

CS 313 - ADA

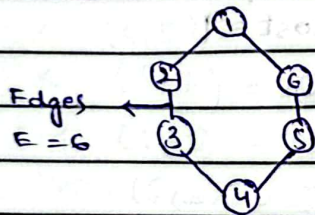
LECTURE # 16

13-12-2023

WEDNESDAY

→ Greedy Algorithm

Minimum Cost Spanning Tree
 ↳ a subgraph of graph



$$G = (V, E)$$

 $V \rightarrow$ Set of vertices / nodes

 $E \rightarrow$ Set of Edges

► Vertices of the

graph with $|V| = 6$

$$V = \{1, 2, 3, 4, 5, 6\}$$

Edges and no cycle.

$$E = \{(1, 2), (2, 3), (3, 4), (4, 5), (5, 6), (6, 1)\}$$

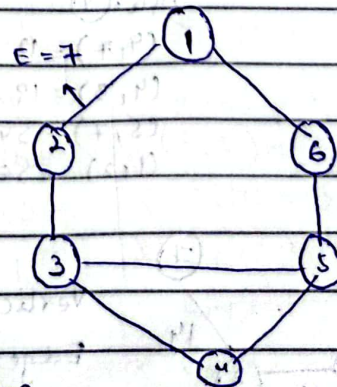
$$6C_5 = 6$$

 \rightarrow Out of 6 Edges we have to choose 5.

$$6! = 6 \times 5! = 6 \times 6 = 6$$

$$5!(6-5)! = 5!1! = 1$$

$$nC_r = \frac{n!}{r!(n-r)!}$$

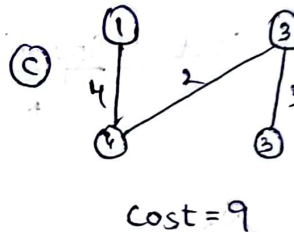
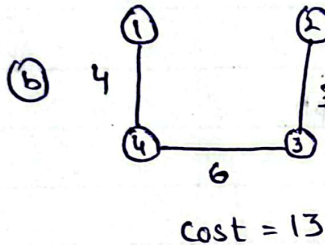
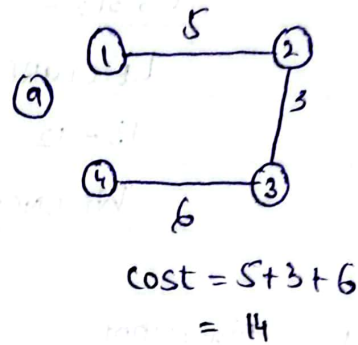
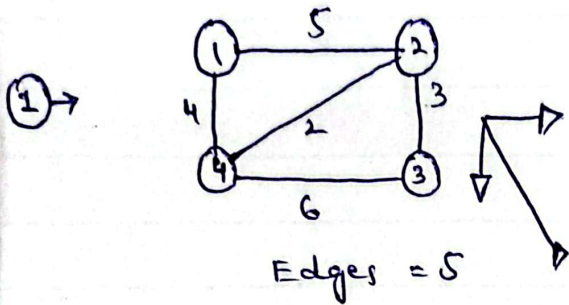


$$7C_5 = 2$$

↓
 represents
 no. of cycles

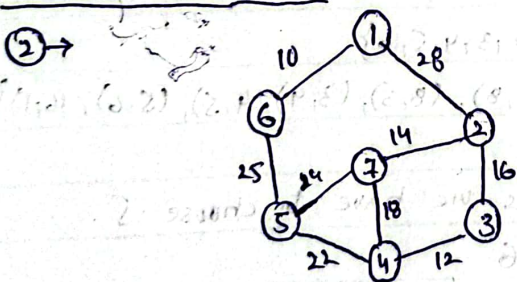
$$7C_5 - 2 = \frac{7!}{5!(7-5)!} - 2$$

→ Minimum Cost Spanning Tree

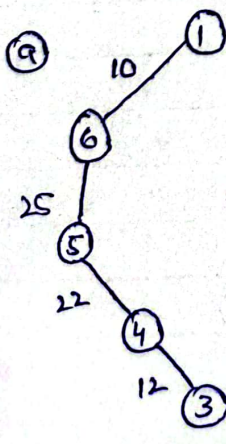


Prim's
→ Kruskal's Algorithm

→ PRIM'S ALGORITHM ↓



$$\text{max. no. of Edges} = \frac{n(n-1)}{2} = \frac{4(4-1)}{2} = 6$$



After ④
 $\checkmark (4,7) = 18$
 $(4,3) = 12$
 $(5,7) = 24$
 $(1,2) = 28$

After ③
 $\checkmark (3,2) = 16$
 $(4,7) = 18$
 $(5,7) = 24$
 $(1,2) = 28$

After ②
 $\checkmark (2,7) = 14$
 $(1,2)/(2,1) = 28$
 $(4,7) = 18$
 $(5,7) = 24$

Vertices = 7 (Complete)
 Edges = 7 - 1 = |V| - 1 = 6 (Complete)
 Cost = 10 + 25 + 22 + 12 + 16 + 14 = 99

