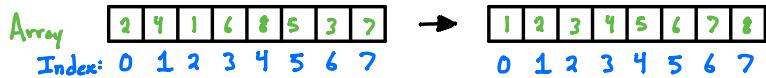
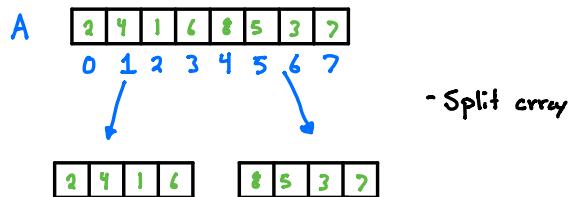


Merge Sort

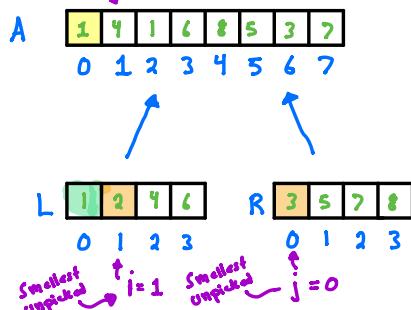


Unsorted

Sorted

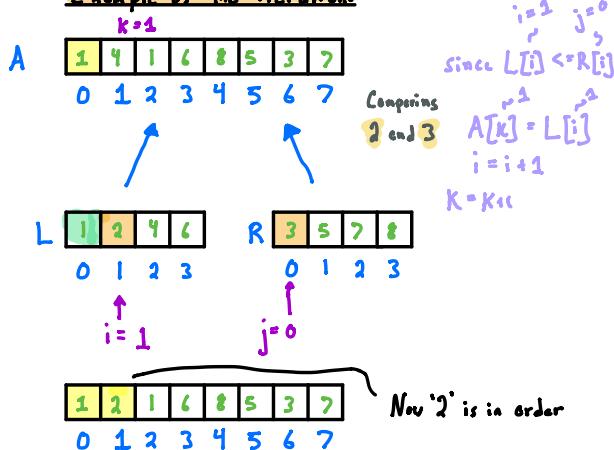


K=1 ~ marks the position that needs to be filled in A.



- Sorted (Merge these to the original array)

Example of the iteration:



Suedo Code:

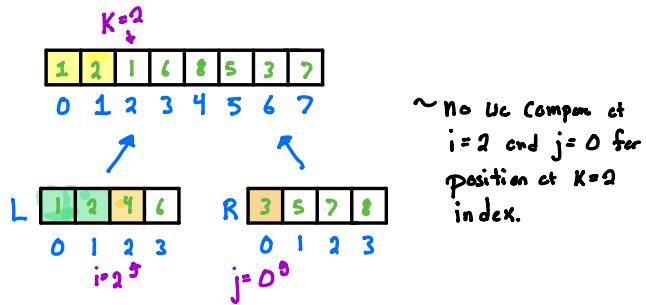
```

def Merge(L, R, A):
    # n L ← Length(L)    List
    # n R ← Length(R)    List
    i = j = k = 0

    while (i < #n L and j < #R):
        if (L[i] <= R[j]):      ~ Computing smallest unprinted in L with the smallest unprinted in R.
            A[k] = L[i]
            i = i+1
        else:
            A[k] = R[j]
            j = j+1
        k = k+1               ← moving to next index in our sorted list

```

next iteration:



~ No we can move on
i=2 and j=0 for
position at $K=2$
index.

What happens when either i or j index is finished first? (are conditional while($i < \#nL$ and $j < \#R$): is false)

```
def Merge(L, R, A):
    # nL ← Length(L)    List
    # nR ← Length(R)    List
    i = j = k = 0
```

while ($i < \#nL$ and $j < \#R$):

```
    if (L[i] <= R[j]):
        A[k] = L[i]
        i = i + 1
    else:
        A[k] = R[j]
        j = j + 1
    k = k + 1
```

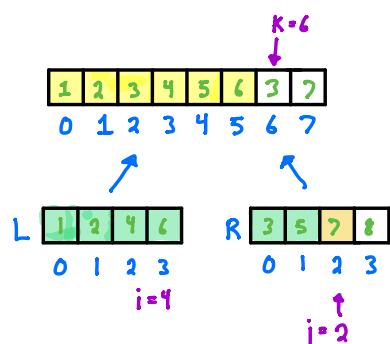
while ($i < \#nL$):

```
A[k] = L[i]
i = i + 1
k = k + 1
```

