

Commonality Analysis for a Library of Linear Algebraic Equation Solver

Devi Prasad Reddy Guttapati

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Table 1: Revision History

Date	Version	Notes
October 4, 2017	1.0	Initial Draft

1 Reference Material

1.1 Table of Units

This section does not apply to this program family.

1.2 Table of Symbols

The table that follows summarizes the symbols used in this document along with their units. The choice of symbols was made to be consistent with the heat transfer literature and with existing documentation for solar water heating systems. The symbols are listed in alphabetical order.

symbol	unit	description
A	-	known $m \times n$ matrix [Remove text, just use equation environment. —SS]
x	-	n -vector
b	-	m -vector
M_1	-	elementary elimination matrix
L	-	lower triangular matrix
U	-	upper triangular matrix
A^{-1}	-	inverse of matrix
I	-	identity matrix
$ A $	-	determinant of matrix

1.3 Abbreviations and Acronyms

symbol	description
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
PS	Physical System Description
R	Requirement
SRS	Software Requirements Specification
T	Theoretical Model
O	Output

2 Introduction

Many of the relationships in nature are linear, that means their effects are proportional to their causes. For example in Mechanics if we take Newtons second law of motion, $\mathbf{F} = m\mathbf{a}$ says that force is proportional to acceleration and mass is the proportionality constant. For example in Electricity if we take Ohm's Law, $\mathbf{V} = \mathbf{iR}$ voltage across the conductor is proportional to the current flowing through it and resistance is the proportionality constant. These examples show us the importance of linear equations and solving them. In matrix notation the general form of linear equation is

$$\mathbf{Ax} = \mathbf{b}$$

where \mathbf{A} is known $m \times n$ matrix, \mathbf{b} is an m -vector and \mathbf{x} is an n -vector. If \mathbf{x} is known, then such a linear relationship enables us to predict effect \mathbf{b} from cause \mathbf{x} by matrix-vector multiplication $\mathbf{b} = \mathbf{Ax}$.

The most important problem in technical computing is the solution of system linear equations.

2.1 Purpose of Document

The purpose of the document is to describe the methods and process for solving the family of linear algebraic equations. A study on the method for solution of system of linear equations and the problems affecting the effectiveness and efficiency will be detected and correct recommendations will be made. The significance of this document is to make a solution technique for solving family of linear equations easier and to reduce stress on the human brain associated with lots of reasoning when solving linear equation.

This document also describes General System Description, Commonalities, Variabilities.

2.2 Scope of the Family

The scope of the family is limited to the library of linear algebraic equation solvers. If the user gives proper input the linear algebraic equation solver aims to solve the equations and give the correct output.

2.3 Characteristics of Intended Reader

The intended readers who read this document must have basic knowledge about linear algebraic equations and the different methods of solving linear algebraic equations which are typically covered in first and second year Linear Algebra courses . [\[Watch the spacing in your sentences with punctuation. —SS\]](#)

2.4 Organization of Document

The template for Commonality Analysis for scientific computing software is proposed by [Smith \(2006\)](#). The document is organized perfectly step by step right from the introduction to the

appendix by explaining the important concepts like General System Description, Commonalities, Variabilities.

3 General System Description

This section identifies the interfaces between the system and its environment, describes the user characteristics and lists the system constraints.

3.1 System Context

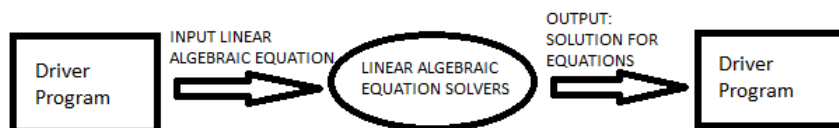


Figure 1: System Context

The figure shows the system context. The user gives the input in the form of linear equations to the solver and the solver aims to give the solution to the equations as the output.

[The user likely makes more sense as program rather than a person. —SS]

- User Responsibilities:

- The main responsibility of the user is to give the appropriate input.
- User must make sure that the input given is error free.
- User must enter the values in matrix form. [Does the user really need to put the data in the correct format? If it isn't in the correct software, the software should be able to detect this. —SS]

- Linear Algebraic Equation Solver Responsibilities:

- The main responsibility of the linear algebraic equation solver is to identify the input which is improper or invalid. [This point shows that your software does check the format, so you don't need the last point in the user responsibility list. —SS]
- Detect data type mismatch, such as a string of characters instead of a floating point number.
- the ultimate responsibility of the linear algebraic equation solver is to solve the equations and to produce the output.

