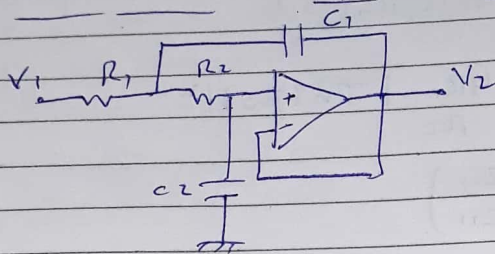


16/11/18

Aux have poles as well as 0's.
 $A_{in}(s) \times B(s)$ have same poles.

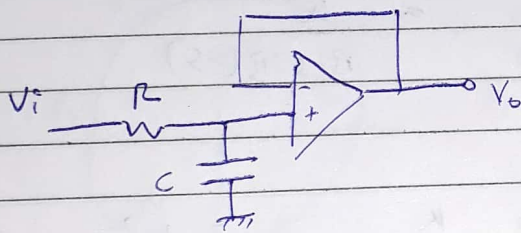
* Butterworth Filter (Sallen-Key Filter)



$$\frac{V_2}{V_1} = \frac{1/R_1 R_2 C_1 C_2}{s^2 + \left(\frac{1}{R_1 C_1} + \frac{1}{R_2 C_1} \right) s + \frac{1}{R_1 R_2 C_1 C_2}}$$

2nd order
lowpass Filter.

$$= \frac{\omega_0^2}{s^2 + \left(\frac{\omega_0}{Q} \right) s + \omega_0^2}$$



1st order filter.

$$\frac{V_o}{V_i} = \frac{1}{1 + sCR}$$

Now just cascade these to get any order filter.

$$R \equiv \frac{1}{C} \cdot 1/R$$

$$\frac{1}{C} \equiv R \cdot 1/C$$

low pass becomes high Pass.

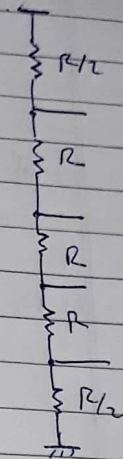
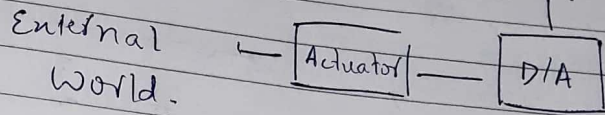
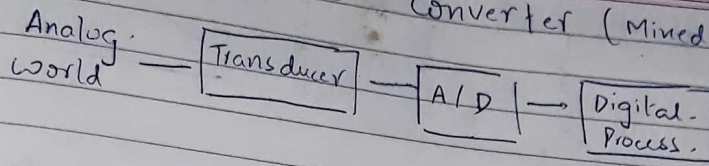
$$s \rightarrow \omega_0'/s \quad \left\{ \omega_0' \rightarrow 3dB \text{ frequency} \right\}$$

lowpass \rightarrow high pass.

Impedance Transformation

16/4/18

D to A and A/D Converter (Mixed Signal Processing)



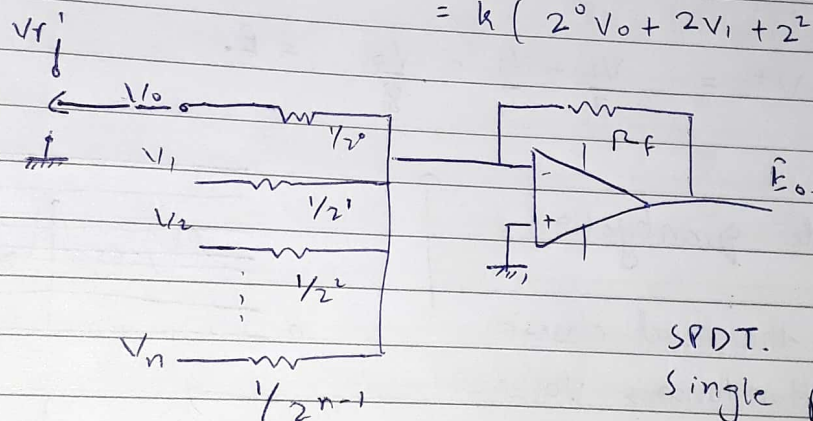
	I/P.		
3 bit I/P.	V_2	V_1	V_0
	0	0	0
	1	0	1
	1	0	0
	1	1	1