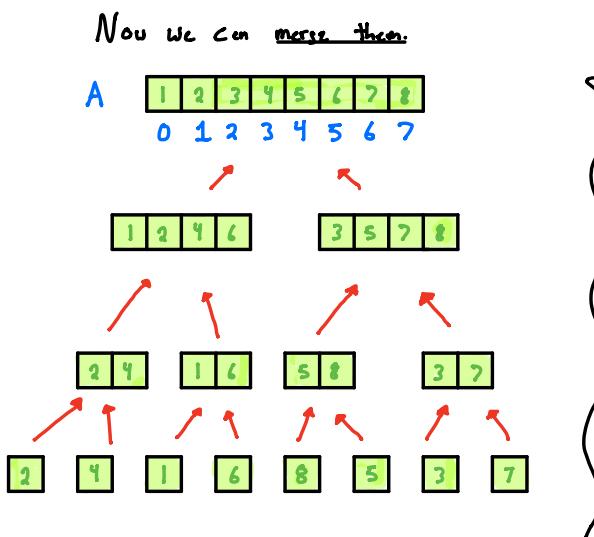
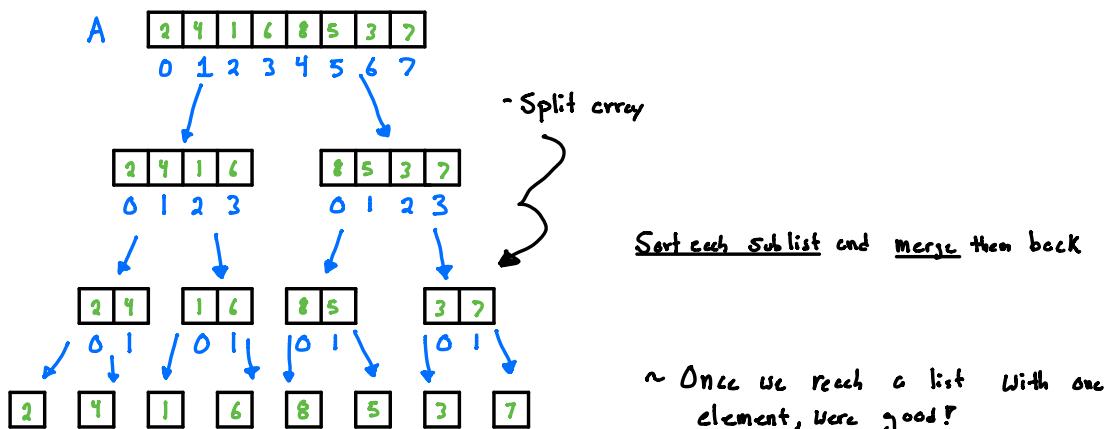
while ($j < \#nR$):

```
A[k] = R[j]
j = j + 1
k = k + 1
```

Once were out of
this while loop only
one while loop at
the bottom will execute



Problem Solved



```
def MergeSort(A):
    n = len(A)
    if n < 2:
        return
    mid = n // 2
    Left = A[0:mid]
    Right = A[mid:n]
    for i in range(0, mid):
        Left[i] = A[i]
    for i in range(mid, n):
        Right[i - mid] = A[i]
```

An array:

2 arrows split original array in L and R halves.

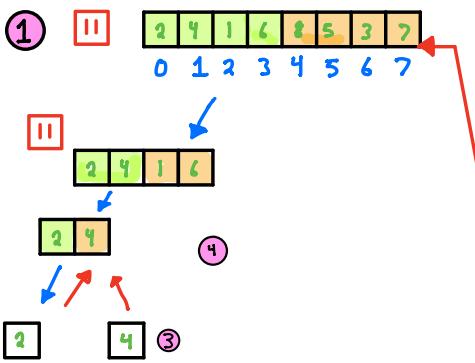
Mergesort(Left)

Mergesort(Right)

Merge(Left, right, A)

We can make a recursive call to solve both Left and Right Lists.

