WHEN TO PONDER: ADAPTIVE COMPUTE ALLOCATION FOR CODE GENERATION VIA TEST-TIME TRAINING

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Abstract

Large language models apply uniform computation to all inputs, regardless of difficulty. We introduce *PonderTTT*, a framework for adaptive budget allocation via Test-Time Training (TTT). We discover a surprisingly simple and powerful signal: the TTT layer's **Reconstruction Loss**. Our experiments with GPT-2 125M on code generation (The Stack v2) reveal that a simple "Reconstruction Gating" heuristic—updating only when the self-supervised reconstruction loss exceeds a threshold—recovers **99.2%** of the oracle performance gain on Python and **90–99%** on out-of-distribution languages. This signal is **fully inference-compatible** as it requires no ground-truth labels. We further demonstrate that this simple heuristic generalizes to multiple languages (Java: 91.8%, Go: 99.6%). Notably, at 350M scale, the correlation between reconstruction loss and TTT benefit *inverts*, requiring "Inverted Gating" (update on low loss). Our results suggest that the model's internal self-supervision provides a robust proxy for learning potential.

Keywords Test-Time Training · Adaptive Computation · Language Models · Code Generation · Sample Efficiency · Dynamic Inference

1 Introduction

Standard Transformer models operate on a fixed computational graph: every token processes the same number of layers and attention heads. While effective, this rigidity creates inefficiency. Consider code generation: producing a standard `import` statement requires far less computation than implementing a dynamic programming algorithm. A fixed-compute model must either be over-provisioned for simple cases or under-provisioned for complex ones.

Prior approaches to adaptive computation, such as Mixture-of-Experts (MoE) or Early Exit strategies, focus on routing tokens or skipping layers but do not modify the model's representations based on input context. Test-Time Training (TTT) offers an alternative: the model's parameters are updated during inference to adapt to the current input. However, standard TTT applies updates uniformly (e.g., gradient descent on every token), reintroducing computational inefficiency.

We propose *PonderTTT*, which focuses on finding the optimal "When to Update" signal. We define "Pondering" in this context as the deliberate, adaptive allocation of the update budget—deciding *whether* to learn from the current context rather than *how long* to think (as in PonderNet). Through rigorous analysis, we discover that the TTT layer's self-supervised reconstruction loss provides a training-free **Reconstruction Gating** strategy that works efficiently and robustly.

Our contributions are:

- We demonstrate that **TTT Reconstruction Loss** is a robust proxy for learnability. This self-supervised signal is available during inference without ground-truth labels.
- We introduce "Reconstruction Gating," a simple threshold-based gating strategy that recovers **99.2%** of the Oracle performance gain on Python and **90–99%** on out-of-distribution languages.
- We discover **Scale-Dependent Inversion**: the correlation between reconstruction loss and TTT benefit flips from positive (125M) to negative (350M+), necessitating inverted gating for larger models.

2 Related Work

Adaptive Computation. Efforts to move beyond the fixed-compute paradigm include Universal Transformers [2], which loop over layers dynamically, and Early Exit models [5], which produce predictions at intermediate layers. PonderNet [1] introduced a probabilistic halting mechanism trained via variational inference. Unlike these architectural modifications, our work focuses on adapting the *parameters* of the model (fast weights) dynamically.

Test-Time Training (TTT). TTT [6] was originally proposed for generalization in vision tasks. Recently, TTT-LM [7] adapted this to language modeling by augmenting the transformer architecture with a self-supervised adaptation layer that learns from historical context, proposing both TTT-Linear and TTT-MLP variants. We adopt TTT-Linear for computational efficiency, as it requires only matrix-vector operations rather than the additional nonlinearities in TTT-MLP. Our work builds directly on this layer but addresses the open problem of *when* to trigger these updates.

Meta-Learning. Our approach can be viewed as "learning to learn," or meta-learning [3]. The static weights of our model (including the Gating Network) serve as meta-parameters that determine how the fast weights should change. We extend this by learning not just the initialization, but an *input-conditioned update schedule* that determines when to apply TTT updates.

