

Binary_seach_with_answer.cpp

```

1  /**
2   *   author:  devesh95
3   *
4   **/
5  #include <bits/stdc++.h>
6  using namespace std;
7
8  #define int          long long int
9  #define double       long double
10 #define F           first
11 #define S           second
12 #define pb          push_back
13 #define lb          lower_bound
14 #define ub          upper_bound
15 #define si          set <int>
16 #define vi          vector <int>
17 #define vvi         vector <vi>
18 #define pii         pair <int, int>
19 #define vpi         vector <pii>
20 #define mii         map <int, int>
21 #define sz(v)       ((int) v.size())
22 #define form(i, a, b) for (int i=a; i<(b); i++)
23 #define forn(i, a)   for (int i=0; i<(a); i++)
24
25 ///////////////////////////////////////////////////////////////////
26 // Binary Search with Answer - Quick Notes
27 //
28 // Purpose: Solve optimization problems by finding the smallest or
29 //           largest value satisfying a condition.
30 //
31 // -----
32 // Problem Statement:
33 // Given n rectangles of size a x b, find the side length of
34 // the smallest square that can contain all rectangles.
35 //
36 // -----
37 // Steps:
38 // 1. Define the `Good` function:
39 //    - `Good(x)` checks if all rectangles can fit in a square of side `x`.
40 //
41 // 2. Binary Search for the answer:
42 //    - Initialize `l` as a bad value (e.g., 0).
43 //    - Initialize `r` as a good value, doubling until `Good(r)` is true.
44 //    - While `l + 1 < r`, calculate `m` as the midpoint of `l` and `r`.
45 //      a. If `Good(m)` is true, set `r = m`.
46 //      b. Otherwise, set `l = m`.
47 //
48 // 3. Result:
49 //    - `r` contains the smallest good value satisfying the condition.
50 //
51 // -----

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52 // Applications:
53 // - Optimization problems with a monotonic condition.
54 // - Finding minimum/maximum values in geometric or numeric setups.
55 //
56 // Tips:i) l is bad and r is good always.
57 //      ii) Don't forget to set precision when working with floating-point.
58 ///////////////////////////////////////////////////
59
60 // Function to solve the problem of finding the smallest square side length
61 void solve_smallest_square() {
62     int a, b, n;
63     cin >> a >> b >> n;
64
65     // Define the Good function
66     auto Good = [&](int m)->bool {
67         if ((m / a) * (m / b) >= n) return true;
68         return false;
69     };
70
71     int l = 0, r = 1; // l is bad and r is good always
72     while (!Good(r)) r *= 2;
73
74     while (l + 1 < r) {
75         int m = l + (r - l) / 2;
76         if (Good(m)) r = m;
77         else l = m;
78     }
79
80     cout << r << '\n';
81 }
82
83 // Function to solve the problem of finding the maximum rope length
84 // Problem Statement:
85 // There are n ropes, you need to cut k pieces of the same length from them.
86 // Find the maximum length of pieces you can get.
87 void solve_rope_problem() {
88     int n, k;
89     cin >> n >> k;
90     vi v(n);
91     forn(i, n) cin >> v[i];
92
93     // Define the Good function
94     auto Good = [&](double m)->bool {
95         int cnt = 0;
96         forn(i, n) {
97             cnt += (double)v[i] / m;
98         }
99         if (cnt >= k) return true;
100         return false;
101     };
102
103     double l = 0, r = 0.0000001;
104     while (Good(r)) r *= 2.0;
105

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106     while (r - l > 0.0000001) {
107         double m = l + (r - l) / 2.0;
108         if (Good(m)) l = m;
109         else r = m;
110     }
111     /* Another safe approach :
112     double l = 0, r = 1e8;
113     forn(i, 100) {
114         double m = (l + r) / 2;
115         if (Good(m))l = m;
116         else r = m;
117     }
118     cout << setprecision(20) << l << '\n';
119 }
120
121 int32_t main() {
122     ios_base::sync_with_stdio(0); cin.tie(0); cout.tie(0);
123
124     #ifndef ONLINE_JUDGE
125         freopen("input.txt", "r", stdin);
126         freopen("output.txt", "w", stdout);
127     #endif
128     clock_t z = clock();
129     int t = 1;
130     //cin >> t;
131     while (t--) {
132         solve_smallest_square();
133         solve_rope_problem();
134     }
135     cerr << "Run Time : " << ((double)(clock() - z) / CLOCKS_PER_SEC);
136     return 0;
137 }
138
```