Once both L and R Sublists are sorted, we can make a call to the merge function to merge L and R Sublists into A.



```

def MergeSort(A):
    An array:
    n = length(A)

    if n < 2:      ← Base Condition or the
                    return
    mid = n // 2
    Left = [0 : mid]
    Right = [mid : n]

    ← 2 arrays split original
        array in L and R
        halves.

    for i in range(0:mid):
        Left[i] = A[i]

    for i in range(mid:n):
        Right[i - mid] = A[i]

```

Recursive Call → MergeSort(Left)

③ Second Recursive Call → MergeSort(Right)
Will be made on the Right array

④ When both recursive calls for this particular Sub list with two elements return back, Merge function will be called.

→ We can make a recursive call to solve both Left and Right Lists.

→ Once both L and R Sublists are sorted, we can make a call to the merge function to merge L and R Sublists into A.

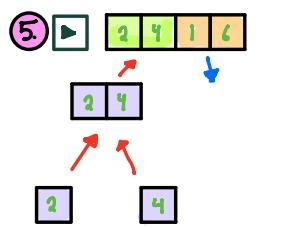
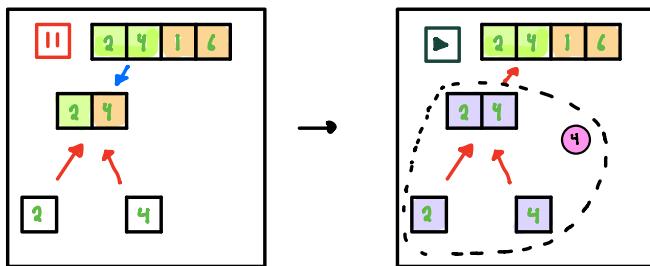
in ① our function call is →
the current array is paused
and the machine says hey,
let me go and finish
this particular function call
and then ill come back
to you. / We keep
splitting the array by
 $n/2$ until our condition
is satisfied ($n < 2$).

② State of execution of the function called with these arrays as arguments are paused.

↙: recursive call

② This array with one element base condition will be true, so this call will exit

- Once $\text{Merge}(\text{Left}, \text{Right}, A)$ is finished the control will return back to the execution of the previous subset $[2, 4, 1, 6]$. (▶)



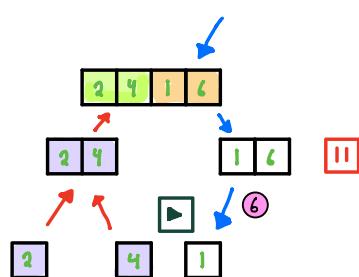
~ Now this sublist will have its Control returned back

- ⑤ : Now this guy will make the second Merge Sort call. It will call Mergesort(right), which will pass in the right array (which was $[1, 6]$), and then were at the top of our def MergeSort(A) function.

~~BIGGEST TAKEAWAY~~

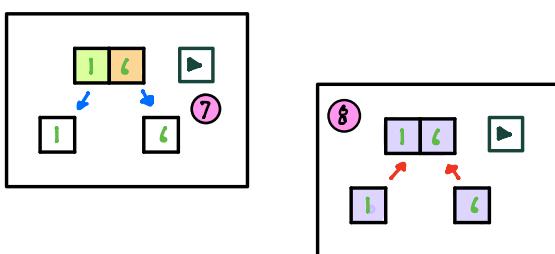
Original Array:

II [2 4 1 6 8 5 3 7]
 0 1 2 3 4 5 6 7



- ⑥ : Now, the array $[1, 6]$ is II and we divide the array, by making another recursive call (Mergesort(Left)).

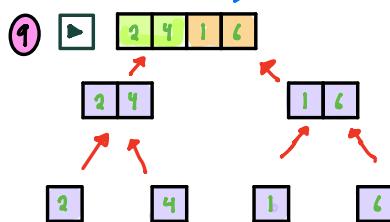
- ⑦ Since the single element is < 2 our Base Condition will make the program to the next line, which will execute the recursive call (Mergesort(Right)) on the right side of the array, which is 6.