3.2 User Characteristics

The end user of Linear Algebraic Equation Solver should have an understanding of undergraduate Level of linear algebra. [\[What level course? Mathematics is quite standardized, so saying Linear Algebra 1, would be helpful. —SS\]](#)

3.3 System Constraints

There are no system constraints applicable.

4 Commonalities

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the Terminology and Definitions, Data Definitions, Goal Statements and Theoretical Models.

4.1 Problem Description

Linear Algebraic Equation Solver is a software library which is developed to solve linear algebraic equations using numerical methods for linear algebraic equation . This solver is used to solve the linear algebraic equations with different number of variables. As many relationships in nature are linear, it will be very handy for students to solve linear algebraic equations.

4.2 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements:

- \mathbf{A} is a known $m \times n$ matrix
- \mathbf{b} is an m -vector
- \mathbf{x} is an n -vector
- \mathbf{A}^{-1} is the inverse of the matrix \mathbf{A}
- $\text{rank}(\mathbf{A}) = n$ the rank of a matrix is the maximum number of linearly independent rows or columns it contains. [\[the rank of a matrix is not always \$n\$. —SS\]](#)
- $\det(\mathbf{A})$ is determinant of matrix \mathbf{A}

[The terminology you have listed is mostly a repetition of symbols you are using elsewhere. Terminology is more for definitions of terms. You could define terms like singular, condition number etc. Your definition of rank seems like an appropriate item to list here. The information above is a better fit for the list of symbols. —SS]

4.3 Data Definitions

Number	DD1
Label	Matrix Representation of the Linear Algebraic Equation
Symbol	$\mathbf{Ax} = \mathbf{b}$
Equation	$\begin{cases} ax_1 + bx_2 = b_1 \\ cx_1 + dx_2 = b_2 \end{cases}$
Description	<p>\mathbf{A} is a known $m \times n$ matrix that is $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$.</p> <p>$\mathbf{b}$ is an m-vector that is $\begin{bmatrix} b_1 \\ b_2 \end{bmatrix}$.</p> <p>$\mathbf{x}$ is an n-vector that is $\begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$. [Your definitions are just for a two by two matrix. You should explain what it means to have an $m \times n$ matrix. —SS]</p>
Source	Scientific Computing, An Introductory Survey, Second Edition by MICHEL [spell check —SS] T. HEATH, Chapter 2. [Use BibTeX for this and put the reference in your list of references —SS]
Ref. By	[IM1], [IM2], [T2], [T1], [A2], [A3] [I've had a look at some of these reference by items and they don't actually have references. You have to actually use the references to put this in. —SS]

Number	DD2
Label	Inverse of a Matrix
Symbol	\mathbf{A}^{-1}
Equation	$\mathbf{A}\mathbf{A}^{-1} = \mathbf{A}^{-1}\mathbf{A} = \mathbf{I}$
Description	<p>\mathbf{A} is a known $m \times n$ matrix.</p> <p>\mathbf{A}^{-1} is the inverse of matrix \mathbf{A} .</p> <p>\mathbf{I} is an Identity matrix . [You should define the identity matrix somewhere. It would be a good data definition. —SS]</p>
Source	Scientific Computing, An Introductory Survey, Second Edition by MICHEL T. HEATH, Chapter 2.
Ref. By	[IM1], [IM2], [DD3], [T2], [A4]

Number	DD3
Label	Determinant of a Matrix
Symbol	$ A $
Equation	$ A = \sum_{i=1}^k a_{ij}C_{ij}$
Description	<p>A is the determinant of matrix \mathbf{A}.</p> <p>\mathbf{C}_{ij} is the cofactor of a_{ij} defined by $\mathbf{C}_{ij} = (-1)^{i+j}\mathbf{M}_{ij}$.</p> <p>\mathbf{M}_{ij} is the minor of matrix \mathbf{A} formed by eliminating row i and column j from \mathbf{A}.</p>
Source	http://mathworld.wolfram.com/Determinant.html
Ref. By	[IM1], [IM2], [DD2], [T2], [A4]