$0 \rightarrow 0V$

$1 \rightarrow V_{ref}$

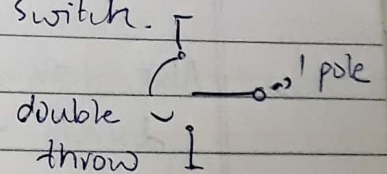
$$E_o = k \sum_{i=0}^{n-1} V_i 2^i$$

$$= k (2^0 V_0 + 2^1 V_1 + 2^2 V_2)$$



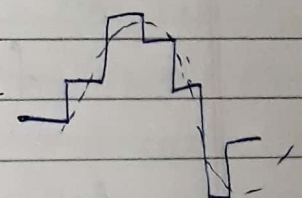
SPDT.

Single pole double throw switch.



Now pass the output through a ~~low~~ filter based on the input or the info abt the signal.

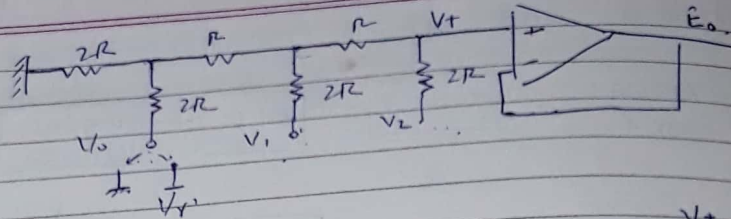
* 2) Weighted Resistor D/A converter.



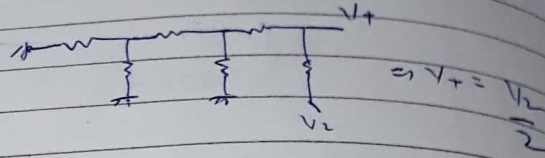
but this depends on resistance values, & which needs to be precise, but resistances are very arbit.

R-2R ladder D/A Converter.

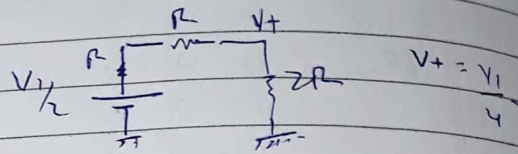
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if $V_2 = 1, V_0 = V_1 = 0$,



Now, $V_2 = V_0 = 0, V_1 = 1$.



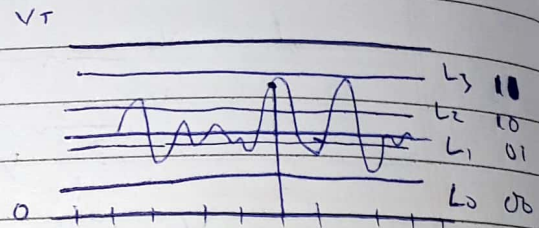
Similarly, $V_0 = 1, V_1 = V_2 = 0$.

$$\Rightarrow V^+ = \frac{V_0}{8}$$

$$\Rightarrow V^+ = \frac{V_2}{2} + \frac{V_1}{4} + \frac{V_0}{8} = E_o$$

Amplitude quantization -

I choose the level closest to instantaneous value.



time quantization

Also, looking at signal only at discrete time -

$$f_s = \frac{1}{T_s}$$

[sampling frequency]

