

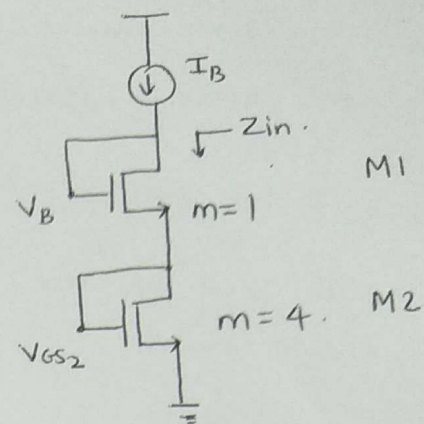
Q1.

$$Z_{in} = \frac{1}{g_{m1}} + \frac{1}{g_{m2}} \quad (1)$$

$$g_{m1} = \sqrt{2 \mu_n C_{ox} \frac{W}{L} I_B} = g_m \quad (0.5)$$

$$g_{m2} = \sqrt{2 \mu_n C_{ox} \frac{4W}{L} I_B} = 2g_m \quad (0.5)$$

$$Z_{in} = \frac{3}{2} \times \frac{1}{g_m} = \frac{1.5}{\sqrt{2 \mu_n C_{ox} \frac{W}{L} I_B}} \quad (0.5)$$



$$I_B = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS1} - V_T)^2 \Rightarrow V_{GS1} = \sqrt{\frac{2 I_B L}{\mu_n C_{ox} W}} + V_T \quad (0.5)$$

$$I_B = \frac{1}{2} \mu_n C_{ox} \frac{4W}{L} (V_{GS2} - V_T)^2 \Rightarrow V_{GS2} = \sqrt{\frac{2 I_B L}{\mu_n C_{ox} (4W)}} + V_T \quad (0.5)$$

$$V_B = V_{GS1} + V_{GS2} \quad (1)$$

$$= 2V_T + 1.5 \sqrt{\frac{2 I_B L}{\mu_n C_{ox} W}} \quad (0.5)$$

Q2.

For calculating $V_{ICM(max)}$;

if $V_G \uparrow \Rightarrow V_S \uparrow$

MB will be the first one to go to triode.

At the limit

$$V_S = V_{DD} - V_{dsatp}$$

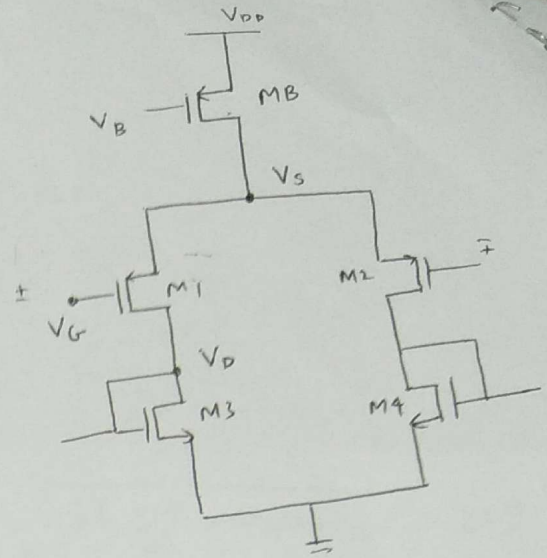
$$V_G = V_S - (V_{dsatp} + V_{Tp})$$

(To maintain current)

$$\therefore V_{ICM(max)} = (V_{DD} - V_{dsatp}) - (V_{dsatp} + V_{Tp})$$

$$= V_{DD} - 2V_{dsatp} - V_{Tp}$$

9.5



For calculating $V_{ICM(min)}$;

