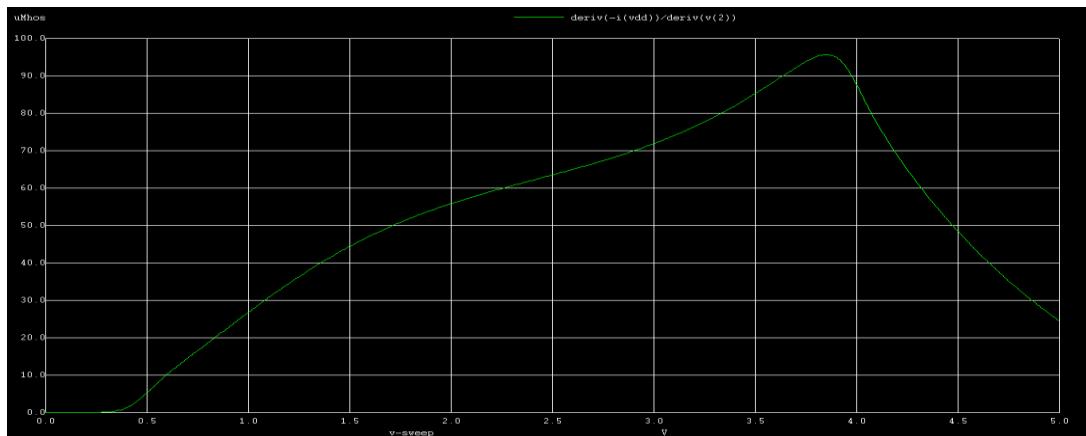


1.

a),b)

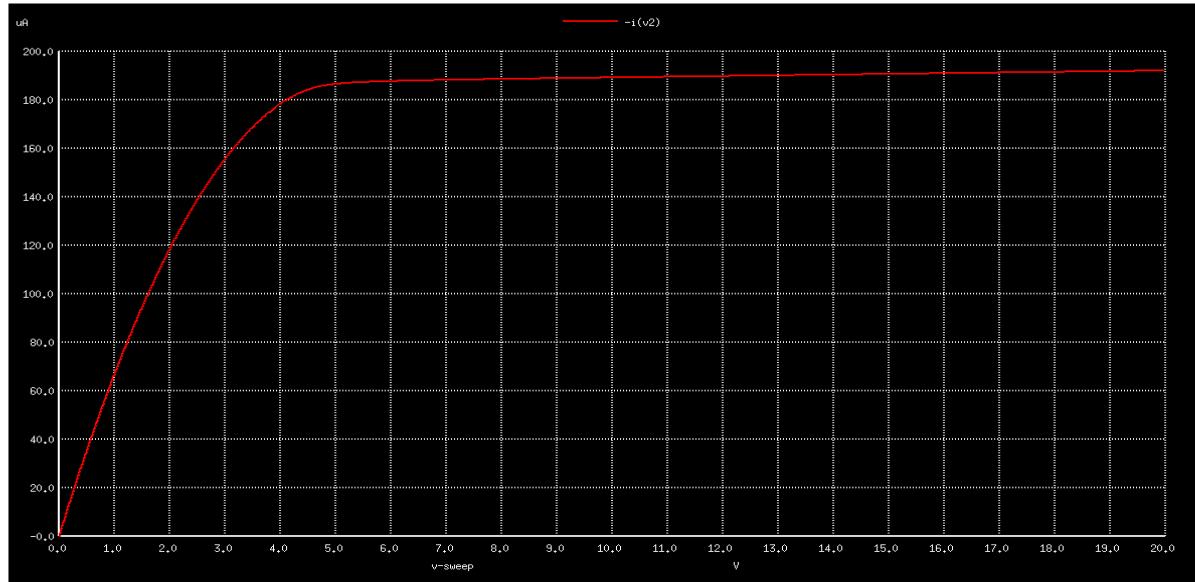
```
1 .include NMOS.txt
2 M1 3 2 0 0 CMOSN W=1u
3 R1 2 1 470
4 VDD 3 0 DC 5v
5 VIN 1 0 DC 0v
6 .dc VIN 0 5 0.01
7 .control
8 run
9 plot -i(VDD)
10 plot deriv(-i(VDD))/deriv(v(2))
11 .endc
12 .end
```



The peak transconductance for the MOSFET at $V_{ds} \approx 5$ V was found to be $95.66 \mu\text{S}$ and corresponding V_{gs} was 3.85V .