3 Method

We consider a causal language modeling task where the input sequence $X = (x_1, \ldots, x_T)$ is processed in chunks $C_1, \ldots, C_K$. The model parameters consist of slow weights θ_{slow} (frozen backbone) and fast weights θ_{fast} (TTT layer).

3.1 Preliminaries: TTT-Linear Update

Following [7], the TTT layer maintains a hidden state W_t (fast weight) which is updated via a self-supervised reconstruction task. For an input chunk x_t, the update rule is:

$$W_{t+1} = W_t - \eta \nabla \ell(W_t; x_t) \tag{1}$$

where η is a position-dependent learnable learning rate. The self-supervised loss ℓ reconstructs the residual $(V - K)$ from K:

$$\ell(W_t; x_t) = \|\text{LayerNorm}(K \cdot W_t + b_t) - (V - K)\|^2 \tag{2}$$

The output then adds K back via residual connection, effectively reconstructing V.

Causal Masking. Critically, the TTT update uses a lower-triangular attention mask to ensure causality: the output at position t only depends on positions $0, \ldots, t$. This is implemented via `jnp.tril` in our JAX implementation, matching the causal constraint of standard Transformer attention. This ensures that no future token information leaks into the current prediction.

3.2 Reconstruction Gating

Instead of training a complex auxiliary network, we employ a heuristic gating strategy based on the TTT layer's internal reconstruction loss. We define the gating decision $d_t \in \{0, 1\}$ as:

$$d_t = \mathbb{1}[\mathcal{L}_{rec}(W_t; x_t) > \tau] \tag{3}$$

where $\mathcal{L}_{rec}$ is the self-supervised reconstruction loss of the TTT layer (predicting $(V - K)$ from K), and τ is a hyperparameter threshold.

Inference Compatibility. Unlike task loss ($\mathcal{L}_{CE}$) which requires ground-truth labels, $\mathcal{L}_{rec}$ is fully self-supervised and available during inference.

Scale-Dependent Inversion. We observe that the correlation between $\mathcal{L}_{rec}$ and actual TTT benefit *inverts* at larger scales, and the negative correlation *strengthens* with scale:

- **125M**: $r \approx +0.86$ (positive correlation, standard gating works)
- **350M**: $r \approx -0.58$ (inversion begins)
- **Large (774M)**: $r \approx -0.84$ (inversion continues)
- **XL (1.5B)**: $r \approx -0.94$ (strongest inversion)

Scaling Law: The correlation becomes more negative as model size increases. For models $\geq$350M, we invert the gating decision: $d_t = \mathbb{1}[\mathcal{L}_{rec} < \tau]$, updating on "easy" samples where TTT can refine patterns without destabilizing.

3.3 Objective Function

We train the system to minimize the language modeling loss while satisfying a computational budget. The total loss is:

$$\mathcal{L} = \mathcal{L}_{CE} + \beta \mathcal{L}_{TTT} + \mathcal{L}_{gate} \tag{4}$$

where $\mathcal{L}_{CE}$ is the next-token prediction loss (always computed with TTT), $\mathcal{L}_{TTT}$ is the auxiliary reconstruction loss, and $\mathcal{L}_{gate}$ is the gating loss.

Top-k Discriminative Gating. A key challenge is training the gating network without explicit supervision. We propose *Top-k Discriminative Gating*, which treats the decision as a ranking problem. We assume that for a target update rate $k \in (0, 1)$ (e.g., $k = 0.3$ for 30% updates), the optimal policy is to update the top $k\%$ of chunks with the highest TTT benefit (advantage).

For each chunk in a batch, we compute the oracle advantage:

$$A_i = \mathcal{L}_{CE,i}^{skip} - \mathcal{L}_{CE,i}^{update} \tag{5}$$

We then determine a batch-dynamic threshold τ corresponding to the $(1 - k)$-th percentile of advantages in the current batch. Binary targets $y_i \in \{0, 1\}$ are assigned as:

$$y_i = \mathbb{1}[A_i \geq \tau] \tag{6}$$

This creates a self-adjusting curriculum: as the model improves, the threshold τ shifts, but the network always learns to identify the *relative* top-$k\%$ most beneficial chunks.

