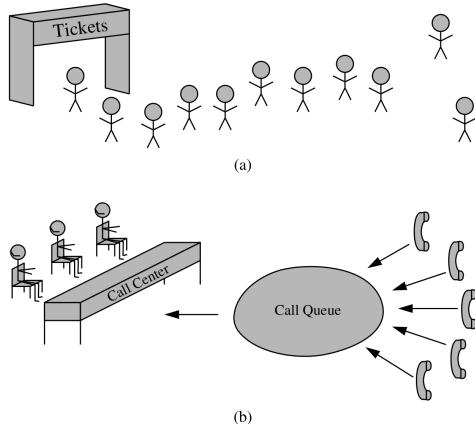


Queues

- Collection of objects that are inserted and removed according to the first-in, first-out (FIFO)
- Elements can be inserted at anytime, but only the element that has been in the queue the longest can be nexted removed.

Examples:

- 1) Printers
- 2) Web server responding to requests.
- 3) Scheduling



Nike SNKR App
~ for some drops

Figure 6.4: Real-world examples of a first-in, first-out queue. (a) People waiting in line to purchase tickets; (b) phone calls being routed to a customer service center.

The Queue Abstract Data Type

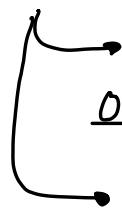
- ~ The Queue abstract data type defines a collection that keeps objects in sequence, where element access and deletion are restricted to the first elements in the queue, and element insertion is restricted to the back of the sequence.

The queue abstract data type (ADT) supports two methods for a queue Q:

Operations:

Q.enqueue(e): Add element e to the back of queue Q.

Q.dequeue(): Remove and return the first element from queue Q;
an error occurs if the queue is empty.



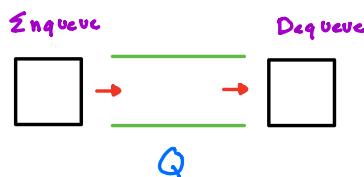
Constant
time
or
 $O(1)$

Other supporting Methods:

Q.first(): Return a reference to the element at the front of queue Q,
without removing it; an error occurs if the queue is empty.

Q.is_empty(): Return True if queue Q does not contain any elements.

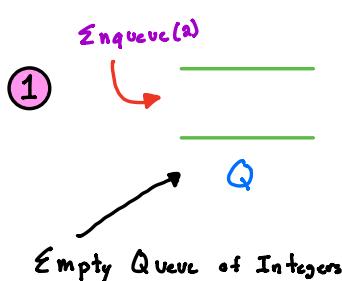
len(Q): Return the number of elements in queue Q; in Python,
we implement this with the special method `__len__`.



~ logically, a queue can be shown as a figure or container open from two sides.

~ An element can be inserted or Enqueued from one side and an element can be removed or de-queued from other side.

~ In queue, insertion and removal should happen from different sides.



Logic/Code

Enqueue (1) ①

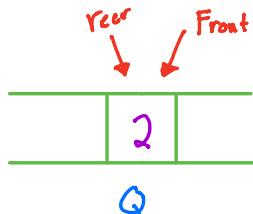
Enqueue (5) ②

Enqueue (3) ③

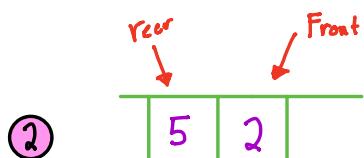
Dequeue() → 2 ④

front() → 5

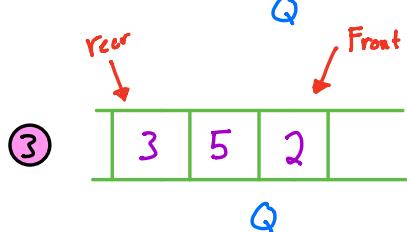
IsEmpty → false



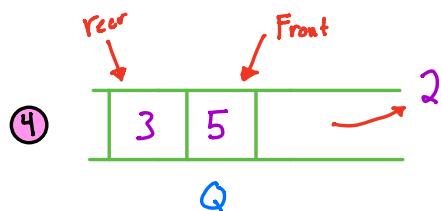
~ After this, Enqueue, we have one element in the queue