$$f_s > 2f_i$$

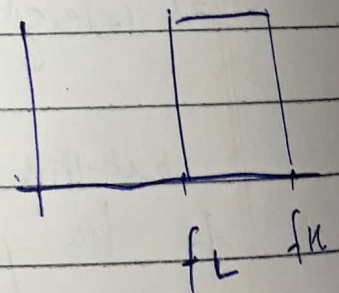
Nyquist relation

Anti-aliasing

if band limited, can do sampling at much lower rate

$$f_s > 2(f_H - f_L)$$

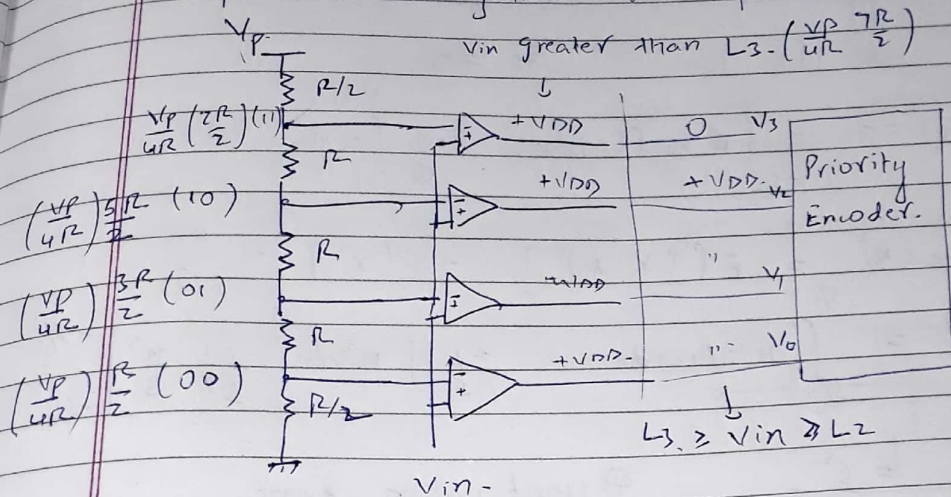
band limited.



f →

Anti-aliasing filter bomp Pass.

amplitude Quantization (as is inf. Time Quantiz. does not.



A/D converter (Flash ADC)

fast. very fast.

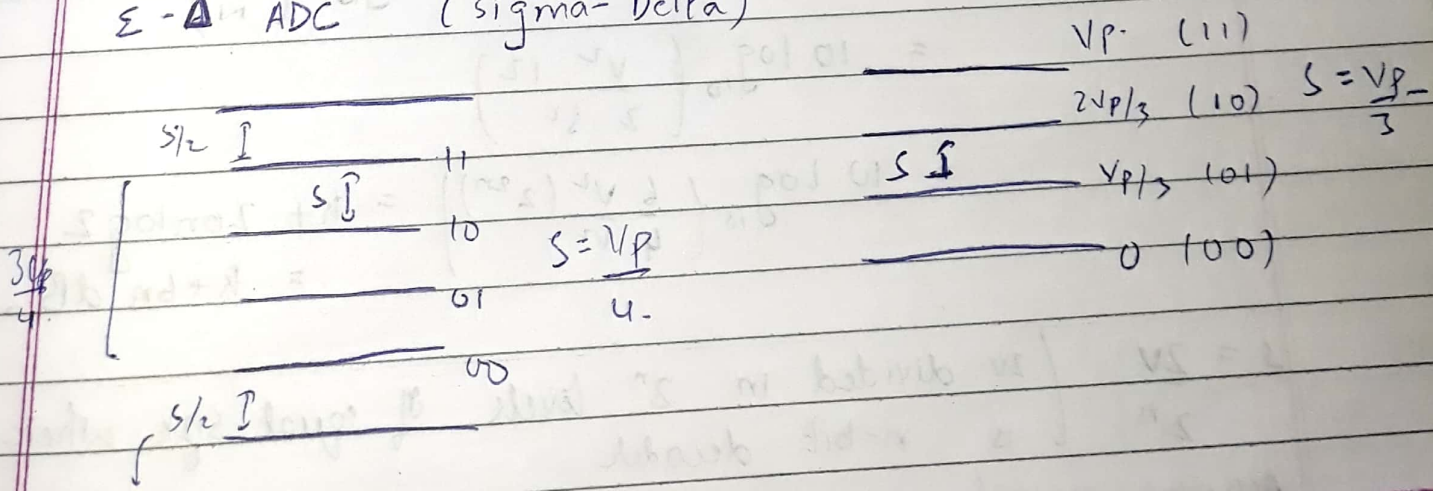
V_3	V_2	V_1	V_0	D_1	D_0
1	x	x	x	1	1
0	1	x	x	1	0
0	0	1	x	0	1
0	0	0	x	0	0

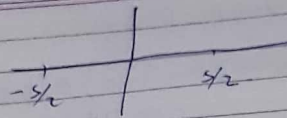
Single Slope A/D Converter-

Dual " " "

Successive Approximation ADC-

$\Sigma - \Delta$ ADC (sigma-Delta)





$f(u) = 1/s$
[uniform - distribution]

$$\bar{u} = 0$$

$$E(u) = 0 = \int_{-s/2}^{s/2} u f(u) du = \frac{1}{s} \int_{-s/2}^{s/2} u du = 0$$

$$\text{Variance}(x) = E[(x - \bar{u})^2] = E[x^2]$$

$$E(x^2) = \int_{-s/2}^{s/2} x^2 f(x) dx = \frac{1}{s} \int_{-s/2}^{s/2} x^2 dx = \frac{1}{s} \left[\frac{x^3}{3} \right]_{-s/2}^{s/2}$$

$$= \frac{s^2}{12}$$

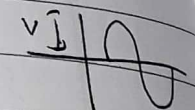
Quantization error.