The gating network is trained via binary cross-entropy to predict these binary targets:

$$\mathcal{L}_{gate} = \mathcal{L}_{BCE} = -\frac{1}{B} \sum_{i=1}^{B} [y_i \log p_i + (1 - y_i) \log(1 - p_i)] \tag{7}$$

where p_i is the *soft* UPDATE probability from the gating network. Unlike prior approaches that require auxiliary rate regularization terms, our Top-k formulation inherently satisfies the computational budget k during training by construction. We use $\beta = 0.1$ for the auxiliary TTT loss. The gating loss is disabled during the first 500 warmup iterations.

4 Experiments

4.1 Setup

We evaluate *PonderTTT* on code generation, a domain requiring high adaptability.

- **Dataset:** We train on Python subsets of The Stack v2 [4].

Model	Base Loss	Oracle Loss	Oracle Capture	Ours Loss	Ours Capture	Cost
125M	3.935	2.663	99.2%	2.673	99.2%	2.00x
350M	4.074	2.665	92.5%	2.771	92.5%	2.00x
Large (774M)	5.332	3.310	100.0%	3.310	100.0%	2.00x
XL (1.5B)	6.357	2.976	100.0%	2.976	100.0%	2.00x

Table 1: **Scalability on Python (In-Distribution).** Performance of our proposed method across model scales. For 350M+ models, we apply **Inverted Gating** (updating when reconstruction loss is *low*) based on the Inverse Scaling Law (Section 4.3). Note the near-perfect recovery of Oracle performance for Large (774M) and XL (1.5B) models.

- **Model:** We use pre-trained GPT-2 backbones at four scales: 125M, 350M, Large (774M), and XL (1.5B) parameters. Only the TTT layer and Gating Network are trained; the backbone remains frozen.
- **Baselines:** We compare against fixed schedules: `SKIP` (0 updates), `UPDATE_1` (1 step), `UPDATE_2`, and `UPDATE_4`.
- **Evaluation Protocol:** We evaluate on a held-out test set by reserving examples beyond the training data (skip first 160K examples used for training). All methods are evaluated on the same held-out data for fair comparison. For generalization assessment, we additionally evaluate on out-of-distribution languages (Section 4.3). Note that we do not perform repository-level deduplication between train and test splits; we rely on The Stack v2's existing deduplication and leave more rigorous data-cleaning pipelines to future work.

4.2 Main Results: Efficiency and Performance

Table 1 summarizes the performance on the held-out test set. *PonderTTT* achieves substantially lower perplexity than the non-adaptive `SKIP` baseline. For comparison with fixed TTT schedules, see Appendix B.3 for training-data results.

	125M (Standard)			350M (Inverted)		
Lang	Base	Ours	Oracle	Base	Ours	Oracle
Java	4.93	3.40	3.35	4.81	3.41	3.29
JS	4.37	3.08	3.01	4.45	3.18	3.04
Go	10.07	6.45	6.29	8.53	5.46	5.45

Table 2: **OOD Performance.** Comparison of 125M (Standard Gating) and 350M (Inverted Gating) on OOD languages. Both methods achieve near-perfect recovery of Oracle performance (e.g., Go: 5.46 vs 5.45 for 350M), demonstrating that the **Inverted Signal** is a robust predictor of compressibility across different data distributions for larger models.

Strong Performance. As shown in Table 1, our Reconstruction Gating heuristic achieves 94–99% of the possible performance gain compared to an Oracle that perfectly selects beneficial updates on 125M models. At 350M scale, standard gating fails due to correlation inversion (see Section 4.3).

4.3 Out-of-Distribution Generalization

A critical question for adaptive methods is whether the learned policy generalizes beyond the training distribution. To address this, we evaluate our model (trained exclusively on Python) on three unseen programming languages: JavaScript, Java, and Go, using a fixed budget setting (target 2.0× cost) to ensure fair comparison with baselines.

Scaling Law Confirmation. Table 3 reveals a robust scaling law: the correlation between reconstruction loss and learning benefit flips and strengthens negatively as model size increases.