Number	DD4
Label	Rank of a Matrix
Symbol	rank(A)
Equation	rank(A) $\leq \min(m, n)$
Description	<p>rank(A) is the rank of matrix A.</p> <p>We assume that A is an $m \times n$ matrix and we define the linear map f by $f(x) = Ax$.</p> <p>The rank of an $m \times n$ matrix is a nonnegative integer and cannot be greater than either m or n . [You haven't really defined rank. —SS]</p>
Source	https://www.cliffsnotes.com/study-guides/algebra/linear-algebra/real-euclidean-vector-spaces/the-rank-of-a-matrix
Ref. By	[IM1], [IM2], [T2], [A4]

4.4 Goal Statements

GS1: Given the general linear algebraic equation problem which is represented by $Ax = b$. The initial values are A and B. The input which are the coefficients, are entered in a matrix form. If the vector b of effects is known then it would likely be able to determine the corresponding vector x of cause.

4.5 Theoretical Models

This section focuses on the general equations and laws that Linear Algebraic Equation Solver is based on.

Number	T1
Label	General Linear Algebraic Equation
Equation	$\mathbf{Ax} = \mathbf{b}$
Description	A linear transformation between two finite dimensional vector spaces is represented by a matrix. In matrix-vector notation, a system of linear algebraic equations has the form $\mathbf{Ax} = \mathbf{b}$ where \mathbf{A} is known $m \times n$ matrix, \mathbf{b} is an m -vector and \mathbf{x} is an n -vector. If \mathbf{x} is known, then such a linear relationship enables us to predict effect \mathbf{b} from cause \mathbf{x} by matrix-vector multiplication $\mathbf{b} = \mathbf{Ax}$. The linear system will also enable us to "reverse engineering", [Use "quote" to get correct quotation marks —SS] if we know the vector \mathbf{b} of effects, we can be able to determine the corresponding vector \mathbf{x} of cause.
Source	http://www.sciencedirect.com/science/article/pii/S0377042794903026
Ref. By	[IM1], [IM2], [A2], [A3], [C1]

[You should introduce the assumption that A is a square matrix here. There is no reason to continue with the more general $m \times n$ case. (You should also add an explicit assumption that A is square. This is also something you should say in the scope section.) —SS]

Number	T2
Label	Existence and Uniqueness
Equation	$\mathbf{Ax} = \mathbf{b}$ An $n \times n$ matrix \mathbf{A} is said to be nonsingular if it satisfies any of the following equivalent conditions: <ol style="list-style-type: none"> 1. \mathbf{A} has an inverse (there is a matrix, denoted by \mathbf{A}^{-1}, such that $\mathbf{AA}^{-1} = \mathbf{A}^{-1}\mathbf{A} = \mathbf{I}$, the identity matrix). 2. Determinant of (\mathbf{A}) is not equals to 0 3. $\text{rank}(\mathbf{A}) = n$ (the rank of a matrix is the maximum number of linearly independent rows or columns it contains). [If you have a list use the itemize or enumerate environments in LaTeX. —SS]
Description	The existence of a solution to a system of linear equations $\mathbf{Ax} = \mathbf{b}$ depend on whether the matrix \mathbf{A} is singular or nonsingular. If the matrix \mathbf{A} is nonsingular, then its inverse \mathbf{A}^{-1} exists, and the system $\mathbf{Ax} = \mathbf{b}$ always has a unique solution $\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$ regardless of the value for \mathbf{b} . If the matrix \mathbf{A} is singular, then the number of solutions is determined by the right hand side vector \mathbf{b} .
Source	http://www.sciencedirect.com/science/article/pii/S0377042794903026
Ref. By	[IM1], [IM2], [DD2], [DD3], [DD4], [A4], [C1]

[\[This shouldn't be a separate theoretical model. It is part of the first model. The potential solutions for a linear system of equations are a unique solution, an infinite number of solutions or no solution. You should then reference definitions that define what rank, singular etc. mean. —SS\]](#)

5 Variabilities

The instance models that govern Linear Algebraic Equation Solver are presented in Subsection 4.2.5. The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.

5.1 Instance Models

This section transforms the problem defined in Section 4.1 into one which is expressed in mathematical terms.

