

Lecture 5

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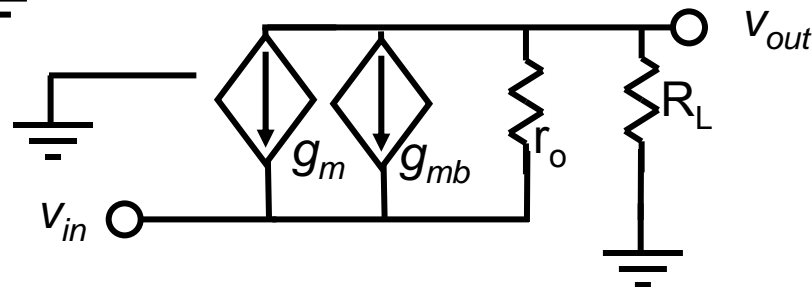
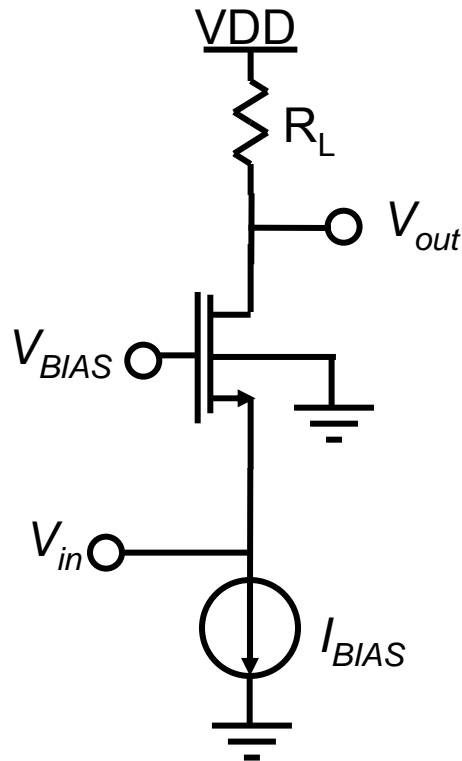
Common Gate Amplifier

- Large signal (bias)

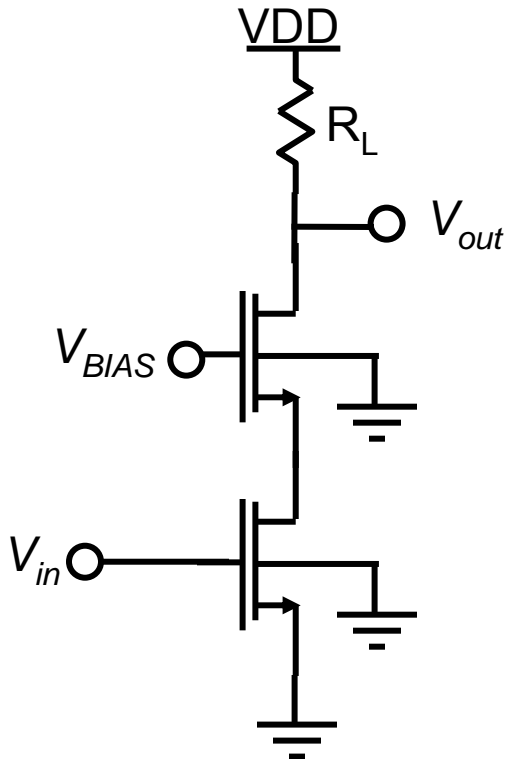
- $V_{out} = VDD - R_L I_{BIAS}$
- $V_{in} = V_{BIAS} - V_{GS} = V_{BIAS} - V_{TH} - (2I_D L)^{1/2} / (W \mu c_{ox})^{1/2}$
- For saturation, $V_{BIAS} < VDD - R_L I_{BIAS} + V_{TH}$

- Small signal

- Gain: $\frac{V_{out}}{V_{in}} = \frac{(g_m + g_{mb})r_o R_L + R_L}{r_o + R_L} \approx g_m (r_o \parallel R_L)$
- Zout: $\frac{V_{out}}{I_{out}} = (r_o \parallel R_L)$
- Zin: $\frac{V_{in}}{I_{in}} = \frac{1}{g_m + g_{mb} + \frac{1}{r_o} - g_m \frac{r_o \parallel R_L}{r_o}} \approx \frac{1}{g_m}$