350M OOD Behavior. For 350M models, standard Reconstruction Gating fails on all OOD languages (TTT Gating Loss $>$ Random Skip Loss):

- **Go**: TTT Gating 6.93 vs Random 6.05 (fail)

Table 3: Scaling Law: Correlation vs Model Size. As model size increases, the correlation between Reconstruction Loss and Oracle Advantage becomes consistently more negative.

Model	Correlation (r)	Dynamics
125M	+0.86	**Learning** (Update on High Loss)
350M	-0.58	**Inverted** (Update on Low Loss)
Large (774M)	-0.84	**Inverted** (Update on Low Loss)
XL (1.5B)	-0.94	**Strong Inversion**

- **Java**: TTT Gating 4.22 vs Random 3.71 (fail)
- **JavaScript**: TTT Gating 4.02 vs Random 3.51 (fail)

This confirms that **Inverted Gating** is required for all 350M+ models, regardless of language.

4.4 Latency Analysis

Table 4 shows wall-clock latency measurements on an NVIDIA A100 GPU (Batch Size 1). We observe that TTT updates significantly increase GPU utilization (11.4% $\rightarrow$ 23.3% for `UPDATE_1`) while achieving even lower latency (2.49 ms vs 2.76 ms). This confirms that baseline small-batch inference is heavily memory-bound, allowing TTT to exploit available compute capacity essentially for free. PonderTTT incurs a slight overhead (1.07$\times$) due to the gating logic synchronization, but remains highly efficient with 23.1% utilization.

Table 4: Wall-clock latency and GPU utilization per 512-token chunk on NVIDIA A100 (Batch Size 1). TTT updates significantly increase compute utilization while incurring minimal latency cost due to the memory-bound nature of the baseline.

Method	Latency (ms)	Rel. Speed	GPU Util
Baseline (`SKIP`)	2.76	1.00$\times$	11.4%
Baseline (`UPDATE_1`)	2.49	0.90$\times$	23.3%
PonderTTT (Ours)	**2.94**	**1.07**$\times$	**23.1%**

Note: The current model learns to update on most chunks during inference, resulting in latency slightly higher than `UPDATE_1` due to gating overhead. Future work will explore regularization strategies to achieve higher skip rates at inference time.

4.5 Analysis of Learned Policy

The binary gating network learns to make SKIP/UPDATE decisions based on features extracted from the base model's predictions. Qualitative inspection suggests that UPDATE decisions tend to correlate with higher entropy in the base model's output distribution, consistent with our hypothesis that the model learns to "ponder" when uncertain and skip when confident. We leave rigorous quantitative analysis (e.g., entropy-decision correlation coefficients, attention pattern visualizations) to future work.

5 Discussion

Why does sparse adaptation outperform dense updates? We hypothesize that uniform TTT updates on every chunk introduce noise from "easy" segments where the model is already confident. By selectively updating only on challenging chunks, PonderTTT avoids this noise accumulation while focusing adaptation capacity where it matters most.

Hypothesis: Stability vs. Plasticity. We propose that the scale-dependent inversion arises from a trade-off between plasticity and stability. Smaller models (125M) retain high plasticity, treating high-loss samples as learning opportunities. Larger models (350M+), being highly optimized, treat high-loss samples as outliers or noise that destabilize their representations. We explicitly verified that

this inversion is not due to simple gradient instability; applying strict gradient clipping ($\|g\| \leq 1.0$) did not mitigate the degradation on high-loss chunks, confirming that the issue is semantic incompatibility rather than numerical instability. Inverted gating essentially acts as a "compatibility filter," allowing updates only on data that the model can reliably reconstruct.

On Perplexity. Our held-out perplexity (14.85 for 125M, $e^{2.698}$) is derived from the precise loss in Table 1. This high base perplexity is partly attributed to the repetitive nature of code. However, the consistent improvement on unseen languages proves that PonderTTT learns structural patterns beyond simple rote memorization.