Number	IM1
Label	Gaussian Elimination Method for solving Linear Algebraic Equations
Input	A, b
Output	M₁, L, U, x [The output should only be x and an element from enumerated type that indicates whether the matrix is singular or not. —SS]
Description	<p>A is a known $m \times n$ matrix.</p> <p>x is an n-vector.</p> <p>b is an m-vector.</p> <p>M₁ is an elementary elimination matrix.</p> <p>L is lower triangular matrix.</p> <p>U is upper triangular matrix.</p>
Sources	http://www.sciencedirect.com/science/article/pii/S0377042794903026
Ref. By	[A1], [A2], [A3], [A4], [A5], [A6], [A7]

[You are really inconsistent with the notation. At some points you use bold face for matrices and vectors, other times you do not. You also are not consistent in putting your variables and equations in the LaTeX equation environment. —SS]

Derivation of Gaussian Elimination Method

It is fairly simple matter to reduce a general linear system $\mathbf{Ax} = \mathbf{b}$ to upper triangular form. We first choose an elementary elimination matrix \mathbf{M}_1 with the first diagonal entry \mathbf{a}_{11} as pivot, so that the first column of \mathbf{A} becomes zero below the first row when premultiplied by \mathbf{M}_1 . All the remaining columns of \mathbf{A} , as well as right-hand-side vector \mathbf{b} , must also be multiplied by \mathbf{M}_1 , so the new system becomes $\mathbf{M}_1\mathbf{Ax} = \mathbf{M}_1\mathbf{b}$.

Next we use the second diagonal entry as pivot to determine a second elementary elimination matrix \mathbf{M}_2 that annihilates all of the entries of the second column of the new matrix, $\mathbf{M}_1\mathbf{A}$, below the second row. Again, \mathbf{M}_2 must be applied to the entire matrix and right-hand-side vector, so that we obtain the further modified linear system $\mathbf{M}_2\mathbf{M}_1\mathbf{Ax} = \mathbf{M}_2\mathbf{M}_1\mathbf{b}$. Note that the first column of the matrix $\mathbf{M}_1\mathbf{A}$ is not effected by \mathbf{M}_2 because all of its entries are zero in the relevant rows. If we define the matrix $\mathbf{M} = \mathbf{M}_{n-1}\dots\mathbf{M}_1$, then the transformed the linear system is

$$\mathbf{MAx} = \mathbf{M}_{n-1}\dots\mathbf{M}_1\mathbf{Ax} = \mathbf{M}_{n-1}\dots\mathbf{M}_1\mathbf{b} = \mathbf{Mb}$$

is upper triangular and can be solved by back-substitution to obtain the solution to the original linear system $\mathbf{Ax} = \mathbf{b}$.

The process we have just described is known as Gaussian elimination. It is also known as LU factorization or LU decomposition because it decomposes the matrix \mathbf{A} into product of a unit lower triangular matrix, \mathbf{L} , and the upper triangular matrix, \mathbf{U} . To see this, recall that the product $\mathbf{L}_k\mathbf{L}_j$ is unit lower triangular if $k < j$, so that [\[spell check! —SS\]](#)

$$\mathbf{L} = \mathbf{M}^{-1} = (\mathbf{M}_{n-1}\dots\mathbf{M}_1)^{-1} = \mathbf{M}_1^{-1}\dots\mathbf{M}_{n-1}^{-1} = \mathbf{L}_1\dots\mathbf{L}_{n-1}$$

is unit lower triangular. We have already seen that, by design, the matrix $\mathbf{U} = \mathbf{MA}$ is upper triangular. Therefore, we have expressed \mathbf{A} as a product

$$\mathbf{A} = \mathbf{LU}$$

where \mathbf{L} is unit lower triangular and \mathbf{U} is upper triangular. Given such a factorization, the linear system $\mathbf{Ax} = \mathbf{b}$ can be written as $\mathbf{LUx} = \mathbf{b}$ and hence can be solved by first solving the lower triangular system $\mathbf{Ly} = \mathbf{b}$ by forward-substitution, then the upper triangular matrix $\mathbf{Ux} = \mathbf{y}$ by back-substitution.

In solving a linear system $\mathbf{Ax} = \mathbf{b}$, the necessary transformation of the right-hand-side vector \mathbf{b} could be included as a part of LU factorization process, or it could be done as a separate step to solve the lower triangular system $\mathbf{Ly} = \mathbf{b}$ after \mathbf{L} has been obtained. In either case, back-substitution for upper triangular matrix is then used to solve the upper triangular system $\mathbf{Ux} = \mathbf{y}$ to obtain the solution \mathbf{x} .