~ Insert another integer,

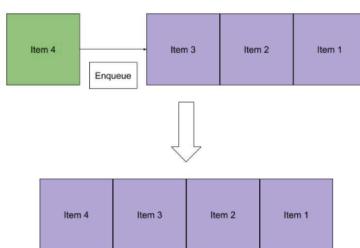


~ Insert another integer,

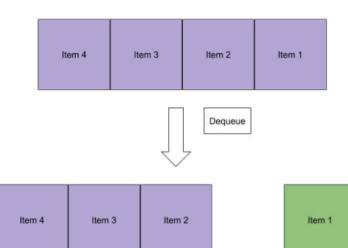


~ 2 will head out of the queue
~ Front moves over to the next item to be queued.

- **enqueue** - adds an element to the end of the queue:



- **dequeue** - removes the element at the beginning of the queue:

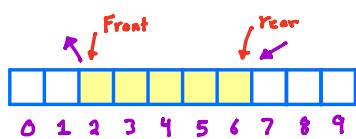


How do we implement this in Python?

- Circular Array ✓

- linked lists

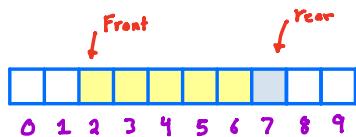
Array Implementation



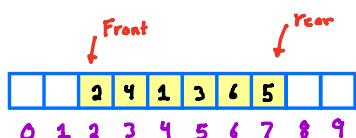
~ any order of front and rear

~ But element must be added from rear and removed from front

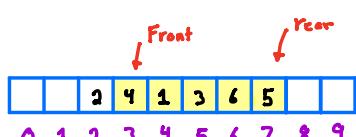
~ At any stage a segment of the array from an index marked as front till an index marked as rear is my Queue and the rest of positions in the array are free space, that can be used to expand the Queue.



~ add a new element towards the rear end, we can write the element to be inserted



~ Inserting the number 5



~ Removing an element from the Queue

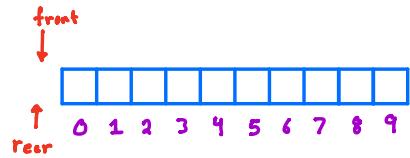
~ By incrementing front we have discarded index 2 from the Queue

Writing Pseudo Code:

- is the array Empty? ↴

```

Front = A[-2]
Rear = A[-2]
IsEmpty():
    if A[Front] == -1 and A[Rear] == -1:
        return True
    else:
        return False
  
```



Q.enqueue(e): Add element e to the back of queue Q.

Q.dequeue(): Remove and return the first element from queue Q; an error occurs if the queue is empty.

Adding an Element to an Queue

Enqueue(x):

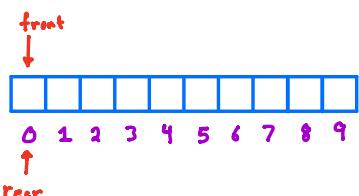
```

if IsFull():
    return
else if IsEmpty():
    front, rear = A[0]
else:
    rear = rear + 1
A[rear] = x
  
```

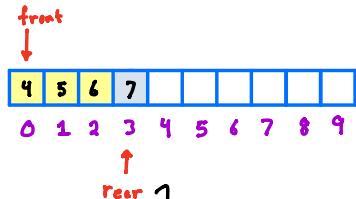
← If array is full return

← If it's not empty

else if:



else ~ Not Empty or Full



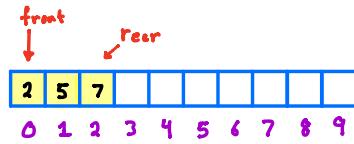
+1 for rear
that becomes the new value
inserted into the Queue

Lets Enqueue some elements:

Enqueue(2)

Enqueue(5)

Enqueue(7)