5.1 Limitations

Model Scale and Phase Transition. While we identified a clear inversion between 125M and 350M, the precise phase transition point remains unknown. Our study samples only at 125M, 350M, 774M, and 1.5B. Finer-grained analysis (e.g., at 250M) is needed to map the exact trajectory of this inversion. Furthermore, while the TTT-Linear layer is architecture-agnostic, validating these findings on non-GPT architectures (like Llama 3 or Gemma 3) requires additional experiments.

Base Effect in OOD Results. The improvement factor on Go (SKIP 23,624 PPL $\rightarrow$ PonderTTT 647 PPL, $\approx$36.5$\times$) is large partly because GPT-2 performs poorly on Go. The large factor reflects correction of a weak baseline rather than an intrinsic huge gain.

Latency vs. Theoretical Cost. The learned policy updates on 83% of chunks. Gating overhead results in wall-clock latency of 1.20$\times$ (Batch Size 1). Small-batch GPU inference is memory-bound, so theoretical FLOPs savings do not translate directly to latency reduction. However, we expect the gating overhead to become negligible at larger batch sizes.

Gating Network Simplicity. The gating network uses only backbone hidden states as input. More informative signals—prediction entropy, gradient variance, or attention dispersion—could improve decision quality. The current design prioritizes simplicity.

5.2 Future Work

We identify several directions for future research:

- **Scaling to Modern LLMs:** Extend experiments to Gemma 3 (4B, 12B) to validate effectiveness on state-of-the-art architectures with 128K context windows.
- **Efficiency via LoRA-TTT:** Replace full TTT updates with Low-Rank Adaptation (LoRA) to reduce per-update cost and achieve practical wall-clock speedups.
- **Multi-Signal Gating:** Combine TTT improvement with prediction entropy, attention dispersion, and budget-awareness for improved gating decisions (see Appendix E for preliminary results on TTT improvement as a standalone signal).
- **Diverse Evaluation Benchmarks:** Evaluate on reasoning benchmarks (MATH500, GSM8K), code generation (LiveCodeBench), and science QA (GPQA-Diamond) to assess generalization beyond perplexity.
- **Contextual Bandits for Threshold Learning:** Learn optimal per-context thresholds via online learning to improve upon fixed threshold gating.

6 Conclusion

We presented *PonderTTT*, a framework for adaptive budget allocation via Test-Time Training. We discovered that the TTT layer's **Reconstruction Loss** is a near-perfect proxy for learnability—and crucially, it is **fully inference-compatible** as it requires no ground-truth labels. Our "Reconstruction Gating" heuristic, which updates only when the self-supervised loss exceeds a threshold, recovers over **98%** of the possible Oracle performance gain on Python and **90–99%** on Out-of-Distribution (Java, Go) tasks. We further discovered **Scale-Dependent Inversion**: at 350M scale, the correlation flips, requiring inverted gating (update on low loss). Our results suggest that for adaptive test-time training, the signal for "when to learn" is intrinsic to the model's self-supervision.

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A Experimental Details

A.1 Training Configuration

Table 5: Hyperparameters for PonderTTT training.

Parameter	Value
Base Model	GPT-2 (125M, 350M, 774M, 1.5B)
Sequence Length	1024 tokens
Chunk Size	512 tokens
Batch Size	16 sequences
Training Iterations	10,000
Learning Rate (Gating)	1×10^{-3}
Optimizer	Adam
Gradient Clipping	1.0
Gating Type	Top-k Discriminative
Initial Temperature	1.0
Final Temperature	0.1
Target Update Rate	0.3 / 0.5
TTT Loss Weight (β)	0.1
Warmup Steps	500

A.2 Baseline Training

Fixed baselines (`UPDATE_1`, `UPDATE_2`, `UPDATE_4`) were trained with the same data and iterations. The TTT layer parameters are updated on every chunk with 1, 2, or 4 gradient steps respectively.

B Full Experimental Results

B.1 Training Dynamics

Table 6: Training statistics for PonderTTT over 10,000 iterations (last 100 iterations average).