[\[The above text is plagiarized. You cannot take someone else's words and present them as your own without citation. The above is almost a direct quote from Heath, but you don't cite that resource here. Please be very careful to not do this. For the current project, it would have been fine to not produce all of these details. You could give a high level overview of the algorithm and simply refer the reader to the Heath textbook for the details. —SS\]](#)

Number	IM2
Label	Gauss-Jordan Elimination Method for solving Linear Algebraic Equations
Input	A, b
Output	x
Description	The algorithm of Gauss-Jordan transforms matrix A by means of elementary transformations into a diagonal matrix (or into the identity matrix), and performs similar transformations to the right-hand side vector b in order to find the solution vector x.
Sources	http://www.sciencedirect.com/science/article/pii/S0377042794903026
Ref. By	[A1], [A2], [A3], [A4], [A5], [A6], [A7]

Derivation of Gauss-Jordan Elimination Method

The transformation of A is achieved in n successive elimination steps. Starting from $\mathbf{A}^{(1)} = \mathbf{A}$, the k^{th} elimination step, $k = 1, \dots, n$, transforms $\mathbf{A}^{(k)}$ into $\mathbf{A}^{(k+1)}$ such that the off-diagonal elements in the k^{th} column, not only below but also above the main diagonal, become zero. Thus, after n steps the diagonal matrix $\mathbf{D} = \mathbf{A}^{(n+1)}$ is obtained. The k^{th} elimination step can be formulated as follows. The pivot of the k^{th} elimination step is $\delta_k = \mathbf{A}_{k,k}^{(k)}$, as in Gaussian elimination. Let \mathbf{g}_k , be the column vector given by

$$\mathbf{g}_k = \mathbf{A}^{(k)} \mathbf{e}_k - \delta_k \mathbf{e}_k$$

therefore the vector obtained from the k^{th} column of $\mathbf{A}^{(k)}$ by replacing its diagonal element by zero. Then the k^{th} elimination step, to introduce the required zeros in the k^{th} column of the matrix, consists of premultiplying $\mathbf{A}^{(k)}$ by the matrix

$$\mathbf{T}_k = \mathbf{I} - \delta_k^{-1} \mathbf{g}_k \mathbf{e}_k^T$$

In other words, $\mathbf{A}^{(k+1)}$ is obtained from $\mathbf{A}^{(k)}$ by means of the rank-one modification

$$\mathbf{A}^{(k+1)} = \mathbf{T}_k \mathbf{A}^{(k)} = \mathbf{A}^{(k)} - \delta_k^{-1} \mathbf{g}_k \mathbf{e}_k^T$$

The corresponding transformation of right-hand side vector b proceeds as follows. Starting from $\mathbf{b}^{(1)} = \mathbf{b}$, the k^{th} elimination step, $k = 1, \dots, n$, transforms $\mathbf{b}^{(k)}$ into $\mathbf{b}^{(k+1)}$ according to

$$\mathbf{b}^{(k+1)} = \mathbf{T}_k \mathbf{b}^{(k)} = \mathbf{b}^{(k)} - \delta_k^{-1} \mathbf{b}_k^{(k)} \mathbf{g}_k,$$

which is a vector update operation.

Thus, the given linear system is transformed into the equivalent system $\mathbf{D}\mathbf{x} = \mathbf{y}$, which is easily solved by calculating

$$\mathbf{x} = \mathbf{D}^{-1}\mathbf{y}.$$

[More plagiarism. This is not okay! You might not previously have known how serious this is, but going forward, please remember that you cannot do this. The text you provided comes directly from “Parallel algorithms for solving large linear systems” by Dekker et al. You do not even cite the article. You might have a feeling that you need all of this detail in the SRS, but you do not. If you aren’t focusing on a variability in the algorithm, you should be able to just give a high level overview and then point to the appropriate external reference. I’m going to assume that the current mistake was a misunderstanding, but if this happens in the future, I will have to consider it a case of Academic Dishonesty. If you have any doubts going forward, please ask me. —SS]

5.2 Assumptions

This section simplifies the original problem and helps in developing the theoretical model by filling in the missing information for the physical system. The numbers given in the square brackets refer to the theoretical model [T], general definition [GD], data definition [DD], instance model [IM], or likely change [LC], in which the respective assumption is used.

