c (C_{gs} + 2C_{db})$
- For $R_c \ll g_m r_o^2$ the 2nd pole doesn't matter.



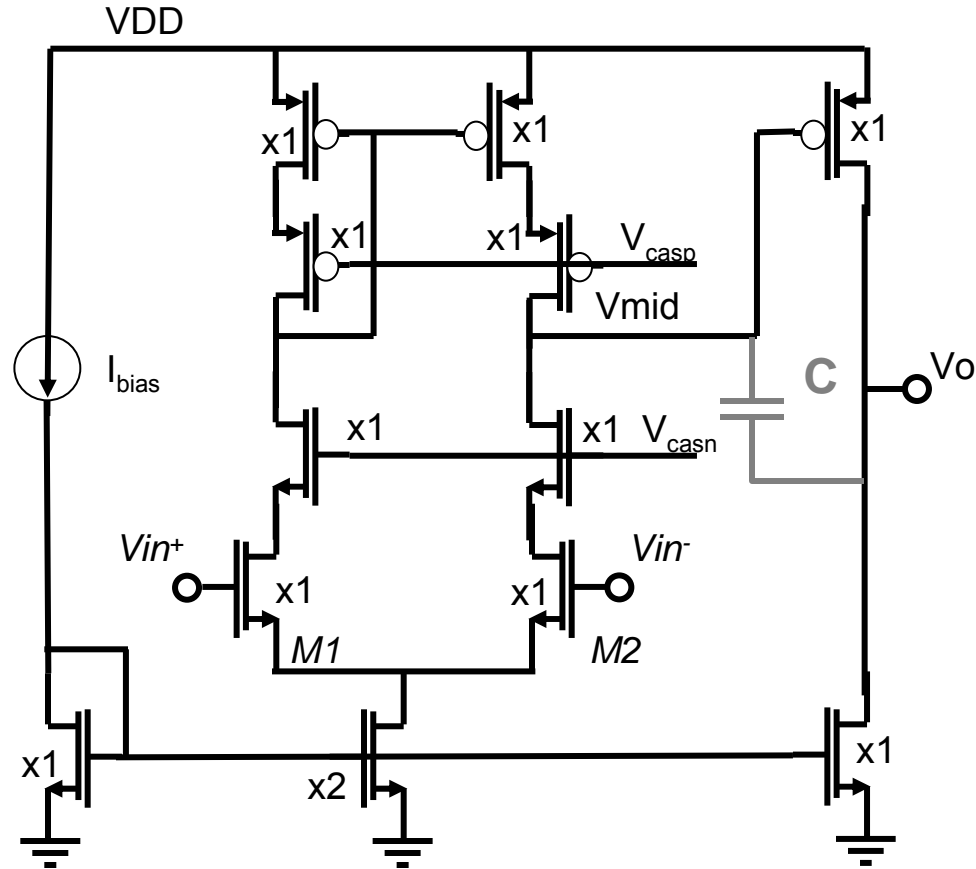
Miller Compensation

- Big capacitors take up a lot of space.
 - Can build effectively larger cap with Miller effect.
 - $C_{eff} = C(1 + g_m(R_L || r_o/2))$
- But really more complicated than that.
- Get transmission zero (RHP)
- Get interactions between midpoint, output
- Get, instead:

$$C_{mid} = C_{gs} + 2C_{db}$$

$$C_L' = 2C_{db} + C_L$$

$$R_L' = R_L \parallel \frac{r_o}{2}$$



$$\frac{V_{out}}{V_{in}} = \frac{g_m \left(\frac{g_m r_o^2}{2} \right) R_L' (sC - g_m)}{1 + s \left(R_L' (C_L' + C) + \left(\frac{g_m r_o^2}{2} \right) (C_L' + C_{mid} + C(1 + g_m R_L')) \right) + s^2 \left(\frac{g_m r_o^2}{2} \right) R_L' (C_L' C_{mid} + C C_{mid} + C_L' C)}$$