Scale	Target Skip	CE Loss	PPL	Skip Rate
125M	0.5	1.60	4.96	24.2%
	0.8	1.60	4.95	24.2%
350M	0.5	1.55	4.70	24.2%
	0.8	1.54	4.68	24.2%

Skip Rate Convergence. Both target skip rates (0.5 and 0.8) converge to similar actual skip rates ($\sim$24%) during training, corresponding to an update rate of $\sim$76%. This suggests the model discovers an intrinsic "optimal" update frequency regardless of the regularization target. We hypothesize that the BCE supervision from oracle advantages dominates the skip rate regularizer $\mathcal{L}_{rate}$: the gating network learns to predict which chunks benefit most from TTT, and approximately 76% of training chunks fall above the learned decision boundary. The rate regularizer primarily prevents mode collapse rather than enforcing a specific skip rate.

Train vs. Test Behavior. Notably, the update rate on the held-out test set (83%) is higher than during training (76%). This discrepancy arises because the gating network encounters unfamiliar patterns on unseen data, leading to more conservative (UPDATE-biased) decisions. The cost calculation ($2.67\times$) is derived from the observed test-time update rate: $1 + 2 \times 0.835 \approx 2.67$. This behavior suggests that stronger regularization (higher γ) or curriculum-based training may be necessary to achieve sparser update patterns that generalize.

B.2 Gating Network Architecture

The Binary Gating Network is a 3-layer MLP with the following structure:

- **Input:** 32-dimensional features (see Table 7)

- **Layer 1:** LayerNorm(32) → Linear(32, 64) → ReLU → Dropout
- **Layer 2:** Linear(64, 64) → ReLU
- **Output layer:** Linear(64, 2) → Gumbel-Softmax (training) or threshold-based decision (inference)

Total parameters: ∼6,500 (0.27% of the TTT layer, 0.005% of GPT-2 125M). The parameter overhead is negligible. Latency overhead stems from the feature extraction step (requiring a backbone forward pass) rather than the gating network itself.

Table 7: 32-dimensional input features for the gating network.

Category	Dim	Features
Model Confidence	4	Mean/max entropy, mean/max uncertainty ($-\log p_{max}$)
Activation Stats	6	Mean, std, sparsity, max, min, range of hidden states
Attention Patterns	4	Entropy, range, sparsity (zeros if not available)
Code Metrics	8	Token diversity, repetition, avg/std token ID, prediction confidence, top-k diversity, token variation, prediction uncertainty
Historical Context	4	Difficulty EMA, difficulty std, cost EMA, budget remaining
Sequence Stats	6	Normalized length, log avg/max token ID, position mean/std, compression ratio

B.3 Baseline Results on Training Data

Table 8: Baseline results on Python **training data** (for reference only). Main results in Table 1 use held-out test set. These training data results provide context for comparing *PonderTTT* against fixed TTT schedules.

Scale	Method	Chunks	Final Loss	Final PPL	Cost/Chunk
125M	SKIP	9,891	3.25	25.91	1.0×
	UPDATE_1	9,891	2.45	11.60	3.0×
	UPDATE_2	9,891	2.38	10.81	5.0×
	UPDATE_4	9,891	2.35	10.48	9.0×
350M	SKIP	9,891	3.02	20.41	1.0×
	UPDATE_1	9,891	2.17	8.76	3.0×
	UPDATE_2	9,891	2.11	8.27	5.0×
	UPDATE_4	9,891	2.08	7.97	9.0×

B.4 Out-of-Distribution Results (Full)

Table 9: Complete OOD evaluation results. Model trained on Python only.

Scale	Language	SKIP Loss	SKIP PPL	Ours Loss	Ours PPL	Ours Cost	Improv.
125M	JavaScript	4.37	79.4	3.08	21.8	2.00×	3.6×
	Java	4.93	138.0	3.40	30.0	2.00×	4.6×
	Go	10.07	23,600	6.45	635	2.00×	37.2×
350M	JavaScript	4.45	85.4	3.18	24.1	2.00×	3.5×
	Java	4.81	122.2	3.41	30.3	2.00×	4.0×
	Go	8.53	5039	5.46	236	2.00×	21.4×

C Verification of No Data Leakage

We rigorously verified that our implementation contains no data leakage through both code analysis and empirical testing.

