

Day:

Date: / /

$$8^{\log n} T\left(\frac{n}{2^{\log n}}\right) + (2^{\log n} - 1)n^2$$

$$8^{\log n} \cdot T\left(\frac{n}{2^{\log n}}\right) + (2^{\log n} - 1)n^2$$

$$n \log^8 : T\left(\frac{n}{n \log^2}\right) + (n^{\log^2} - 1)n^2$$

$$n^3 T\left(\frac{n}{n}\right) + (n-1)n^2$$

$$n^3 T(1) + n^3 - n^2$$

$$= n^3 + n^3 - n^2 = 2n^3 - n^2 = O(n^3)$$

Strassen's Multiplication:

1. Reduce No of Multiplication :  $e = 7$

$$2. \quad P = (A_{11} + A_{22})(B_{11} + B_{22}) \quad S = A_{22}(B_{21} - B_{11})$$

$$Q = (A_{21} + A_{22}) \cdot B_{11} \quad T = (A_{11} + A_{12})B_{22}$$

$$R = A_{11}(B_{12} - B_{22}) \quad U = (A_{22} - A_{11}) \cdot (B_{11} + B_{12})$$

$$V = (A_{12} - A_{22})(B_{21} + B_{22})$$

$$C_{11} = P + S - T + V$$

$$C_{21} = Q + S$$

$$C_{12} = R + T$$

$$C_{22} = P + R - Q + U$$

$$T(n) = 7T\left(\frac{n}{2}\right) + n^2 \rightarrow O(n^{\log 7}) = O(n^{2.81})$$

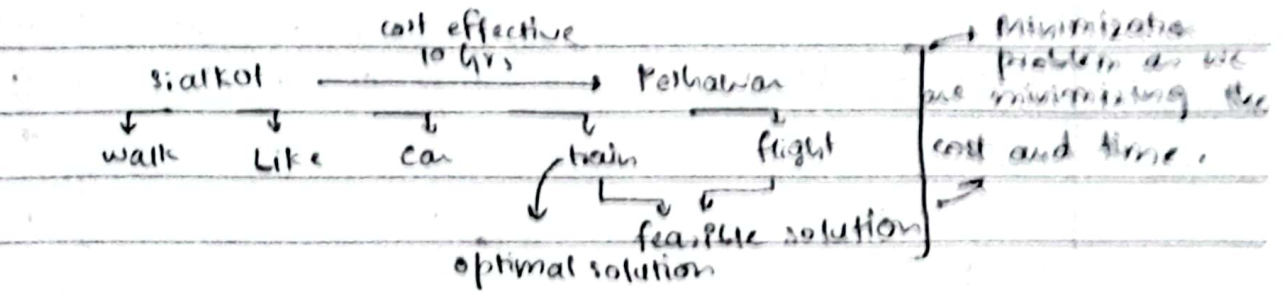
Greedy Paradigm Approach:

1. a design for solving a problem.
2. used for optimization problem  $\rightarrow$  (i) Maximisation (ii) Minimization
3. It has objective and constraints.
4. Solution which meets the constraints to complete objective is Feasible solution.
5. Optimal solution will always be 1.

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Day:

Date: / /



1. Dynamic Programming
  2. Branch and Bound
- can also be used for optimal solution.

o/s. Knapsack Problem

fractional Knapsack Problem

→ Knapsack Problem:

	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$	
objects :	1	2	3	4	5	6	7	11 - 4 = 11
Profit :	10	5	15	7	6	18	3	11 - 7 = 6
weight :	2	3	5	7	1	4	1	

constraints: Do not exceed the capacity of Bag = 15kg

objective: Gives maximum Profit.

$P/w$

	5	1.67	3	1	6	4.5	3
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Bag capacity =  $m = 15$

$$m - 1 = 14 \quad 2 - 20 = 14 - 2 = 12 \quad 12 - 8 = 8 \quad 8 - 5 = 3 \quad 3 - 1 = 2$$

$$2 - 20 = 0$$

$$x_i w_i = (1 \times 2) + (2/3 \times 3) + (1 \times 5) + (0 \times 7) + (1 \times 1) + (1 \times 4) + (1 \times 1)$$

$$x_i w_i = 2 + 2 + 5 + 0 + 1 + 4 + 1$$

$$x_i w_i = 15$$

$$\text{constraint} \rightarrow \sum x_i w_i \leq m \quad \because m = 15 \text{ kg}$$

$$\text{Profit} = x_i P_i = (1 \times 10) + (2/3 \times 5) + (1 \times 15) + (0 \times 7) + (1 \times 6) + (1 \times 18) + (1 \times 3)$$

$$x_i P_i = 10 + 10/3 + 15 + 0 + 6 + 18 + 3$$

$$x_i P_i = 55.3$$

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Day:

Date: / /

Based on profit:

	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$
	1	0	1	$4/7$	0	1	0

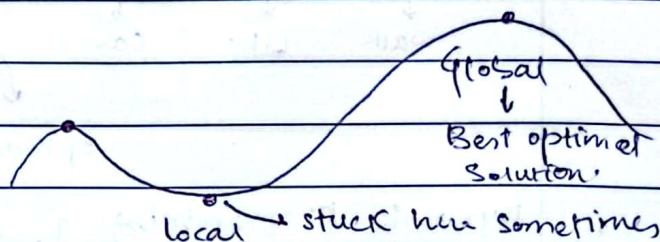
$$m = 15$$

$$15 - 4 = 11$$

$$11 - 5 = 6$$

$$6 - 2 = 4$$

$$4 - 4 = 0$$



$$x_i P_i = (1 \times 10) + (0) + (1 \times 18) + \left(\frac{4}{7} \times 7\right) + (0) + (1 \times 18) + (0)$$

$$= 10 + 18 + 4 + 18$$

$$= 47 \text{ Am}$$

$$\begin{array}{r} 1 \\ 2 \ 9 \\ 1 \ 8 \\ \hline 4 \ 7 \end{array}$$

Previous approach on the basis of weight is more optimal for maximizing profit

$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$
1	1	$4/8$	0	1	1	1

$$m = 15$$

$$15 - 1 = 14$$

$$14 - 1 = 13$$

$$13 - 2 = 11$$

$$11 - 3 = 8$$

$$8 - 4 = 4$$

$$4 - 4 = 0$$

$$x_i P_i = (1 \times 10) + (1 \times 7) + \left(\frac{4}{8} \times 12\right) + (0) + (1 \times 6) + (1 \times 18) + (1 \times 3)$$

$$= 10 + 7 + 12 + 6 + 18 + 3$$

$$= 54$$

$$\begin{array}{r} 2 \\ 3 \ 6 \\ 1 \ 8 \\ \hline 2 \ 4 \end{array}$$

Hello guys

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Day:

Date: / /

Page No. /

New

Job sequencing with deadlines :

Jobs J	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>	J <sub>5</sub>
Profit P	20	15	10	5	1
Deadline D	2	2	1	3	3

$$\textcircled{2} \quad \underline{J_2} \quad \underline{J_1} \quad \underline{J_4} \quad \underline{J_3} \quad \underline{J_5}$$

$$20 + 15 + 5 = 40$$

Job	slots	solution	Profit
J <sub>1</sub>	[1, 2]	{J <sub>1</sub> }	20
J <sub>2</sub>	[0, 1][1, 2]	{J <sub>1</sub> , J <sub>2</sub> }	20 + 15
J <sub>3</sub>	[0, 1][1, 2]	{J <sub>1</sub> , J <sub>2</sub> }	20 + 15
J <sub>4</sub>	[0, 1][1, 2][2, 3]	{J <sub>1</sub> , J <sub>2</sub> , J <sub>3</sub> }	20 + 15 + 5
J <sub>5</sub>	[0, 1][1, 2][2, 3]	{J <sub>1</sub> , J <sub>2</sub> , J <sub>3</sub> }	20 + 15 + 5

- 1) We can't Backtrack in Greedy Algorithm.
- 2) We may get stuck in Local minima in Greedy.

Activity Selection:

→ Given activities (lectures) and one room, Now schedule as many activities as possible, such that they do not conflict each other.

Hehehehehehe

Hello guys

Kia?

Prince

Bad boy

Ignore

us ne baat ki the kal

Day:

Date: / /

	i	1	2	3	4	5	6	7	8	9
	<del>S<sub>i</sub></del>	2	2	4	1	5	8	9	11	13
	F <sub>i</sub>	3	5	7	8	9	10	11	14	16
duration	d <sub>i</sub>	1	3	3	7	4	2	2	3	3
By difference	App 1	✓	X	✓	X	X	✓	X	✓	X
By low Ending Time	App 2	✓	X	✓	X	X	✓	X	✓	X
	Plan St	X			X	✓	X	✓	X	✓
	Total subsets	$= 2^9$								

Solution:

 $\{a_1, a_3, a_6, a_8\} \rightarrow \text{optimal Solution?}$ 

it will be difficult to achieve optimal solution if there is more conflicts

i	=	1	2	3
S <sub>i</sub>	=	4	1	5
F <sub>i</sub>	=	6	8	10
d <sub>i</sub>	=	2	4	5

~~✓~~  
~~X~~  
~~X~~  
 Greedy Solution =  $\{a_1\}$

App 1

optimal Solution =  $\{a_2, a_3\}$

Approach 2

1. Min Duration X
2. Min start time X
3. Min End Time ✓  $\rightarrow$  optimal Solution.
4. Max Start time

Looking for

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Day:

Date: / /

Activity Selection Algorithm:

$\therefore S \ \& \ F$  are array  
start      finish

Greedy A/C  $(S, F, n)$

$\therefore n = \text{no. of activities}$

// sort activities in both arrays by finish time in ascending order.

add  $A[0]$  to  $A$   $\hookrightarrow (n \log n)$

for  $(i = 1 \text{ to } i = n)$   $\rightarrow n$

$k = 1$

~~for  $k = 2$  to  $n$~~

if  $S[i] \geq F[k]$

add  $E[i]$  to  $A$

$k = i$

Time complexity =  $n + n \cdot \log n = O(n \cdot \log n)$

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