→ Kruskal's Algorithm

Arrange weights in ascending order.

$$\checkmark (1, 6) = 10$$

$$\checkmark (3, 4) = 14$$

$$\checkmark (2, 7) = 14$$

$$\checkmark (2, 3) = 16$$

$$\times (4, 7) = 18$$

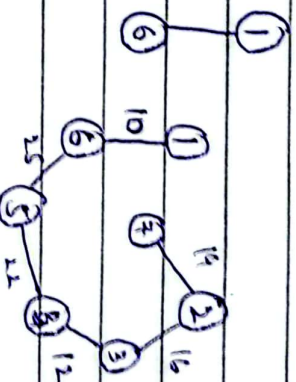
$$\checkmark (4, 5) = 22$$

$$\times (5, 7) = 25$$

$$\checkmark (1, 2) = 28$$

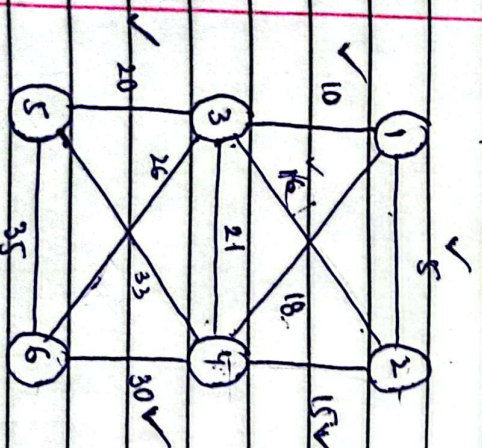
$$\times (5, 6) = 25$$

→ Because we'll not consider those who'll create a cycle.

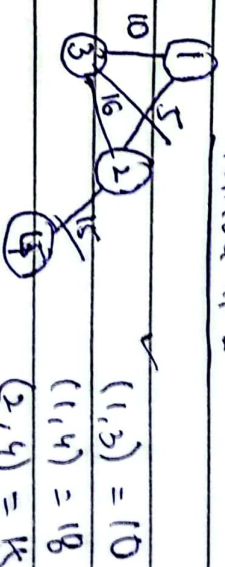


Cost = 99

Example # 2



Method # 1



$$(1, 3) = 10$$

$$(1, 4) = 18$$

$$(2, 4) = 15$$

$$(1, 2) = 5$$

$$(3, 4) = 21$$

$$(2, 3) = 16$$

$$(1, 4) = 18$$

$$(2, 4) = 15$$

$$(1, 3) = 10$$

$$(1, 4) = 18$$

$$(2, 4) = 15$$

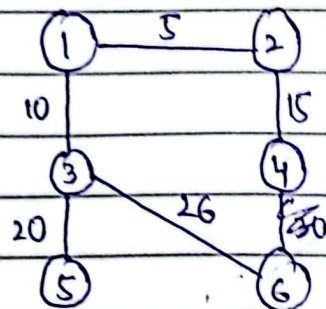
Wednesday
13-Dec-2023

ADA - Quiz

Zakir Matloob

04072113055

→ Prim's Algorithm:-



After (6)

$$(6, 5) = 35$$

$$(3, 6) = 33 \quad 26$$

$$(4, 5) = 33$$

$$(3, 4) = 21$$

$$\checkmark (3, 5) = 20$$

$$\times (2, 3) = 16$$

$$\times (1, 4) = 18$$

$$\text{Vertices} = 6$$

$$\text{Edges} = 6 - 1 = 5$$

$$\text{Cost} = 5076$$

$$= 5 + 15 + 10 + 20 + 26$$

#Step by Step on next page

After (5)