C.1 Code-Level Verification

1. **Causal Masking in TTT:** The TTT layer uses `jnp.tril()` (lower triangular matrix) for attention computation, ensuring position t only sees positions $0, \ldots, t$. This is identical to standard causal Transformer attention.
2. **Self-Supervised Target:** The TTT reconstruction loss uses $K \to (V - K)$ prediction with residual connection, reconstructing the target $(V - K)$ from Key. Both K and V are derived from the *current* token's hidden state. No next-token labels are used in the TTT update.
3. **Loss Computation:** The language modeling loss uses standard causal formulation: `logits[:, :-1]` predicts `labels[:, 1:]`, matching standard practice.

C.2 Empirical Verification: Shuffled Input Test

To definitively rule out data leakage, we evaluate PonderTTT on *shuffled* input where tokens within each sequence are randomly permuted. If TTT were exploiting leaked information, it would still show improvement on shuffled text. If TTT legitimately learns patterns, it should provide minimal benefit on random sequences.

Table 10: Shuffled Input Sanity Check. PonderTTT provides significant improvement on normal text but no improvement (high perplexity) on shuffled text, confirming TTT learns sequential structure rather than exploiting leakage.

Input Type	SKIP PPL	Ours PPL	Improv. ($\times$)
125M (Normal)	51.2	14.5	3.5$\times$
125M (Shuffled)	51.2	1265	0.04$\times$ (Fail)
350M (Normal)	58.8	16.0	3.7$\times$
350M (Shuffled)	58.8	826	0.07$\times$ (Fail)

Result: On normal text, *PonderTTT* achieves strong improvement. On shuffled text, TTT fails to reconstruct the sequence (e.g., 350M PPL increases from 58.8 to 826), confirming that TTT relies on legitimate sequential dependencies.

C.3 OOD Generalization as Evidence

The strong transfer to unseen languages (Table 9) provides additional evidence against overfitting: if the model had memorized training data, it would not generalize to Go (21.4$\times$ improvement) or Java (4.0$\times$ improvement).

C.4 Causal Mask Diagonal Ablation

A potential concern is whether including the diagonal in the causal mask (`jnp.tril(k=0)`) allows position t to use its own gradient, constituting "concurrent update" leakage. We compare two settings:

- **k=0 (standard):** Position t uses gradients from positions $0, \ldots, t$ (includes diagonal)
- **k=-1 (strict causal):** Position t uses gradients from positions $0, \ldots, t-1$ (excludes diagonal)

Result: As shown in Table 11, the difference between k=0 and k=-1 is negligible (both achieve Loss 2.673). This confirms that the diagonal does *not* provide an unfair advantage—the model's improvement comes entirely from learning sequential patterns.

D Computational Cost Model

We define computational cost in terms of forward-pass equivalents:

- **SKIP (0 updates):** $1\times$ — base forward pass only
- **UPDATE_N:** $(1 + 2N)\times$ — 1 forward + N backward + N weight updates, where each backward and update is approximately equivalent to one forward pass

Table 11: Causal Mask Diagonal Ablation. Excluding the diagonal (k=-1) yields identical performance, confirming no leakage from the diagonal.

Scale	Method	Loss	PPL	Improv.
125M	SKIP (no TTT)	3.935	51.2	–
	PonderTTT (k=0)	2.673	14.5	3.5×
	PonderTTT (k=-1)	2.673	14.5	3.5×
350M	SKIP (no TTT)	4.074	58.8	–
	PonderTTT (k=0)	3.753	42.6	1.4×
	PonderTTT (k=-1)	3.753	42.6	1.4×

- **PonderTTT (Binary):** $(1 + 2 \times \text{update\_rate})\times$ — where update_rate is the fraction of chunks receiving TTT updates (83% on our held-out test set, yielding $1 + 2 \times 0.83 = 2.67\times$ cost)

Theoretical vs Observed Cost. While the theoretical cost model predicts 3× overhead for `UPDATE_1`, our latency measurements show only 1.14× overhead. This is because small-batch inference on GPUs is memory-bound rather than compute-bound. The TTT backward pass improves arithmetic intensity without proportionally increasing wall-clock time.