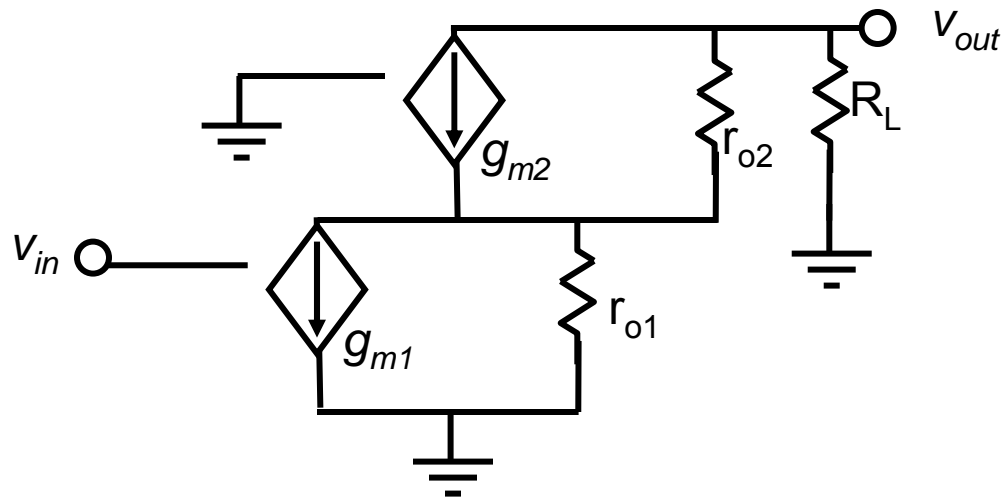


Cascode amplifier



- Large signal (bias)

- $I_{D1} = I_{D2} = W_1/L_1 \mu c_{ox} / 2 (V_{in} - V_{TH})^2$
- $V_{out} = V_{DD} - R_L I_{D2}$
- For M_2 saturation, $V_{BIAS} < V_{DD} - R_L I_{D2} + V_{TH}$
- For M_1 saturation, $V_{BIAS} > V_{TH} + V_{OD1} + V_{OD2}$



Cascode amplifier

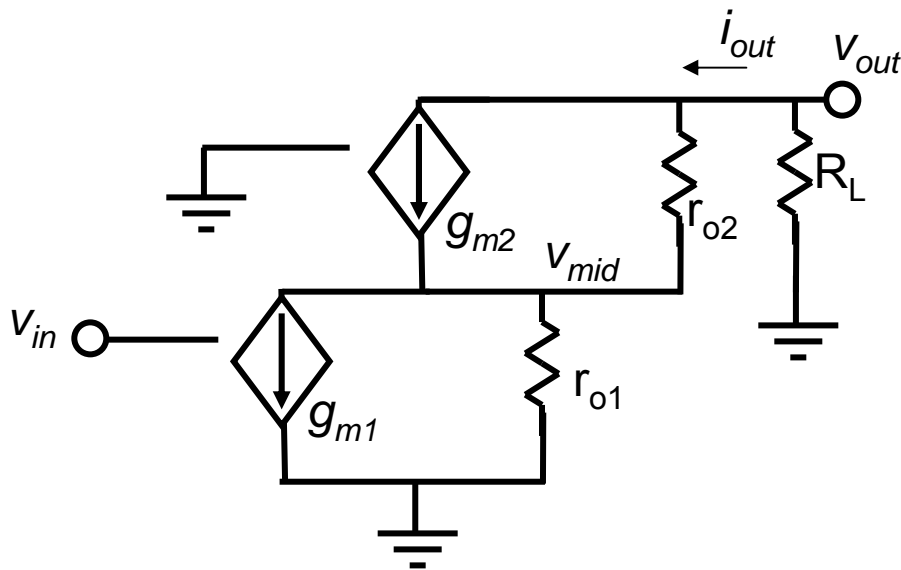
- Want to find equivalent g_m' , r_{out} for combined circuit
- $G_m' = i_{out}/v_{in}$ for $R_L = 0$