$$\times (5, 6) = 35$$

$$\times (5, 4) = 33$$

$$\times (6, 3) = 26$$

$$\times (3, 4) = 21$$

$$\times (2, 3) = 16$$

$$\times (1, 4) = 18$$

→ Kruskal's Algorithm

$$\checkmark (1, 2) \rightarrow 5$$

$$\checkmark (1, 3) \rightarrow 10$$

$$\checkmark (2, 4) \rightarrow 15$$

$$\times (2, 3) \rightarrow 16$$

$$\times (1, 4) \rightarrow 18$$

$$\checkmark (3, 5) \rightarrow 20$$

$$\times (3, 4) \rightarrow 21$$

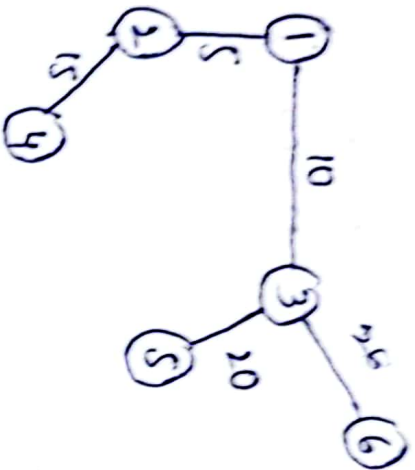
$$\checkmark (3, 6) \rightarrow 26$$

$$\times (4, 6) \rightarrow 30$$

$$(3, 6) = 33$$

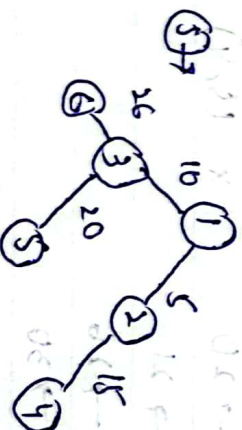
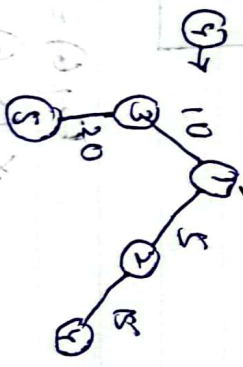
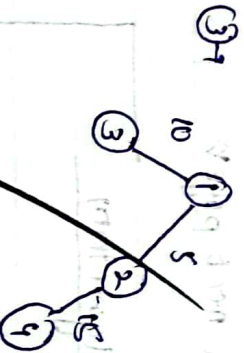
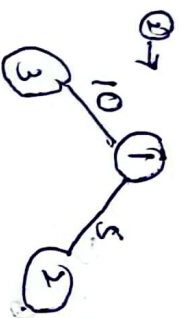
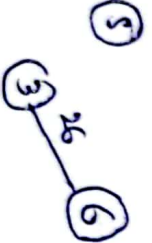
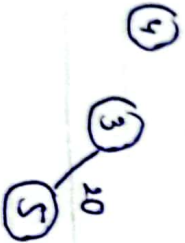
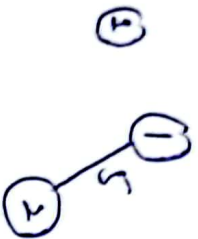
$$\times (5, 6) \rightarrow 35$$

$$\times (5, 4) \rightarrow 33$$

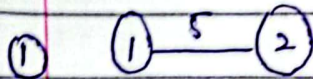


$$\text{Cost} = 15 + 5 + 10 + 20 + 25 = 75$$

Node - by - Node



→ Prim's Node-by-Node



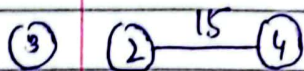
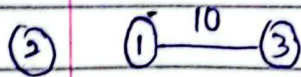
② → After ②

✓ (1,3) → 10

(1,4) = 18

(2,4) = 15

(2,3) = 16



③ → After ③

(3,5) = 20

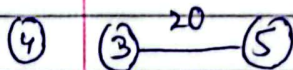
(3,6) = 26

(3,4) = 21

(2,3) = 16

✓ (2,4) = 15

(1,4) = 18



Cost = 5 + 10 + 15 + 20 + 26

= 76

④ → After ④

(4,6) = 30

(4,5) = 33

(3,4) = 21

× (1,4) = 18

✓ (3,5) = 20

(3,6) = 26

× (2,3) = 16

After ⑤ →

(5,6) = 35

(4,5) = 33

(4,6) = 30

✓ (3,6) = 26

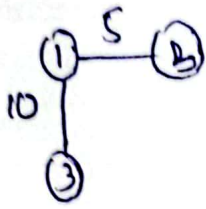
× (3,4) = 21

× (1,4) = 18

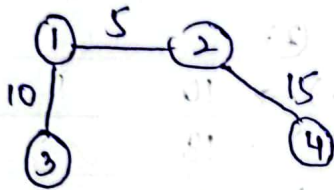
× (2,3) = 16 × (1,4) = 18



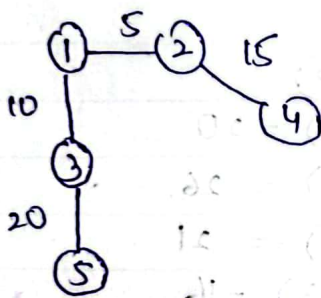
2 →



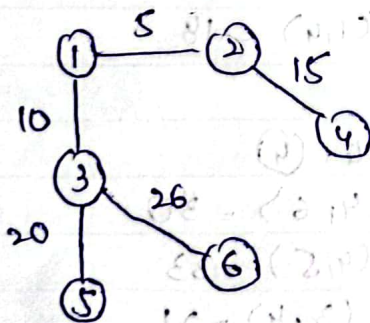
3 →



4 →



5 →



$$\begin{aligned}
 &dc = (v, c) \\
 &di = (v, i) \\
 &dc = (2, 1) \\
 &di = (2, 1) \\
 &dc = (2, 1) \\
 &di = (2, 1)
 \end{aligned}$$

$$\begin{aligned}
 &dc = (v, c) \\
 &di = (v, i) \\
 &dc = (2, 1) \\
 &di = (2, 1) \\
 &dc = (2, 1) \\
 &di = (2, 1)
 \end{aligned}$$

$$di = (v, i) \quad di = (v, i)$$