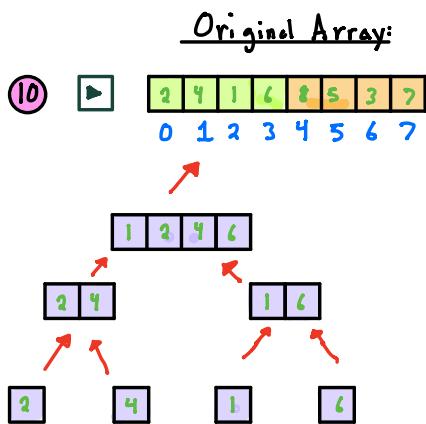
- ⑧ When both recursive calls for this particular sublist with two elements return back, Merge(Left, right, A) will be called.

Original Array:

II	2	4	1	6	8	5	3	7
	0	1	2	3	4	5	6	7

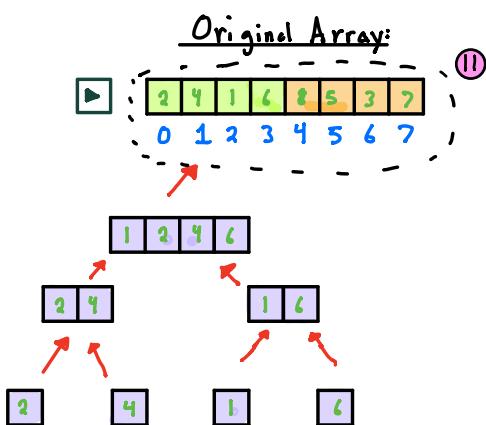


①: Then Control will return back to the array 2,4,1,6 and Merge(left,right,A) will be called



⑩ Once 1,2,4,6 will finish Merge(left,right,A) the Control Will return back to the function call corresponding to the Original array

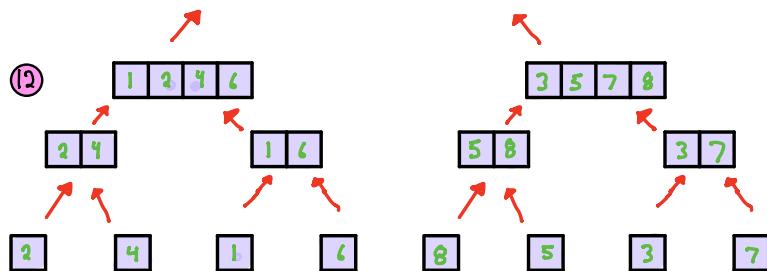
and then this guy



⑪ And then this guy will make another recursive call to do the right side of our Original array.

Original Array:

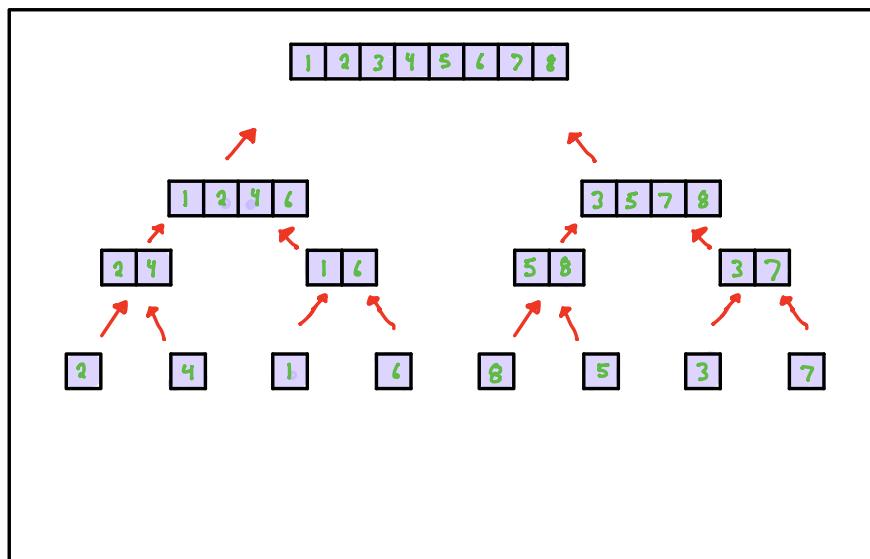
2 4 1 6 8 5 3 7



⑫ Repeat Algorithm on other side!

~ Then `Merge(left,right,A)` will be called for [1, 4, 6] and [3, 5, 7]

- Boom its merged!



Sorted Array Using merge sort