to make sure we have equal space.
 $R, R/2$

D/A \leftrightarrow A/D

$$N = \frac{s^2}{12}$$

$$E = \frac{V^2}{2} \text{ (Energy of signal)}$$



$$\text{SNR (Signal to noise ratio)} = 10 \log_{10} \left(\frac{E}{N} \right)$$

$$= 10 \log_{10} \left(\frac{V^2}{2} \frac{12}{s^2} \right)$$

$$= 10 \log_{10} \left(\frac{6}{4} \frac{V^2}{s^2} (2^{2n}) \right) = k + 20n \log 2 = k + 6n \text{ dB}$$

$s = \frac{2V}{2^n}$ (2V divided in 2^n levels of equal size where n) is n-bit decoder

Assump. \rightarrow uniform distribution of levels. signal is pure sin.

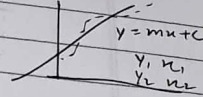
Noise is coming by quantization error.

$$\text{Error} = \frac{1}{n} \sum (Y - Y_i)^2$$

minimize this.

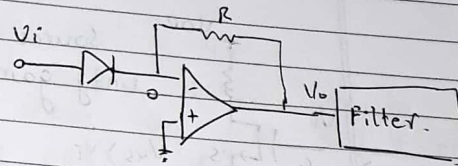
We take the variance, as we don't care about the sign of error.

every bit we increase, we get an improvement of b.d.B.



$$i = I_0 e^{V_i / n k T}$$

$$= - \frac{V_0}{R}$$

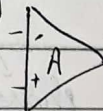
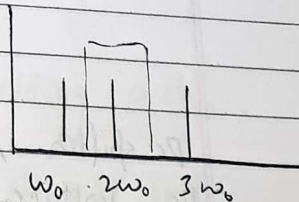


$$V_0 = - I_0 R e^{V_i / n k T}$$

$$= - I_0 R \left[1 + \frac{V_i}{n k T} + \frac{V_i^2}{2 n^2 k^2 T^2} + \dots \right]$$

$$V_i = V_m \sin \omega t$$

How to introduce a phase shift.



If assume gain to be A, still get $V_o \approx f(A, R, I_0)$

$A \rightarrow \infty$ gives same result.

भारतीय प्रौद्योगिकी संस्थान
INDIAN INSTITUTE OF TECHNOLOGY

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शाखा/प्रभाग/Branch/Div.

शिक्षण देव

प्र.सं./Q. No.

आरंभिक पृष्ठ
Starting Page No.

अंक/Marks

परीक्षा में बैठने वाले अभ्यर्थियों को निम्नलिखित बातें ध्यान में रखनी होंगी:

1. परीक्षा के पहले दो घंटे की अवधि मिलेगी। दो घंटे के बाद यदि लिखना पड़ती है तो वह पर्यवेक्षक की आज्ञा की अवधि में वह प्रश्न पत्र और उत्तर लिखेंगे।
2. हर अभ्यर्थी उनके लिए विशेष पर्यवेक्षक के सूचनानुसार वह परीक्षा केंद्र पर उपस्थित होंगे।
3. अभ्यर्थी उत्तर पुस्तिका की ओर ध्यान दें।
4. अभ्यर्थी इस उत्तर पुस्तिका में अन्य विवरण लिखेंगे। उत्तर लिखेंगे।

अंतिम 10 मिनट की अवधि में उत्तर लिखेंगे।

6. अभ्यर्थी के उपयोग में किसी भी पुस्तक, सलाह दी जाती है कि टिप्पणी अथवा पुस्तक रखें।

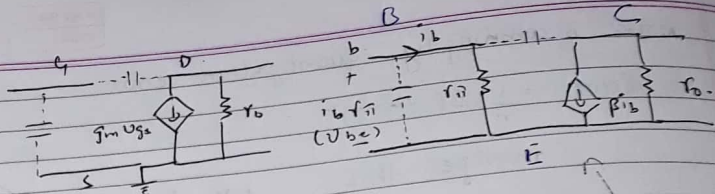
7. अभ्यर्थी इस पुस्तिका का कच्चा उपयोग न करें।