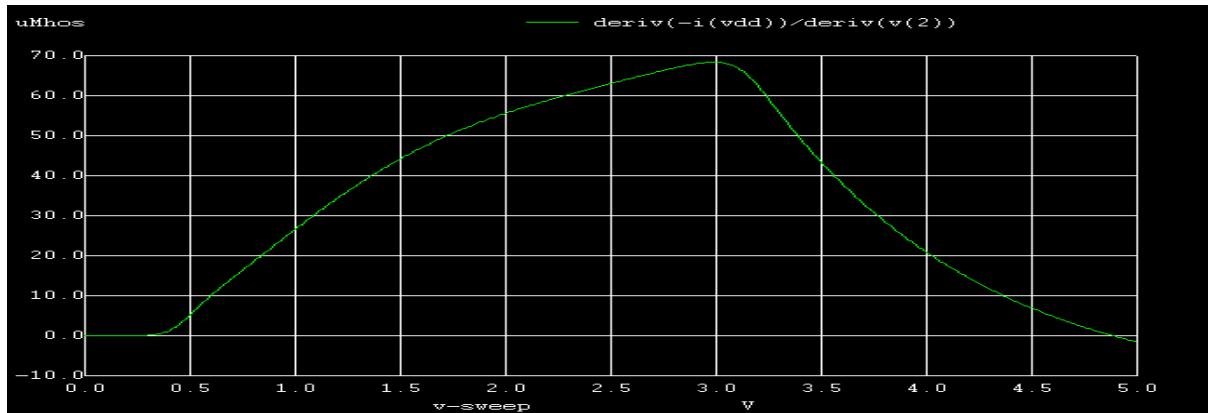
c)

```
.include sim.txt
M1 3 2 0 0 CMOSN w=1u
V1 2 0 DC 3.85v
V2 3 0 DC 5v
.dc V2 0 20 0.01
.control
run
plot -i(V2)
.endc
.end
```

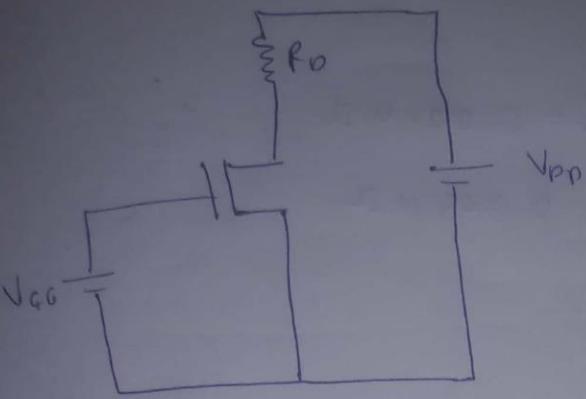


Output impedance @ $V_{gs}=3.85\text{V}$ and $V_{ds}=5\text{V}$: 345KOhm

d)



Peak transconductance for $V_{ds}=3\text{V}$ is observed to be 68.6047uMhos and output impedance is 34.1KOhm .

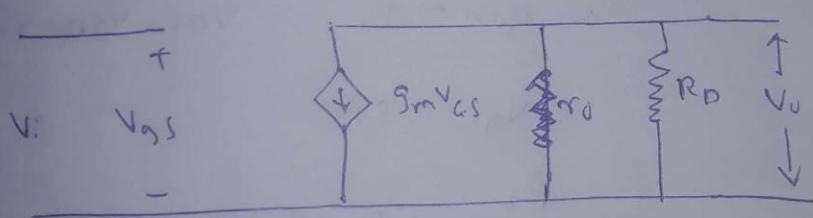


From Spice simulations

$$g_m = 95.66 \mu\Omega^{-1} \quad I_D = 0.186 \text{ mA}$$

$$r_o = 0.345 \text{ M}\Omega \quad V_{DS} = 3.85 \text{ V}$$

Small signal equivalent circuit



$$\text{Desired gain} = A_v = 2$$

$$g_m(r_o \parallel R_D) = 2$$

$$95.66 \mu\Omega^{-1} (r_o \parallel R_D) \text{ M}\Omega = 2$$

$$(r_o \parallel R_D) = 0.021$$

$$r_o \parallel R_D = 0.021 r_o + 0.021 R_D$$

$$(r_o - 0.021) R_D = 0.021 r_o$$

$$R_D = \frac{0.021 r_o}{r_o - 0.021}$$

$$R_D = 0.0223 \text{ M}\Omega$$

Output Impedance

i) with R_D $R_o = (r_d || R_D) = 0.021 \text{ M}\Omega$

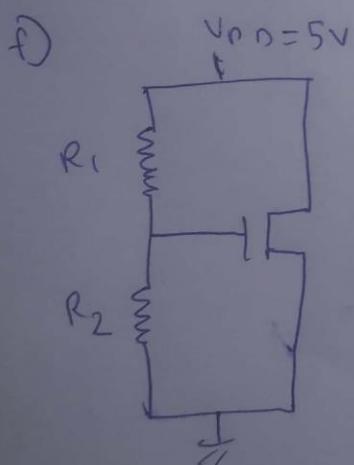
ii) without R_D $R_o = r_d = 0.345 \text{ M}\Omega$

Source Voltages

$$V_{CC} = V_{GS} = 3.85 \text{ V}$$

$$\begin{aligned} V_{DD} &= V_{OS} + I_D R_D \\ &= 5 + 0.186 \text{ mA} \times 0.0223 \text{ M}\Omega \end{aligned}$$

$$V_{DD} = 9.14 \text{ V}$$



For gain = 2

$$V_{OS} = V_{DD} = 5 \text{ V}$$

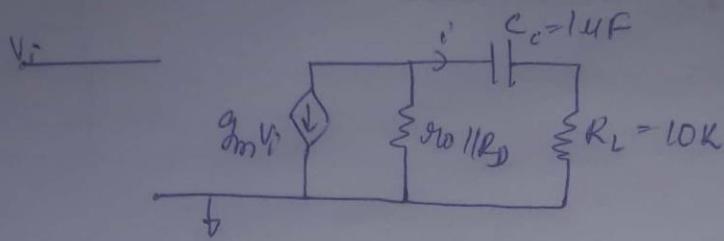
$$V_{GS} = 3.85 \text{ V}$$

$$\frac{R_2}{R_1 + R_2} \times 5 = 3.85$$

$$\text{let } R_2 = 10 \text{ k}$$

$$R_1 = 2.987 \text{ k}$$

g)



$$r_o || R_D = 345 \text{ k}\Omega || 22.3 \text{ k}\Omega = 21 \text{ k}\Omega$$

$$i = -g_m V_i \frac{r_o || R_D}{r_o || R_D + \frac{1}{C_L s} + R_L}$$

$$= -\frac{g_m V_i (r_o || R_D) C_L s}{1 + (r_o || R_D + R_L) C_L s}$$

$$V_o = i R_L$$

$$A_V = -\frac{g_m R_L (r_o || R_D) C_L s}{1 + (r_o || R_D + R_L) C_L s}$$

$$= -\frac{95.66 \mu \times 21 \text{ k} \times 10 \text{ k} \times 1 \mu \cdot \text{s}}{1 + (31 \text{ k}) 1 \mu \cdot \text{s}}$$

$$= -\frac{2.00886 \times 10^{-2} \text{ s}}{1 + 0.031 \text{ s}}$$

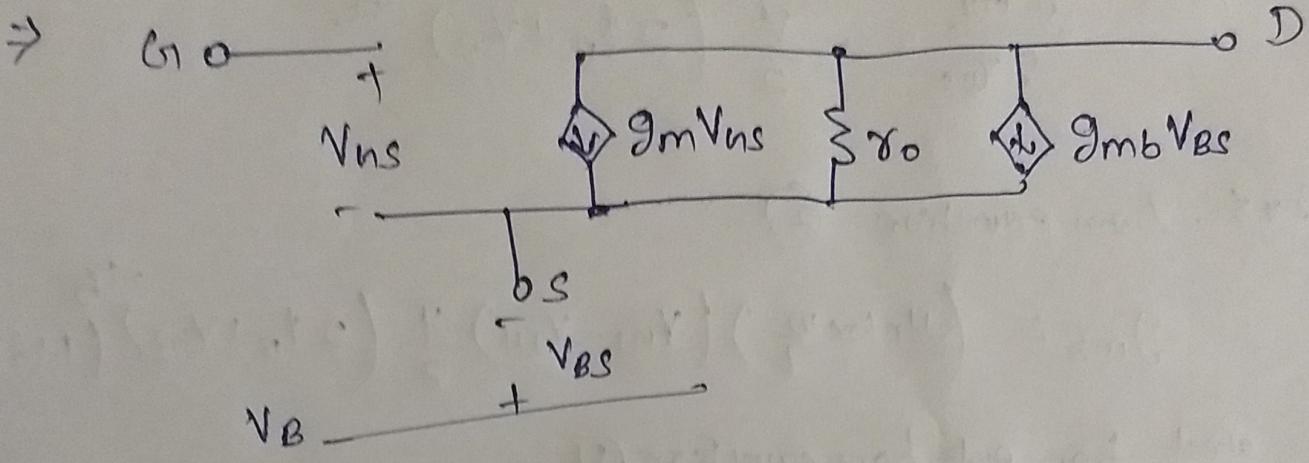
$$|A_V| @ 1 \text{ MHz} = \frac{2.00886 \times 10^{-2} \times 10^6 \times 2\pi}{\sqrt{1 + (0.031 \times 2\pi \times 10^6)^2}} \\ = 64.8019 \times 10^{-2} = 0.648019$$

$$|A_V| @ 1 \text{ mHz} = 2.00886 \times 10^{-2} \times 2\pi \times 10^{-3} \\ = 1.2622 \times 10^{-4}$$

when $V_{BS} \neq 0$ then

Small signal equivalent circuit is given below at current

$$I_{DS} = \frac{1}{2} \mu n \text{lo} \times \frac{W}{L} (V_{DS} - V_{TH})^2 (1 + dV_{DS}) \quad \text{--- (1)}$$



$$\Rightarrow \text{where } r_o = \left(\frac{\partial I_D}{\partial V_{DS}} \right)^{-1} = \frac{1}{\frac{1}{2} \mu n \text{lo} \times \frac{W}{L} (V_{DS} - V_{TH})^2} \approx \boxed{r_o \approx \frac{1}{d I_D}}$$

and

$$g_m = \left. \frac{\partial I_D}{\partial V_{DS}} \right|_{V_{DS}=\text{constant}}$$

(transconductance)

$$g_m = \mu n \text{lo} \times \frac{W}{L} (V_{DS} - V_{TH}) (1 + dV_{DS}) \quad \text{(from equation (1))}$$

and

$$g_{mb} = \left. \frac{\partial I_D}{\partial V_{BS}} \right|_{V_{DS}=\text{constant}} = \mu n \text{lo} \times \frac{W}{L} (V_{DS} - V_{TH}) \left(-\frac{\partial V_{TH}}{\partial V_{BS}} \right) (1 + dV_{DS})$$

\Rightarrow Also given $V_{TH} = V_{TO} + \gamma (\int \beta \phi_B + V_{SB}) - \int 2\phi_B$

--- (2)

$$\text{then } \frac{\partial V_{TH}}{\partial V_{SB}} = \frac{Y}{2} (2\phi_B + V_{SB})^{-Y/2}$$

We can write $\frac{\partial V_{TH}}{\partial V_{SB}} = - \frac{\partial V_{TH}}{\partial V_{BS}}$

Hence $\frac{\partial V_{TH}}{\partial V_{BS}} = - \frac{Y}{2} (2\phi_B + V_{SB})^{-Y/2}$

thus, from equation ②

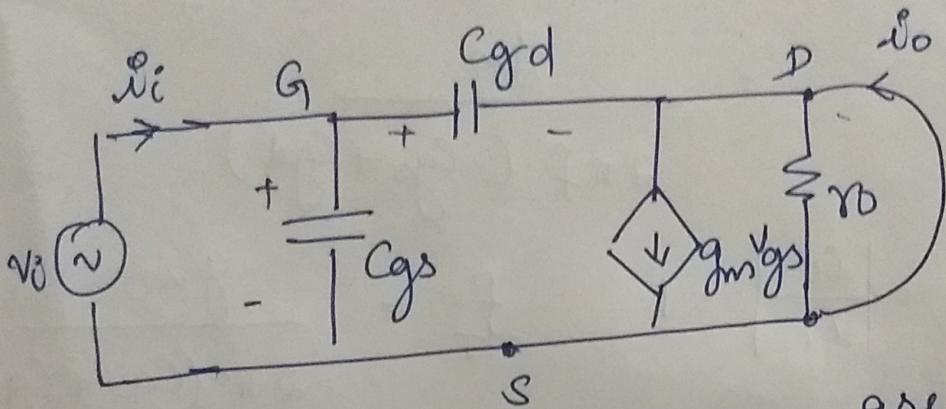
$$g_{mb} = \left(\mu_n \cos \frac{\pi}{L} \right) (V_{BS} - V_{TH}) \frac{Y}{2} (2\phi_B + V_{SB})^{-Y/2} (1 + \delta V_{BS})$$

~~and also from equation ①~~

and from equation of $g_m = \mu_n \cos \frac{\pi}{L} (V_{BS} - V_{TH})(1 + \delta V_{BS})$

Hence
$$g_{mb} = \boxed{g_m \cdot \frac{Y}{2 \sqrt{2\phi_B + V_{SB}}}}$$

3. The small signal equivalent model of MOSFET when o/p terminal is shorted to ground is shown below



Since drain and source are shorted

$$v_{gd} = v_{gs} = v_o$$

\therefore The input current

$$i_i^o = j\omega(C_{gs} + C_{gd})v_{gs}$$

The output current

$$i_o^o = g_m v_{gs} - j\omega C_{gd} v_{gs}$$

The short circuit current gain

$$\frac{i_o^o}{i_i^o} = \frac{g_m - j\omega C_{gd}}{j\omega(C_{gs} + C_{gd})}$$

Since C_{gd} is very small

$$\approx \frac{g_m}{j\omega(C_{gs} + C_{gd})}$$

$$\left| \frac{v_o}{i_i} \right| = \frac{g_m}{\omega (C_{gs} + C_{gd})}$$

$$= \frac{g_m}{2\pi f (C_{gs} + C_{gd})}$$

When $\left| \frac{v_o}{i_i} \right| = 1$ $f_T = \frac{g_m}{2\pi (C_{gs} + C_{gd})}$.

when $C_{gs} = 1 \text{ nF}$ & $C_{gd} = 0$

$$f_{T1} = \frac{g_m}{2\pi C_{gs}} = \frac{g_m}{2\pi} \times 6 \text{ Hz}$$

$$= 15.2247 \text{ kHz}$$

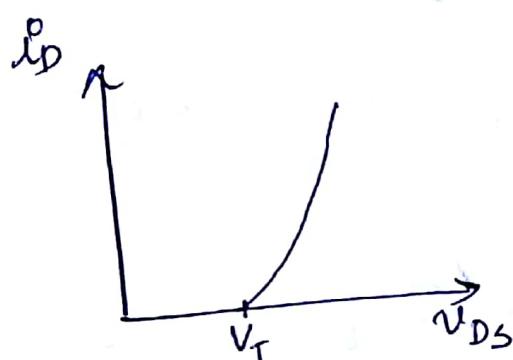
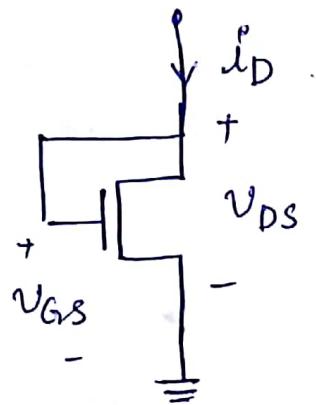
when $C_{gs} = 1 \text{ nF}$ & $C_{gd} = 0.2 \text{ nF}$

$$f_{T2} = \frac{g_m}{2\pi (C_{gs} + C_{gd})} = \frac{g_m}{2 \cdot 4\pi} \text{ Hz}$$

$$= 12.6873 \text{ kHz}$$

Q.4)

When the MOSFET has the gate connected to the drain, it acts like a diode with characteristics similar to a pn junction diode



$V_{GS} = V_{DS}$, MOSFET is in saturation

$$i_D = \frac{\mu_n C_{ox} W}{2L} (V_{GS} - V_T)^2$$

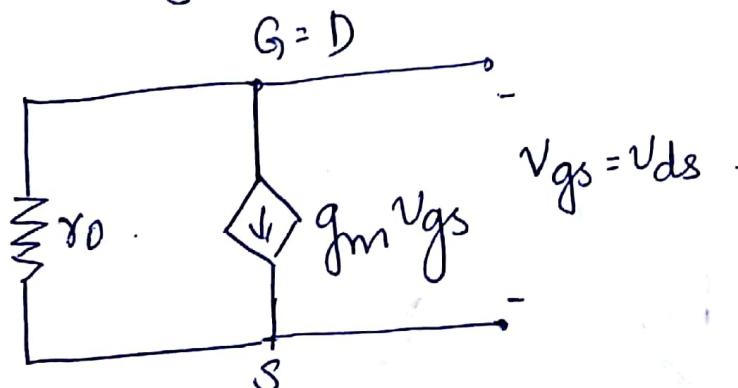
$$= \frac{\mu_n C_{ox} W}{2L} (V_{DS} - V_T)^2$$

$$= \frac{B}{2} (V_{DS} - V_T)^2$$

$$V_{DS} = V_{GS} = V_T + \sqrt{\frac{2 i_D}{B}}$$

$$\text{where } B = \mu_n C_{ox} \frac{W}{L}$$

The small signal equivalent circuit model (excluding capacitor & bulk and source are at same potential)