A1: It is assumed that user will not declare the method by which the linear algebraic equation is solved.

[IM1], [IM2].

[Remember that the user is a driver program. The driver should be able to select the algorithm that is desired. I don’t think there is any reason to not make the algorithm choice up to the caller. —SS]

A2: The entry of values for A, b will be of the explicit form such that $Ax = b$ as described.

[T1]. [IM1], [IM2]

[This isn’t really an assumption. You are just restating the requirements. Your software should be able to detect if the inputs are not in the correct format. —SS]

A3: it is assumed that the values for A, b are entered in matrix form.

[IM1], [IM2], [T2], [T1], [DD2], [DD3], [DD4], [GS1]

[The software can check this; you don’t need to assume it. —SS]

A4: It is assumed that the entered matrix A is non-singular.

[IM1], [IM2], [A2], [DD2], [GS1]

[You shouldn't really have to assume this. If the matrix is singular, the solver will fail and you can tell the user that the matrix is ill-conditioned. (You likely won't know whether it is singular, or just close to singular, but for our purposes this is fine.) —SS]

A5: It is assumed that the entry of values for A, b will not have any complex numbers.

[IM1], [IM2], [T2], [T1], [DD2], [DD3], [DD4], [GS1]

[This is not the place to say the type of A. The type is not an assumption, but part of the requirements. Really it is a scope decision. —SS]

A6: It is assumed that the entry of values for A is from the set of \mathbb{R} .

[IM1], [IM2], [T2], [T1]

[Same assumption as the previous, but said a different way. Same comment as above applies. —SS]

A7: It is assumed that the entry of values for A is from the set of \mathbb{R} .

[IM1], [IM2], [T2], [T1]

[The final assumptions are the same assumption twice. —SS]

5.3 Calculation

C1: Check the inputs if they satisfy the input assumptions.

[GS1], [A2], [A3], [A5], [A6], [A7], [T2], [T1], [IM1], [IM2]

C2: Perform the linear algebraic solver model when the user calls the program.

[GS1], [A2], [A3], [A5], [A6], [A7], [T2], [T1], [IM1], [IM2]

[The first variability is related to input, not calculation. —SS] [Your calculation variabilities are the choice between IM1 and IM2. —SS]

5.4 Output

Not Applicable

[Why not? Couldn't you have an output option of writing the values to a file, instead of to memory? Your output might include the residual, or it might not. —SS]

6 Traceability Matrices and Graphs

The purpose of the traceability matrices is to provide easy references on what has to be additionally modified if a certain component is changed. Every time a component is changed, the items in the column of that component that are marked with an “X” should be modified as well. Table 2 shows the dependencies of theoretical models, data definitions, and instance models with each other. Table 3 shows the dependencies of theoretical models, data definitions, instance models, and likely changes on the assumptions..

	DD1	DD2	DD3	DD4	T1	T2	IM1	IM2
DD1					X	X	X	X
DD2			X			X	X	X
DD3		X				X	X	X
DD4						X	X	X
T1							X	X
T2							X	X
IM1								
IM2								

Table 2: Traceability Matrix Showing the Connections Between Items of Different Sections

	A1	A2	A3	A4	A5	A6	A7	C1	C2
GS1			X	X	X			X	X
DD1				X					
DD2			X		X				
DD3			X		X				
DD4			X		X				
T1		X	X		X	X	X	X	X
T2			X		X	X	X	X	X
IM1	X	X	X	X	X	X	X	X	X
IM2	X	X	X	X	X	X	X	X	X

Table 3: Traceability Matrix Showing the Connections Between Assumptions and Other Items

References

Spencer Smith. Systematic development of requirements documentation for general purpose scientific computing software. In *Requirements Engineering, 14th IEEE International Conference*, pages 209–218. IEEE, 2006.

[You should have more references than just this. —SS]

[Your document would be improved with explicit type information. To start with, simply add this information to the table of symbols. After this, you should look for other places where the type information would be helpful. —SS]

[You would have been better off with a simpler document. A generalized version of what you presented in class is better than trying to “fake” your way through derivation of different algorithms. —SS]