$$V_D = V_{dsatn} + V_{Tn}$$

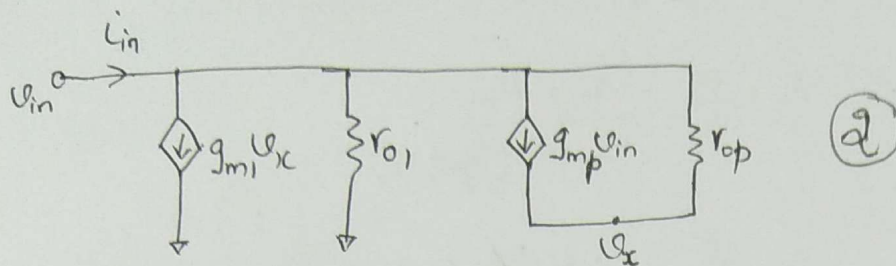
M1 will go to triode if V_G is decreased beyond $V_{ICM(min)}$.

$$\therefore V_S - V_{ICM(min)} - V_{Tp} = V_S - (V_{dsatn} + V_{Tn})$$

$$V_{ICM(min)} \Rightarrow V_{dsatn} + V_{Tn} - V_{Tp}$$

9.5

Q.1) Small signal Model



$$I_{in} = g_{m1}V_x + \frac{V_{in}}{r_{o1}} + \frac{(V_{in} - V_x)}{r_{op}} + g_m V_{in} \quad (1)$$

$$V_x = (1 + g_m r_{op}) V_{in}$$

$$\therefore I_{in} = \left[(1 + g_m r_{op}) \left(g_{m1} - \frac{1}{r_{o2}} \right) + g_m + \frac{1}{r_{o2}} \right] V_{in}$$

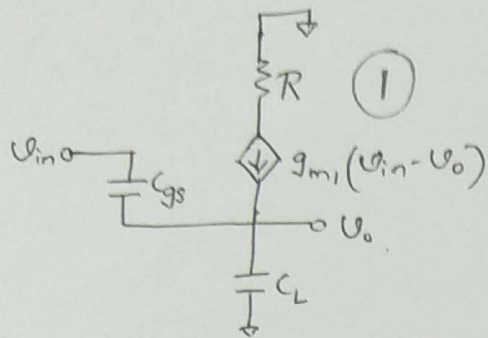
$$\therefore \frac{I_{in}}{V_{in}} = g_{m1} (1 + g_m r_{op})$$

$$\therefore Z_{in} \approx \frac{1}{g_{m1} g_m r_{op}} \quad (1), \text{ assuming } 1 + g_m r_{op} \approx g_m r_{op} \text{ i.e. } g_m r_{op} \gg 1.$$

For a simple current mirror, the input impedance $Z_{in} = \frac{1}{g_{m1}} \quad (1)$

Transistor M_p , reduces the input impedance by a factor $g_m r_{op}$ (Self gain of M_p)

Qh) Small signal Model



$$(V_0 - V_{in})sC_{gs} + V_0sC_L - g_m(V_{in} - V_0) = 0$$

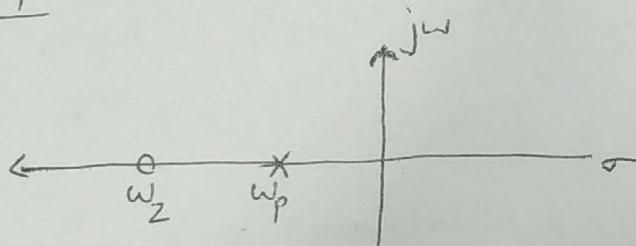
$$\therefore A_v = \frac{V_o}{V_{in}} = \frac{g_m + sC_{gs}}{g_m + s(C_{gs} + C_L)}$$

$$A_v = \frac{1 + s(g_m/C_{gs})}{1 + s\left(\frac{g_m}{C_{gs} + C_L}\right)}$$

\therefore Left Half plane zero, ω_z at $-g_m/C_{gs}$

\therefore Left Half plane pole, ω_p at $-g_m/(C_{gs} + C_L)$

Pole-Zero plot



Bode - plot