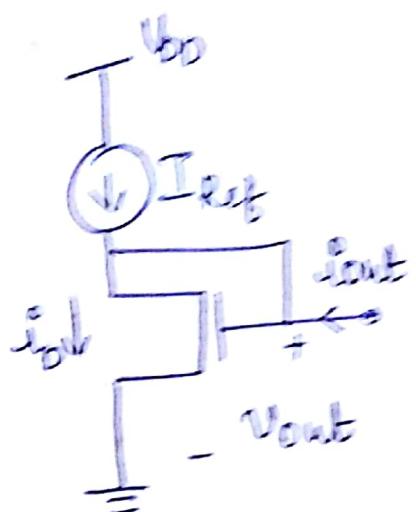
The output resistance

$$R_{out} = \frac{1}{g_m} \parallel r_o$$

$$\approx \frac{1}{g_m}$$

1. How to synthesize a voltage source with this

Assume a current source is available



$V_{GS} = V_{DS}$ take a value needed to mark the current-

$$i_D = i_{out} + I_{ref} = \frac{R}{2} (V_{out} - V_T)^2$$

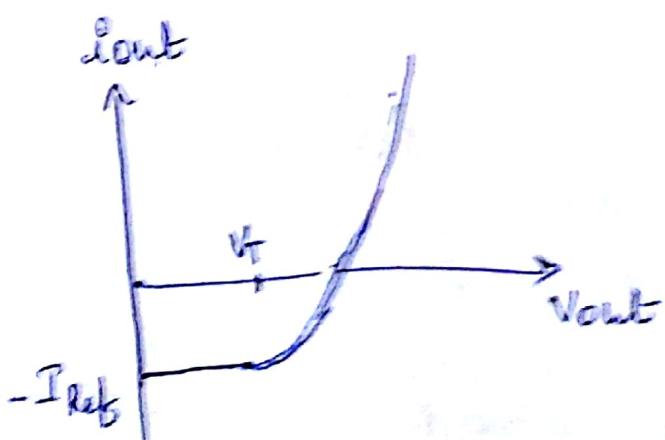
$$\therefore V_{out} = V_T + \sqrt{\frac{I_{ref} + i_{out}}{R/2}}$$

where $R = \mu n \frac{k_B T}{L}$

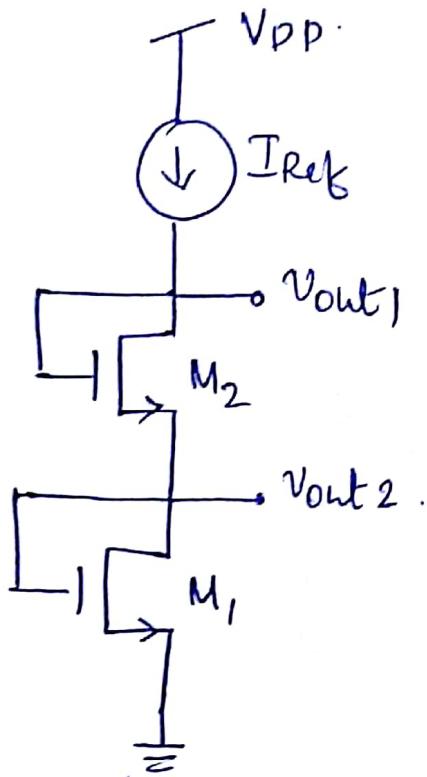
V_{out} is a function of I_{ref} & ω_L .

$I_{ref} \uparrow \Rightarrow V_{out} \uparrow$

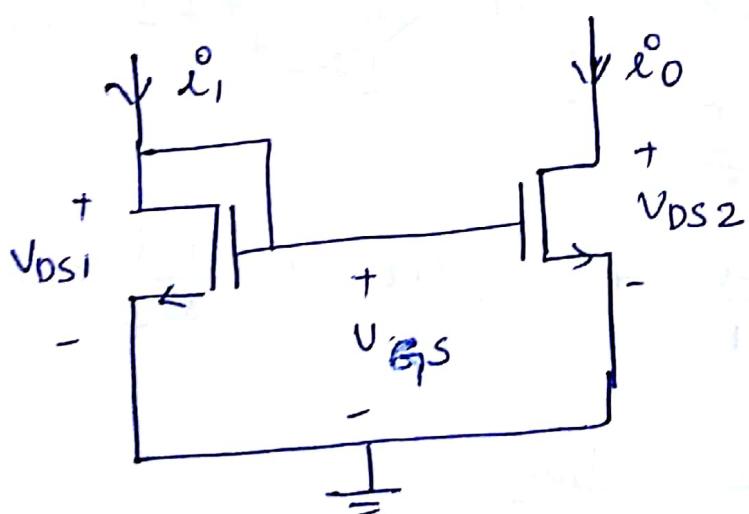
$\omega_L \uparrow \Rightarrow V_{out} \downarrow$