Dequeue Sudo Code:

Dequeue():

if IsEmpty():
return

else if front == rear:
front, rear = A[-1] ~ if Q has one element
~ Our Dequeue will
make the Queue empty

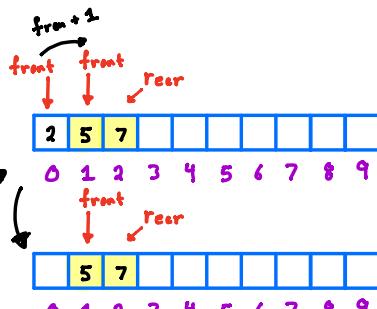
else:
front = front + 1 ~

Enqueue(2)

Enqueue(5)

Enqueue(7)

Dequeue() → It will increment front



- Front will be
incremented, and our
Value will be returned

Enqueue(3)

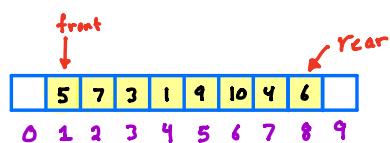
Enqueue(1)

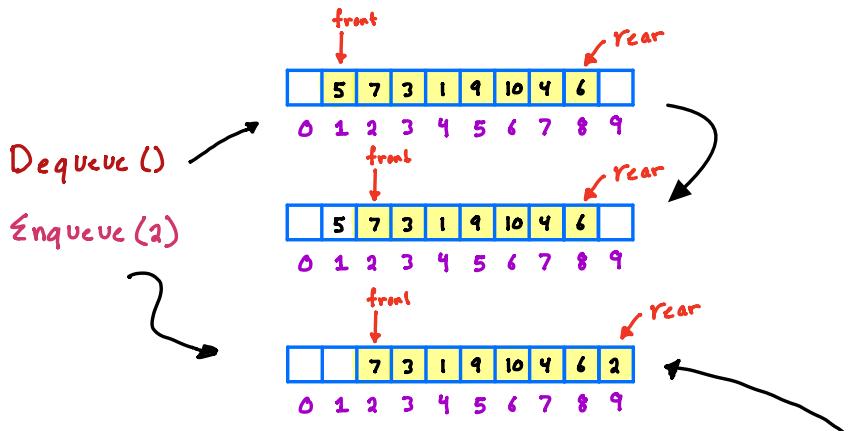
Enqueue(9)

Enqueue(10)

Enqueue(4)

Enqueue(6)

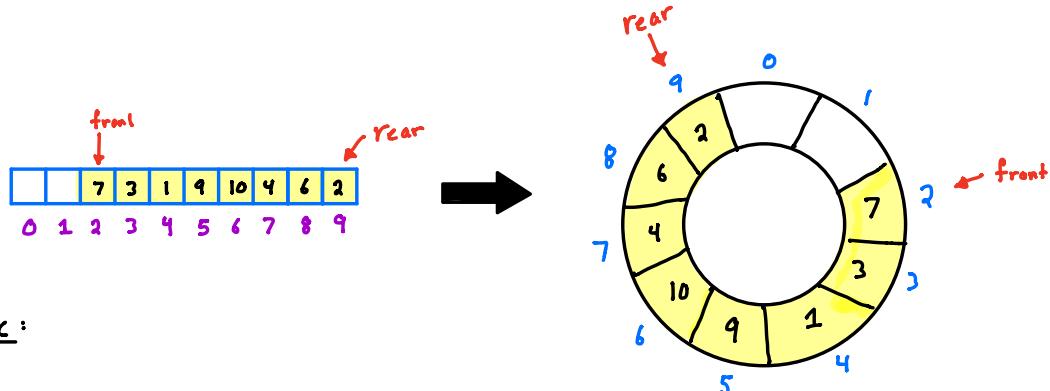




At this point, we cannot Enqueue an element anymore

- What will we do!?