– KCL for v_{mid} :

$$0 = v_{in} g_{m1} + \frac{v_{mid}}{r_{o1}} + \frac{v_{mid}}{r_{o2}} + v_{mid} g_{m2}$$

$$i_{out} = \frac{v_{mid}}{r_{o2}} + v_{mid} g_{m2} = v_{in} \frac{g_{m1} r_{o1} (1 + g_{m2} r_{o2})}{g_{m2} r_{o1} r_{o2} + r_{o1} + r_{o2}}$$

$$g_m = \frac{g_{m1} r_{o1} r_{o2} (1 + g_{m2} r_{o2})}{g_{m2} r_{o1} r_{o2}^2 + r_{o1} r_{o2} + r_{o2}^2} \approx g_{m1}$$



- $r_{out} = i_{out}/v_{out}$ for $v_{in} = 0$

– KCL for v_{mid} :

$$0 = \frac{v_{mid}}{r_{o1}} + \frac{v_{mid} - v_{out}}{r_{o2}} + v_{mid} g_{m2}$$

$$I_{out} = \frac{v_{mid} - v_{out}}{r_{o2}} + v_{mid} g_{m2} = v_{out} \left(\frac{r_{o1} (1 + g_{m2} r_{o2})}{g_{m2} r_{o1} r_{o2}^2 + r_{o1} r_{o2} + r_{o2}^2} - \frac{1}{r_{o2}} \right)$$

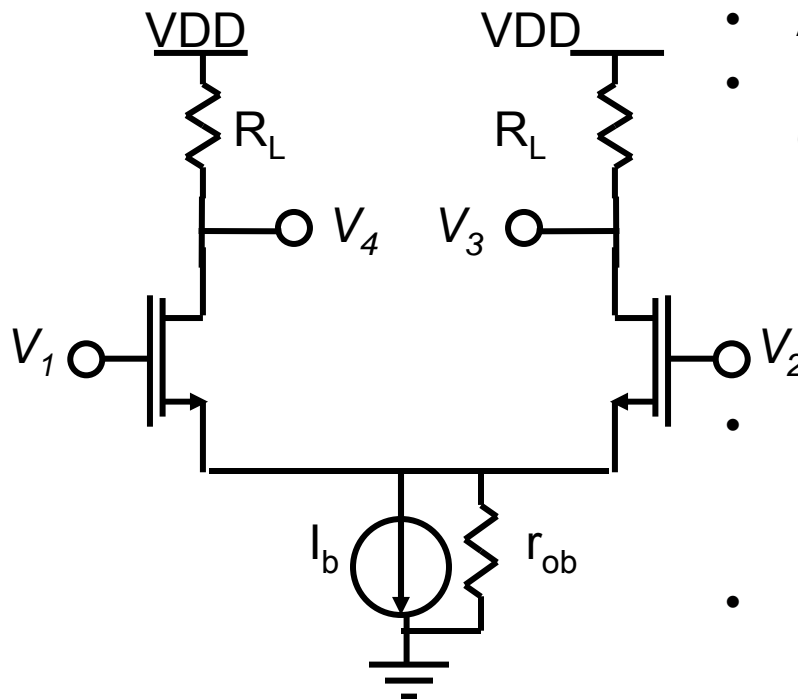
$$= v_{out} \left(\frac{r_{o1} (1 + g_{m2} r_{o2}) - (g_{m2} r_{o1} r_{o2} + r_{o1} + r_{o2})}{g_{m2} r_{o1} r_{o2}^2 + r_{o1} r_{o2} + r_{o2}^2} \right) = v_{out} \left(\frac{1}{g_{m2} r_{o1} r_{o2} + r_{o1} + r_{o2}} \right)$$

$$r_{out} = \frac{v_{out}}{i_{out}} = g_{m2} r_{o1} r_{o2} + r_{o1} + r_{o2} \approx g_{m2} r_{o1} r_{o2}$$

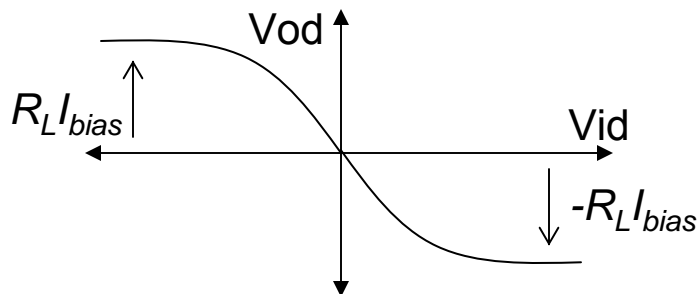
So, gain = $-g_m(r_{out} || R_L) \sim -g_{m1}((g_{m2} r_{o1} r_{o2}) || R_L)$

Max gain = $-g_m r_{out} \sim -g_{m1} g_{m2} r_{o1} r_{o2}$

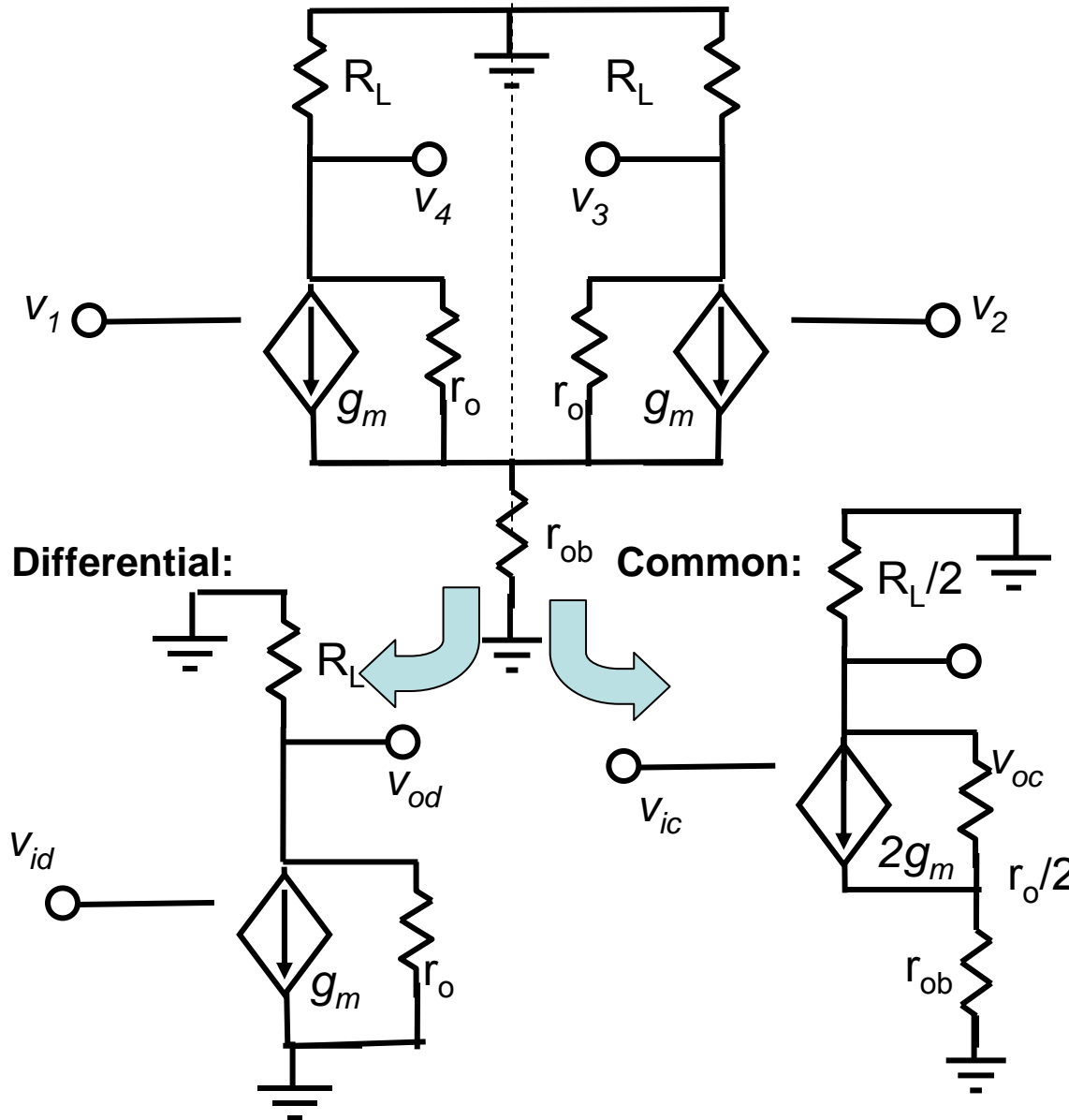
Differential pairs



- Assume the transistors are identical.
- Redefine inputs, outputs as differential, common mode:
 - $V_{id} = V_1 - V_2$
 - $V_{ic} = (V_1 + V_2)/2$
 - $V_{od} = V_4 - V_3$
 - $V_{oc} = (V_4 + V_3)/2$
- Can also do this for drain currents:
 - $I_{dd} = I_{d1} - I_{d2}$
 - $I_{dc} = (I_{d1} + I_{d2})/2 = I_{bias}/2$
- Implies output common mode ~ constant:
 - $V_{oc} = V_{DD} - R_L I_{bias}/2$
- To find V_{od} , solve for V_C too
 - $I_b = W/L\mu c_{ox}[(V_1 - V_C - V_{TH})^2 + (V_2 - V_C - V_{TH})^2]$
 - $V_{od} = R_L \cdot W/L\mu c_{ox}[(V_1 - V_C - V_{TH})^2 - (V_2 - V_C - V_{TH})^2]$

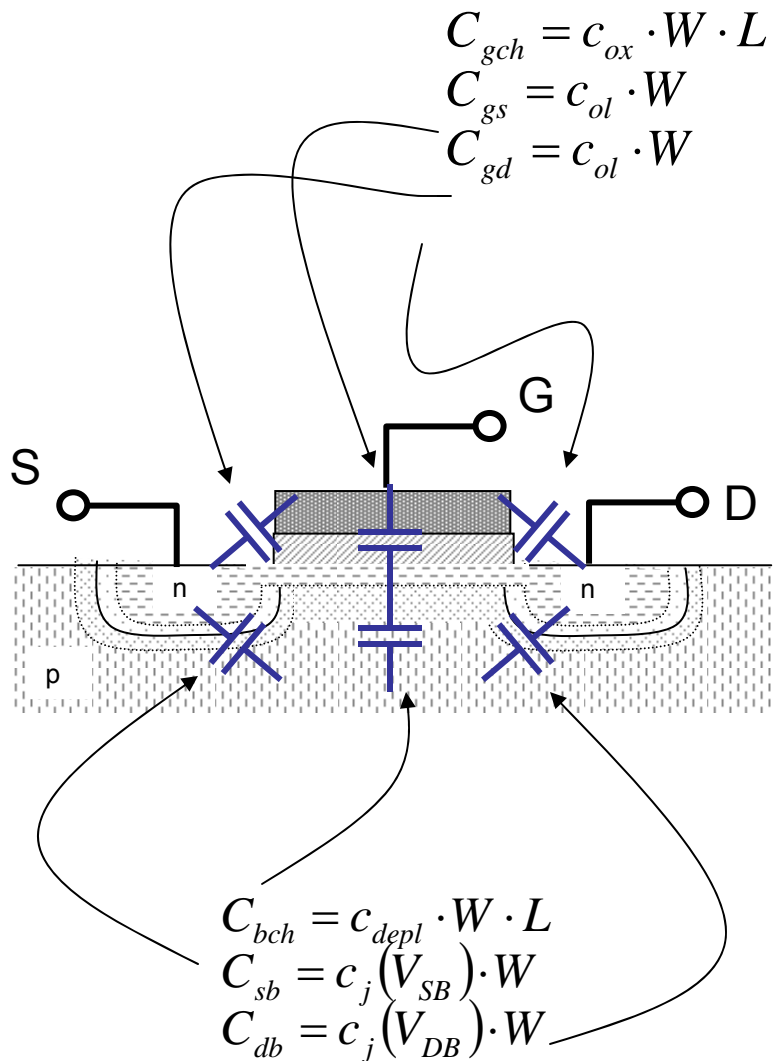


Small-Signal, Diff Pair



- Again define in terms of differential, common mode:
 - $v_{id} = V_1 - V_2$
 - $v_{ic} = (V_1 + V_2)/2$
 - $v_{od} = V_4 - V_3$
 - $v_{oc} = (V_4 + V_3)/2$
- Use half circuit analysis:
- Common mode, combine both sides in parallel
 - $v_{cs} \sim v_{ic}$ (if $2g_m \gg 1/r_{ob}$)
 - $i_b \sim v_{ic}/r_{ob}$, $v_{oc} = i_b R_L/2$
 - Gain: $A_c = v_{oc}/v_{ic} = R_L/2r_{ob}$
- Differential mode, insert “virtual grounds” at symmetry points
 - $A_d = v_{od}/v_{id} = (-g_m(R_L || r_o))$
 - Differential mode just like a common-source amp!
- Common mode rejection:
 - $A_d/A_c \sim gm/2r_{ob}$

Accounting for device capacitance



- Expect capacitance across oxide
 - from gate to channel:
 - to source
 - and to drain
- Expect depletion capacitance:
 - from bulk to channel,
 - to source
 - and to drain