2. Voltage divider network using diode connected MOSFET (active resistor)

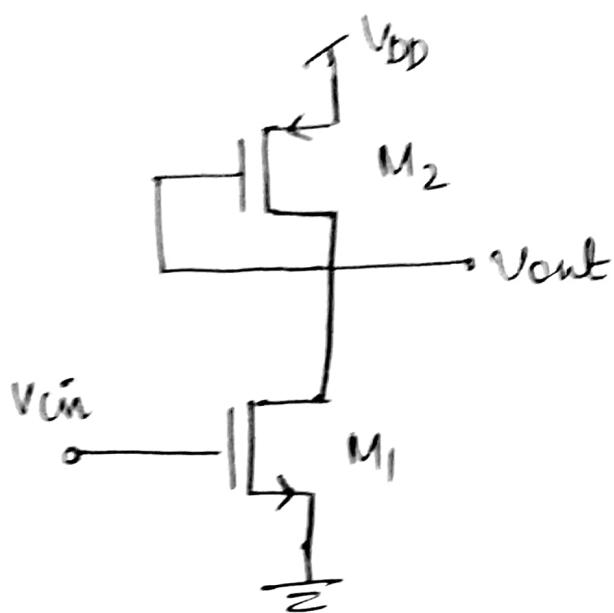


3. The MOS diode is used as a component of a current mirror



$$\frac{i_0^o}{i_1^o} = \frac{\beta_2}{\beta_1} \frac{(V_{GS} - V_{T1})^2}{(V_{GS} - V_{T2})^2} \frac{1 + \lambda V_{DS2}}{1 + \lambda V_{DS1}}$$

5. nmos inverter with active pmos load



$$\frac{V_{out}}{V_{in}} \approx -\frac{g_{m1}}{g_{m2}}$$

$$R_{out} \approx \frac{1}{g_{m2}}$$

Q5. For calculating Cgd..

Ngspice code:

*Compute unity current gain frequency

.include tsmc.txt

M1 2 1 0 0 CMOSN W=1u

RD 2 6 10k

VDD 6 5 DC 10v

VGG 1 0 DC 4.5V

V0 5 0 AC 0.01

*defining the run-time control functions

.AC DEC 20 1 1000Gig

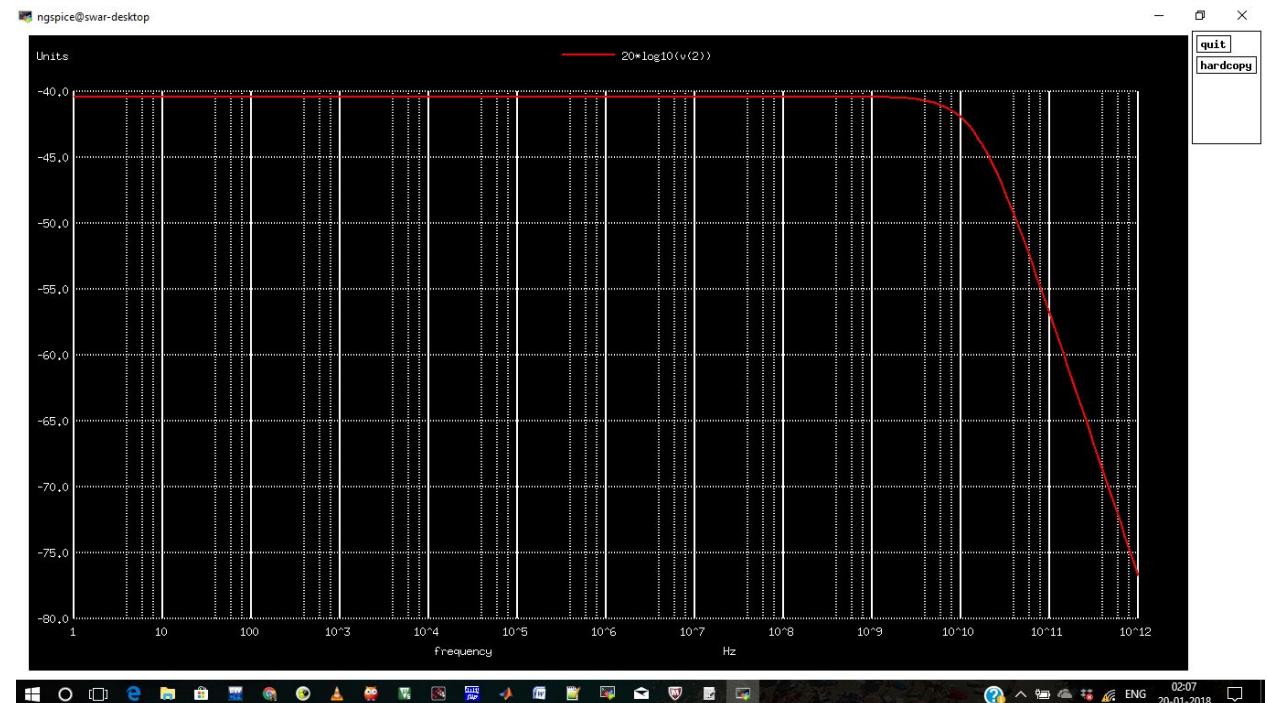
.control

run

plot 20*log10(V(2))

