

Question 1.

Write an algorithm beautiful(A, n)

Input : An integer array with n elements such that the best-case running time is equal to the worst-case running time. Write the algorithm and give your analysis to justify your claim.

```
public static int beautiful(int[] A, int n){
    int sum = 0;
    for (int i = 0; i < n; i++) {
        sum += A[i];
    }
    return sum;
}
```

Explanation: The best-case and worst-case running times of the beautiful function are the same because the function always iterates through all n elements of the array, regardless of the array's content. For every element, the function performs a constant-time operation (adding it to the sum), meaning the time complexity is $O(n)$ in both cases. There are no conditions that would cause early termination or skipping any elements, ensuring that the algorithm consistently processes the entire array.

Question 2

Order them based on their complexity.

2^n , $2^{(2n)}$, $2^{(n+1)}$, $2^{(2^n)}$

Ans: 2^n , $2^{(n+1)}$, $2^{(2n)}$, $2^{(2^n)}$

Question 3

Mention one algorithm you know for each of the time complexities listed.

Ans:

$O(1)$ = Accessing Array Index

$O(\log n)$ = Binary Search

$O(n)$ = Looping through an array

$O(n \log n)$ = Merge Sort

$O(n^2)$ = Bubble Sort

$O(n^3)$ = Using 3 loops to find all possible combinations of 3 element sets of n elements.

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$O(2^n)$ = Using recursion to find fibonacci number of n

Question 4

Apply Master Theorem and determine the time complexity of fib(n) shown in Lesson 2. If you cannot apply Master Theorem please give detailed explanation.

Ans: Master Theorem cannot be used for fib(n) shown in lesson 2 because in order to use this formula there needs to be recurrences that arise from Divide-And-Conquer algorithms. For fib(n) in lesson 2 it is just decreasing numbers by 1 and 2 for each recursive call. For the Master formula to work it needs to divide n elements to equal parts.

$$T(n) = \begin{cases} d & \text{if } n = 1 \\ aT(\lceil \frac{n}{b} \rceil) + cn^k & \text{otherwise} \end{cases}$$

b in the above formula represents a number to equally divided parts and it does not work for Fibonacci recursive functions.