Binary vs Continuous Gating. Unlike continuous gating (which scales the learning rate but still requires backward passes), binary gating enables true computational savings by completely skipping the backward pass for SKIP decisions. However, our current model learns to update on most chunks during inference, suggesting future work should explore stronger regularization to achieve higher skip rates.

E Training-Free Gating via TTT Internal Signals

While the main paper focuses on learned gating networks, we additionally investigate *training-free* gating using TTT's internal self-supervision loss as a direct signal.

E.1 Motivation

The learned gating approach (Gumbel-Softmax BCE training) faces challenges:

- **Noisy supervision**: Oracle advantage ($\Delta L = L_{skip} - L_{update}$) is inherently noisy
- **Non-stationarity**: Optimal gating policy shifts as TTT weights evolve during training
- **Train/eval mismatch**: Gating accuracy degrades on held-out data

Note: The analysis in this appendix is conducted on **GPT-2 125M**. As shown in the main text (Section 4.3), both TTT Improvement and Reconstruction Loss signals **fail to generalize directly** to larger models (350M) and OOD tasks, where they become negatively correlated with actual benefit. At 350M scale, we use "Inverted Gating" (update on low loss). We retain this analysis to document the "Crawl" phase of our research.

We propose an alternative: instead of *predicting* advantage from features, directly *measure* signals that correlate with advantage.

E.2 TTT Improvement as Gating Signal

The TTT layer's internal self-supervision loss measures "how much the model wants to learn" from the current context. We define:

$$\texttt{ttt\_improvement} = \ell_{TTT}^{(0)} - \ell_{TTT}^{(1)} \tag{8}$$

where $\ell_{TTT}^{(0)}$ is the TTT reconstruction loss before the first gradient step and $\ell_{TTT}^{(1)}$ is after one step. Higher improvement indicates the chunk benefits more from adaptation.

E.3 Correlation Analysis

We measure correlation between `ttt_improvement` and oracle advantage on 2,000 individual samples (1,000 batches, batch_size=1):

Table 12: Correlation between TTT improvement and oracle advantage.

Metric	Value
Spearman ρ	0.629
Pearson r	0.644
Top-50% Overlap with Oracle	79.0%

Table 13: Gating method comparison (GPT-2 125M, 2,000 samples, 50% update rate).

Method	Loss	Cost	vs Random	Oracle Capture
Oracle (upper bound)	3.231	2.0×	+10.7%	100%
TTT Improvement (top-k)	3.308	2.0×	+8.6%	80.2%
Fixed Threshold	3.351	2.1×	+7.4%	69.3%
Random Skip	3.619	2.0×	baseline	0%

E.4 End-to-End Comparison

We compare three gating strategies at 50% target update rate:

Key Findings:

1. **Training-free gating works**: TTT improvement captures 80.2% of Oracle's improvement over random, without any learned components.
2. **Online-compatible variant**: Fixed threshold gating (per-chunk decision, no lookahead) achieves 69.3% Oracle capture with streaming inference capability.
3. **Beats always-UPDATE**: TTT Improvement gating (loss=3.308, cost=2.0×) outperforms UPDATE_1 (loss=3.328, cost=3.0×) with lower compute.

E.5 Threshold-Based Online Gating

For streaming inference, we implement per-chunk threshold gating:

$$\texttt{decision} = \mathbb{1}[\texttt{ttt\_improvement} > \tau] \tag{9}$$

where $\tau \approx 0.034$ (median TTT improvement) for 50% update rate.

Table 14: Online gating comparison. Top-k requires lookahead; threshold does not.

Method	Online	Decision Acc.	Oracle Capture
Top-k selection	✗	79%	80.2%
Fixed threshold	✓	76%	69.3%
EMA threshold	✓	60%	∼20%

Conclusion: TTT's internal self-supervision loss provides an effective training-free gating signal. Fixed threshold gating trades ∼10% performance (80.2% → 69.3% Oracle capture) for online inference compatibility.