8. अभ्यर्थी इस पुस्तिका में कोई भी टिप्पणी न लिखें।

9. परीक्षा चलते-चलते या सम्प्रेषण न करें।

10. खुली पुस्तक साइक्लोस्टेन क्लास नोटाई इंग्लिश उप

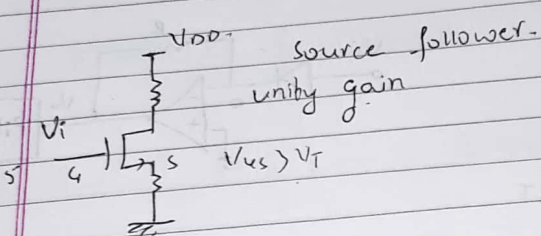
11. पर्यवेक्षक



$$\beta = g_m r_{\pi}$$

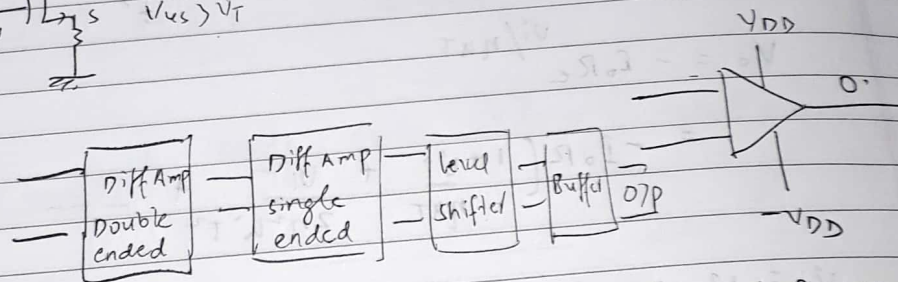
$$\beta i_b = g_m V_{be}$$

depletion capacitance
diffusion capacitance



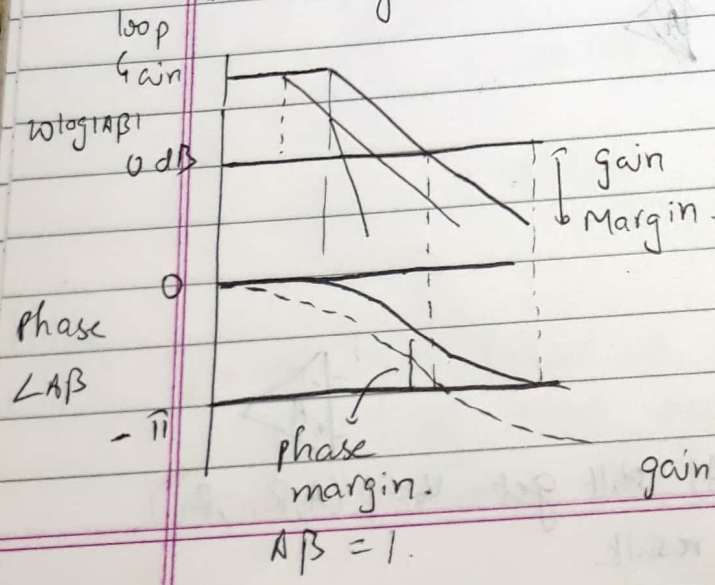
source follower.
unity gain

DC shift also, V_{th} more



if input 0, we expect output to be 0. if bipolar.

DC shifter, can make DC voltage 0 at the output.



$$\frac{1 - j\omega RC}{1 + j\omega RC}$$

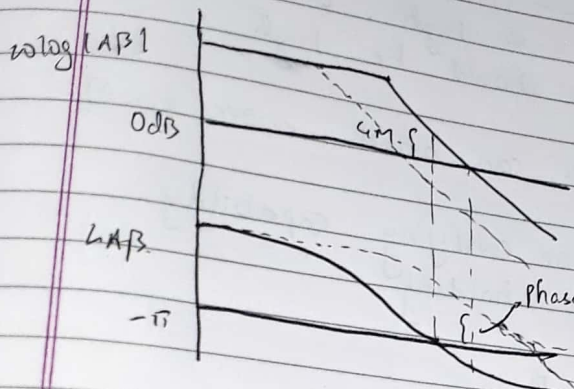
All pass filter with phase shift.

gain 1, phase should be π .