Miller Compensation

- What a mess! But we can interpret: assume

- $C_{mid} \ll C, g_m r_o^2 \gg R_L' \longrightarrow$

$$\frac{V_{out}}{V_{in}} = \frac{g_m \left(\frac{g_m r_o^2}{2} \right) R_L' (sC - g_m)}{1 + s \left(R_L' (C_L' + C) + \left(\frac{g_m r_o^2}{2} \right) (C_L' + C_{mid} + C(1 + g_m R_L')) \right) + s^2 \left(\frac{g_m r_o^2}{2} \right) R_L' (C_L' C_{mid} + C C_{mid} + C_L' C)}$$

- $g_m R_L > 1, g_m R_L' C \gg C_L' \longrightarrow$

$$\frac{V_{out}}{V_{in}} = \frac{g_m \left(\frac{g_m r_o^2}{2} \right) R_L' (sC - g_m)}{1 + s \left(\left(\frac{g_m r_o^2}{2} \right) (C_L' + C(1 + g_m R_L')) \right) + s^2 \left(\frac{g_m r_o^2}{2} \right) R_L' (C C_{mid} + C_L' C)}$$

- 1st pole where
Just Rout of OTA and
Millerized cap

$$1 \approx s \left(\left(\frac{g_m r_o^2}{2} \right) (C(g_m R_L')) \right) \Rightarrow p_1 \approx \frac{1}{\frac{g_m r_o^2}{2} C(g_m R_L')}$$

- 2nd pole where:
Basically original output
pole increased by gmRL

$$s \left(\left(\frac{g_m r_o^2}{2} \right) (C(g_m R_L')) \right) \approx s^2 \left(\frac{g_m r_o^2}{2} \right) R_L' (C C_{mid} + C_L' C)$$

- So for large enough C, p1 moves in as 1/gmRL, p2 moves out as gmRL: "pole splitting"

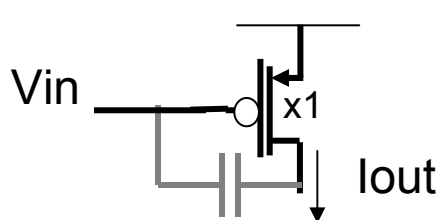
$$p_2 = \frac{\left(\frac{g_m r_o^2}{2} \right) (C(g_m R_L'))}{\left(\frac{g_m r_o^2}{2} \right) R_L' (C C_{mid} + C_L' C)} = \frac{(g_m R_L')}{R_L' (C_{mid} + C_L' C)}$$

Vo

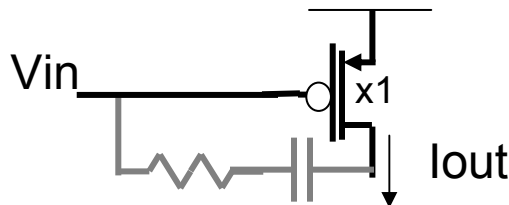
That pesky RHP zero

$$\frac{V_{out}}{V_{in}} = \frac{g_m \left(\frac{g_m r_o^2}{2} \right) R_L' (sC - g_m)}{1 + s \left(R_L' (C_L' + C) + \left(\frac{g_m r_o^2}{2} \right) (C_L' + C_{mid} + C(1 + g_m R_L')) \right) + s^2 \left(\frac{g_m r_o^2}{2} \right) R_L' (C_L' C_{mid} + C C_{mid} + C_L' C)}$$

- Miller compensation lowers dominant pole
 - But PM not much better
 - RHP zero adds phase
 - may increase UGBW too
- Can cancel with series R



$$\frac{I_{out}}{V_{in}} = -g_m + sC$$



$$\frac{I_{out}}{V_{in}} = -g_m - sgmRC + sC$$

If $g_m R > 1 \rightarrow$ zero moves to LHP