Circular Array



Logic:

Current position = i

Next position = $(i+1) \% N$ \leftarrow Size of Array
 \sim Will give remainder

Previous position = $(i+N-1) \% N$

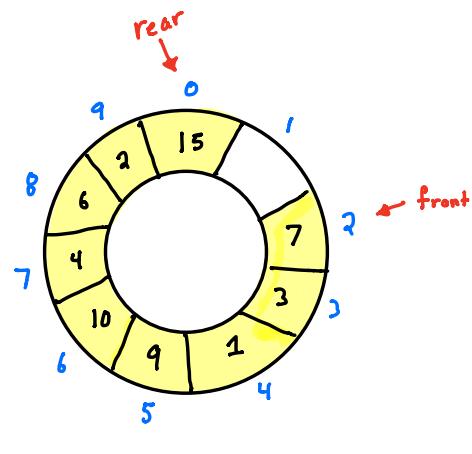
For the Example above:

$$i = N-1 \\ \text{Next} = N \% N = 0$$

Modify Sudo Code:

```
IsEmpty():
    if front == -1 and rear == -1:
        return True
    else:
        return False
```

```
Enqueue(x):
    if (rear+1) % N == Front
        return
    else if IsEmpty():
        front, rear = 0
    else:
        rear = (rear + 1) % N
    A[rear] = x
    ↗ Modular
    ↗ Gives us the
    ↗ remainder!
```



Enqueue(15)

$$\begin{aligned} \text{rear} &= (\text{rear} + 1) \% N \\ &= (9 + 1) \% 10 \\ \text{rear} &= 0 \end{aligned}$$

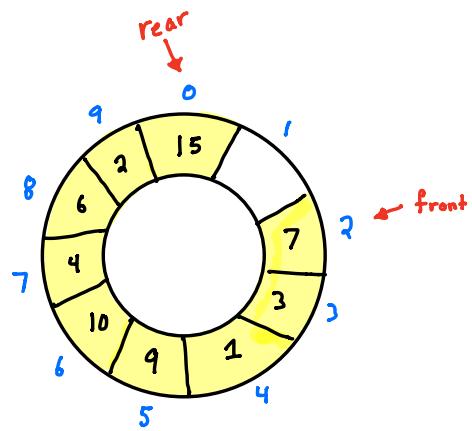
$$\begin{aligned} A[\text{rear}] &= x \\ A[0] &= 15 \end{aligned}$$

Dequeue()

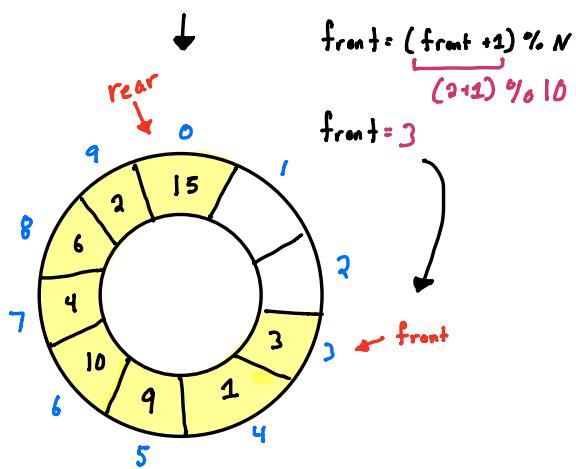
```
if IsEmpty():
    return
else if front == rear:
    front, rear = A[-1]      ~ Q is empty
else:
    front = (front + 1) % N
```

front()

return A[front]



Dequeue()