GIC. generalized Impedance converter

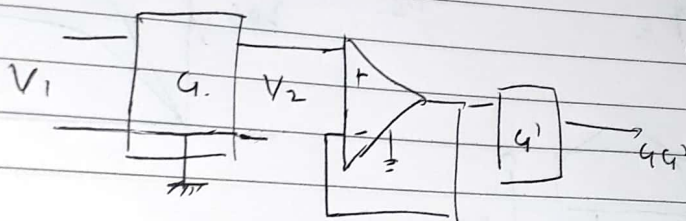
$$\frac{Z}{(s+a)}$$

$$Z_{11} = \frac{Z_1 Z_3 Z_5}{Z_2 Z_4}$$



This is not stable, chances of oscillation. at $-180^\circ, |A\beta| > 1$

add a transfer func, to reduce the gain, but it will also add a phase shift



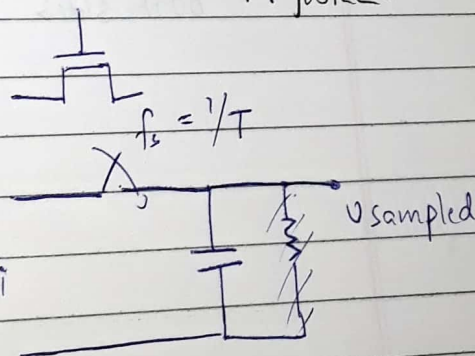
add a pole earlier to it.

Can change the phase plots by adding a shift, all pass filter, mag. plot doesn't change.

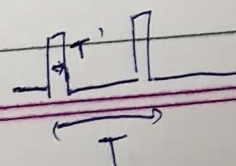
{ Gain Comp
Pole Comp

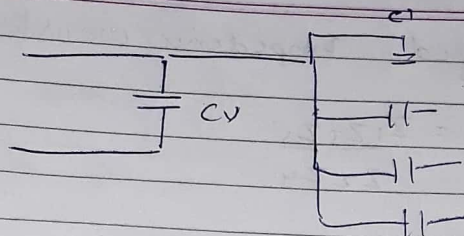
$$G' = \frac{1 - j\omega RC}{1 + j\omega RC}$$

Can't keep t' small, as then associated energy with particular sample is very low can't drive next circuit.



Can't be large, as value is



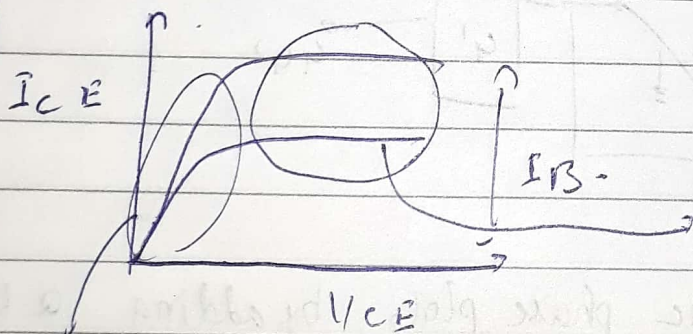
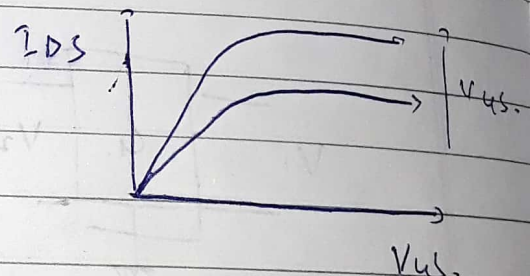
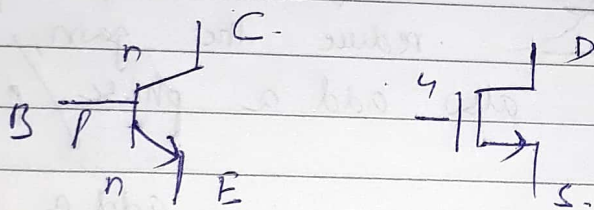


fan out max. no. of inputs connected to output of another circuit

We want C_V high, $\therefore C$ high. C_L high, takes time to charge. $\therefore \tau$ should be high.

C' should be ~~high~~ low, \therefore can attach more no. of ~~out~~ inputs.

limit on fan in \rightarrow current carrying capability.
" " " " out \rightarrow charge holding "



Active Region.

Saturation Region.

Region - , Base is saturated with charge, both sides