.endc

.en



$$f_T = \frac{1}{2\pi C_{gd} * R_d}$$

Here, f_T corresponds to the point where amplitude is 3dB below the highest.
From Figure above $f_T = 15.7 \text{ GHz}$
Putting $R_D = 10k\Omega$ we get $C_{gd} = 0.001\text{pF}$

For Calculating Cgs ..

*Compute unity current gain frequency

.include tsmc.txt

M1 2 1 0 0 CMOSN W=1u

RD 2 6 40k

VDD 6 0 DC 40v

VGG 1 3 DC 3.8V

*Vin 3 0 AC 0.01 sin(0 0.1 0.5Gig)

Vin 3 0 AC 0.01

C0 2 4 1

R0 4 5 0

V0 5 0 0

*defining the run-time control functions

.AC DEC 20 10Meg 1Gig

*.tran 0.005m 0.4m

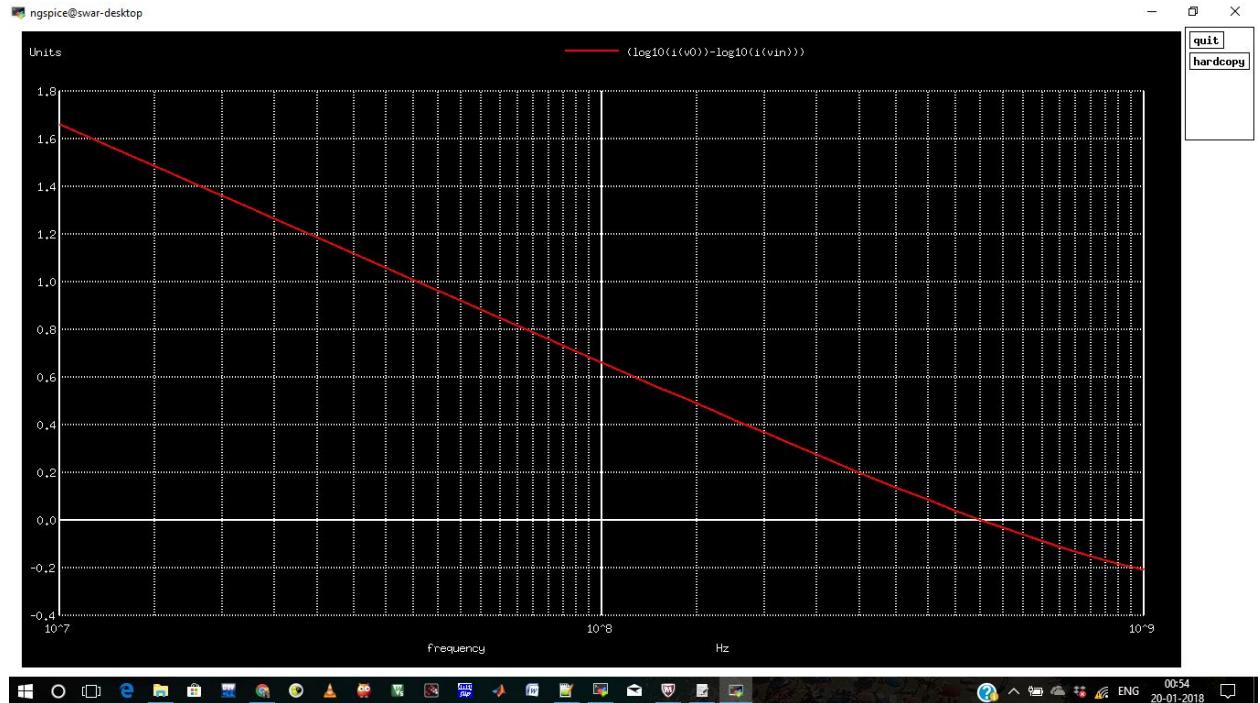
.control

run

plot (log10(I(V0))-log10(I(Vin)))

.endc

.end



$$f_T = \frac{g_m}{2\pi(C_{gs} + C_{gd})}$$

Here, f_T corresponds to the point where current gain is unity.

From Figure above $f_T = 0.49 \text{ GHz}$

Putting $g_m = 95.66 \mu S$ we get $C_{gs} = 0.031 pF - C_{gd} = 0.030 pF$