- Where, c_{ox} is the unit oxide cap
 - $c_{ox} = 4\text{fF}/\mu\text{m}^2$ - $12\text{fF}/\mu\text{m}^2$
- c_{ol} is the overlap capacitance
 - $c_{ol} \sim 0.2\text{fF}/\mu\text{m}$
- c_{depl} is the unit depletion cap
 - $c_{depl} \sim c_{ox}/5$ (when in inversion)
- c_j is the reversed-biased junction cap
 - $c_j(V) \sim 0.3\text{fF}/(1+V/0.7)^{1/2}$

Complete small signal model

- Want to eliminate channel node:
 - Generally neglect c_{depl} unless in cut-off

- In triode ($V_{\text{DS}} = 0$)
 - Split C_{gch} between source, drain

$$C_{gs} = C_{ol} \cdot W + C_{ox} \cdot W \cdot L/2$$

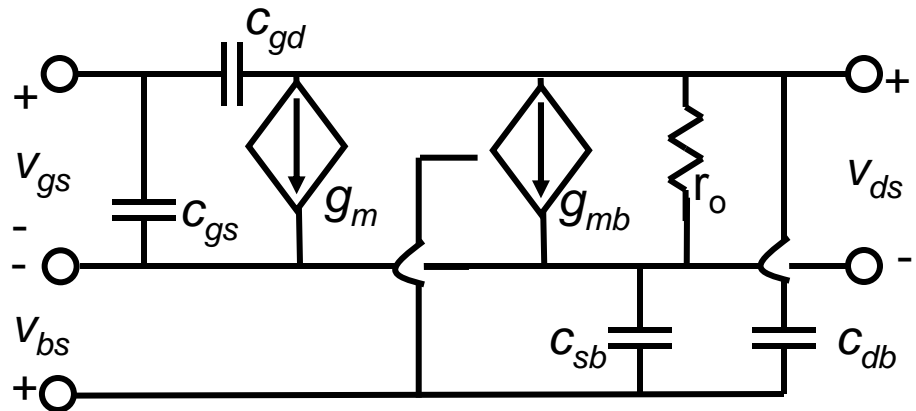
$$C_{gd} = C_{ol} \cdot W + C_{ox} \cdot W \cdot L/2$$

- In saturation
 - channel tied only to source,
 - but close to pinch off $V_{\text{Gch}} \rightarrow V_{\text{TH}}$ regardless of V_{GS}
 - So get partial coupling to source:

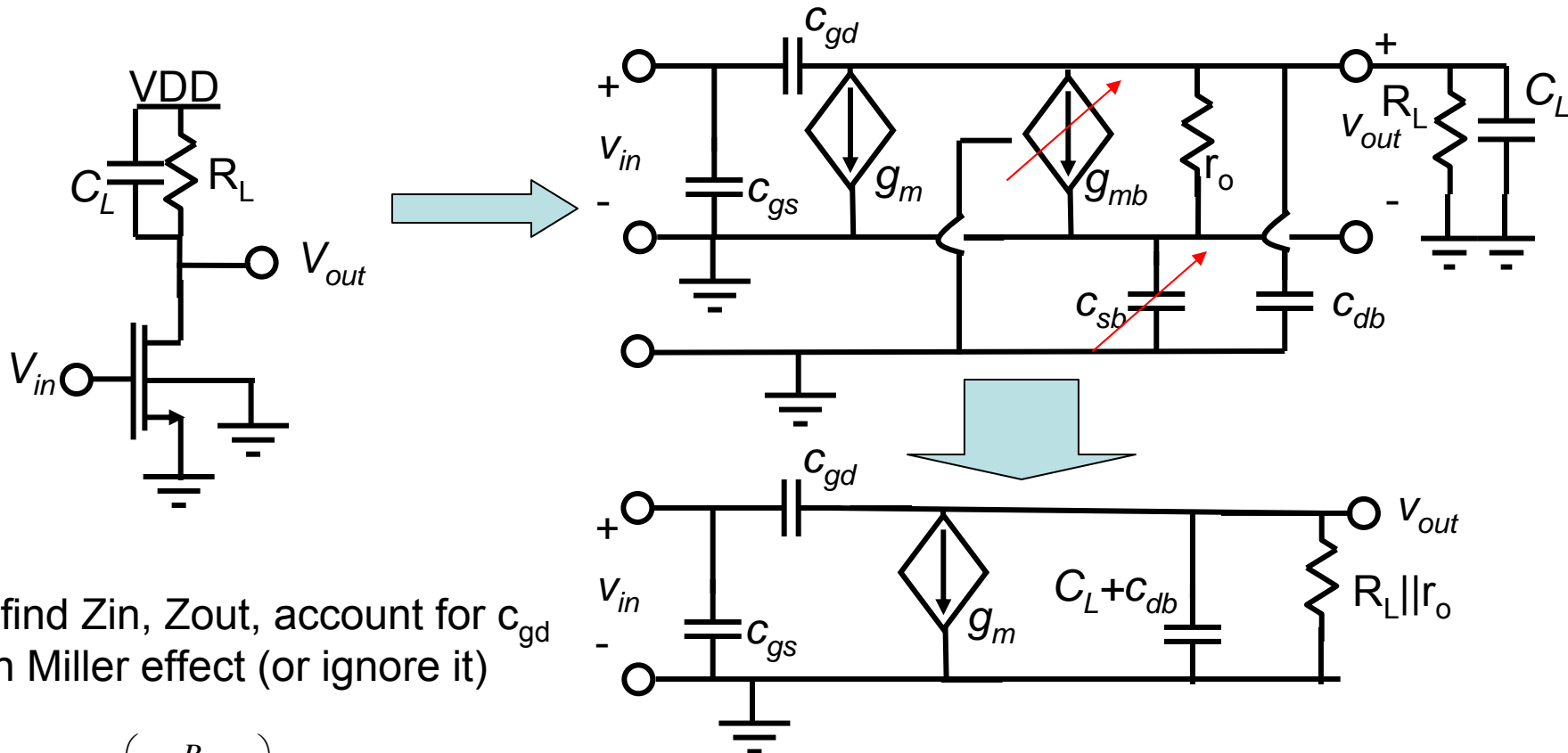
$$C_{gs} = C_{ol} \cdot W + C_{ox} \cdot W \cdot L \cdot 2/3$$

$$C_{gd} = C_{ol} \cdot W$$

- So get complete small signal model:



C.S. example



To find Z_{in} , Z_{out} , account for c_{gd} with Miller effect (or ignore it)

$$A \approx \frac{-g_m \left(\frac{R_L}{1 + g_{ds} R_L} \right)}{1 + j\omega (c_{db} + c_{gd}) \left(\frac{R_L}{1 + g_{ds} R_L} \right)}$$

$$\approx \frac{-g_m R_L}{1 + g_{ds} R_L + j\omega (c_{db} + c_{gd}) R_L}$$

$$Z_{in} = \frac{1}{j\omega (c_{gs} + (1 - A) c_{gd})}$$

$$\approx \frac{1}{j\omega (c_{gs} + (1 + g_m R_L) c_{gd})}$$

$$Z_{out} = \frac{\left(\frac{R_L}{1 + g_{ds} R_L} \right)}{1 + j\omega \left(c_{db} + \left(\frac{1 - A}{-A} \right) c_{gd} \right) \left(\frac{R_L}{1 + g_{ds} R_L} \right)}$$

$$\approx \frac{R_L}{1 + g_{ds} R_L + j\omega (c_{db} + c_{gd}) R_L}$$