

Binary Search Tree (BST) Operations: Time & Space Complexity

Operation	Balanced BST	Skewed BST	Iterative vs Recursive	Best Approach & Why?	Time Complexity	Space Complexity
Insert	Recursive (Good)	Iterative (Best)	Iterative (safe), Recursive (Readable)	Recursive is cleaner, but Iterative avoids deep recursion	$O(\log N)$ / $O(N)$	$O(\log N)$ / $O(1)$
Search	Recursive (Good)	Iterative (Best)	Iterative (best for large datasets)	Iterative is safer since recursion may cause stack overflow	$O(\log N)$ / $O(N)$	$O(\log N)$ / $O(1)$
Delete	Recursive (Best)	Iterative (Not Feasible)	Recursive (better logic handling)	Recursive is preferred for handling two-child deletion cases	$O(\log N)$ / $O(N)$	$O(\log N)$ / $O(1)$
Inorder Traversal	Recursive (Good)	Iterative (Good)	Recursive (best for depth reduction)	Recursive is natural, but Iterative needed for large trees	$O(N)$	$O(N)$ / $O(\log N)$
Preorder Traversal	Recursive (Good)	Iterative (Good)	Recursive (simple), Iterative (for large trees)	Iterative requires explicit stack, recursive is easier	$O(N)$	$O(N)$
Postorder Traversal	Recursive (Best)	Iterative (Feasible)	Recursive (better structured)	Iterative is tricky as it requires two stacks	$O(N)$	$O(N)$
Level Order (BFS)	Iterative (Best)	Iterative (Best)	Iterative (only feasible approach)	Uses a queue, recursion is not practical	$O(N)$	$O(N)$
Height Calculation	Recursive (Best)	Recursive (Not Feasible)	Recursive (uses simple logic)	$1 + \max(\text{left}, \text{right})$, but deep recursion issue in skewed trees	$O(N)$	$O(\log N)$ / $O(N)$
Check if BST is Balanced	Recursive (Best)	Recursive (Not Feasible)	Recursive (best approach)	Needs recursion to check height and balance	$O(N)$ / $O(N^2)$	$O(\log N)$ / $O(N)$

When to Use What?

Scenario	Best Approach	Why?
Tree is small or balanced	Use Recursive	Cleaner & more natural
Tree is large or unbalanced	Use Iterative	Prevents deep recursion & stack overflow
Level Order Traversal (BFS)	Use Iterative (Queue-based)	No recursion alternative
Deletion in BST	Use Recursive	Handles all cases efficiently
Performance is a concern	Use Iterative	Uses $O(1)$ space, avoids recursion overhead