Example from book: A Python Implementation of a Queue

```

1 class ArrayQueue:
2     """FIFO queue implementation using a Python list as underlying storage."""
3     DEFAULT_CAPACITY = 10      # moderate capacity for all new queues
4
5     def __init__(self):
6         """Create an empty queue."""
7         self._data = [None] * ArrayQueue.DEFAULT_CAPACITY
8         self._size = 0
9         self._front = 0
10
11    def __len__(self):
12        """Return the number of elements in the queue."""
13        return self._size
14
15    def is_empty(self):
16        """Return True if the queue is empty."""
17        return self._size == 0
18
19    def first(self):
20        """Return (but do not remove) the element at the front of the queue.
21
22        Raise Empty exception if the queue is empty.
23        """
24        if self.is_empty():
25            raise Empty('Queue is empty')
26        return self._data[self._front]
27
28    def dequeue(self):
29        """Remove and return the first element of the queue (i.e., FIFO).
30
31        Raise Empty exception if the queue is empty.
32        """
33        if self.is_empty():
34            raise Empty('Queue is empty')
35        answer = self._data[self._front]           Answer is equal to the front index in our Queue list
36        self._data[self._front] = None             # help garbage collection ~ The index of our recently removed item is now "none"
37        self._front = (self._front + 1) % len(self._data) New front of Queue index
38        self._size -= 1                         Size of Queue list
39        return answer                          is reduced by 1.
40
41    def enqueue(self, e):
42        """Add an element to the back of queue."""
43        if self._size == len(self._data):
44            self._resize(2 * len(self._data))       # double the array size
45        avail = (self._front + self._size) % len(self._data) ~ finds available spot in Queue, "the rear"
46        self._data[avail] = e                   ← Places the element in the rear
47        self._size += 1
48
49    def __resize(self, cap):
50        """Resize to a new list of capacity >= len(self)."""
51        old = self._data                      # we assume cap >= len(self)
52        self._data = [None] * cap              # keep track of existing list
53        self._size = 0                        # allocate list with new capacity
54        walk = self._front
55        for k in range(self._size):
56            self._data[k] = old[walk]          # only consider existing elements
57            walk = (1 + walk) % len(old)     # intentionally shift indices
58            self._front = 0                  # use old size as modulus
59            self._size = self._size + 1       # front has been realigned

```

Instances:

- `_data`: is a reference to a `list` instance with a fixed capacity.
- `_size`: is an integer representing the current number of elements stored in the queue (as opposed to the length of the `_data` list).
- `_front`: is an integer that represents the index within `_data` of the first element of the queue (assuming the queue is not empty).

Resizing the Queue

When `enqueue` is called at a time when the size of the queue equals the size of the underlying list, we rely on a standard technique of doubling the storage capacity of the underlying list. In this way, our approach is similar to the one used when we implemented a `DynamicArray` in Section 5.3.1.

However, more care is needed in the queue's `_resize` utility than was needed in the corresponding method of the `DynamicArray` class. After creating a temporary reference to the old list of values, we allocate a new list that is twice the size and copy references from the old list to the new list. While transferring the contents, we intentionally realign the front of the queue with index 0 in the new array, as shown in Figure 6.7. This realignment is not purely cosmetic. Since the modular arithmetic depends on the size of the array, our state would be flawed had we transferred each element to its same index in the new array.

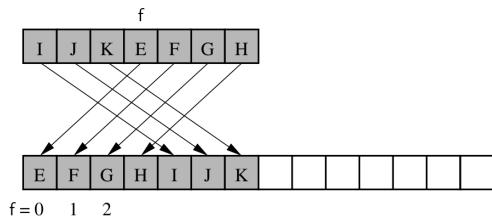


Figure 6.7: Resizing the queue, while realigning the front element with index 0.

How would we reduce the size of the array?

Insert this @ after line 38:

```
if 0 < self._size < len(self._data) // 4:  
    self._resize(len(self._data) // 2)
```

Analyzing the Array-Based Queue Implementation

| Operation | Running Time |
|---------------------------|--------------|
| <code>Q.enqueue(e)</code> | $O(1)^*$ |
| <code>Q.dequeue()</code> | $O(1)^*$ |
| <code>Q.first()</code> | $O(1)$ |
| <code>Q.is.empty()</code> | $O(1)$ |
| <code>len(Q)</code> | $O(1)$ |

*amortized

Table 6.3: Performance of an array-based implementation of a queue. The bounds for enqueue and dequeue are amortized due to the resizing of the array. The space usage is $O(n)$, where n is the current number of elements in the queue.

Example from Code above: