

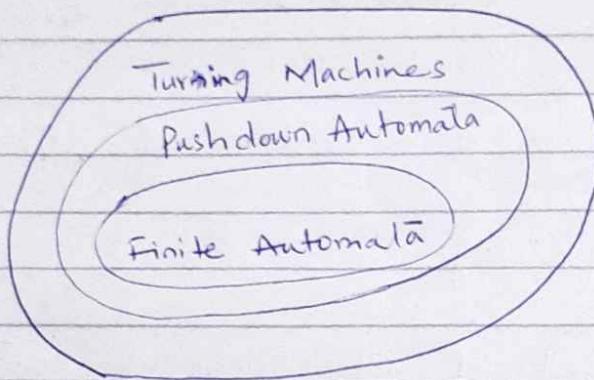
CS-331-TOA

THEORY OF AUTOMATA

DR. AKMAL KHATTAK

→ Course Outline and Introduction:

- Machine
- Regular Expression
- Grammar



Machine → Abstract form of computations.

↳ Not hardware → Abstract Machines.

→ Mathematically Modeling of Computational Tasks.

- Symbols - a, b, c, ---, 0, 1, 2, 3, ---, -, , ...

- Alphabets - A collection of Symbols

$$\Sigma = \{a, b, c\}$$

$$\Sigma = \{a, b, 0, 1, 2\}$$

- String / Word — A sequence of symbols.

e.g.: aabc, acbab.

Input Alphabet $\rightarrow \Sigma = \{a, b\}$

a b ab aab	$aac \times$ Invalid <u>'c'</u> .
-----------------------------	-----------------------------------

Valid String

- Language \rightarrow A collection of strings. & Rules

$$\Sigma = \{a, b\}$$

L_1 = Set of all strings of length 2.

$$= \{aa, ab, ba, bb\} \rightarrow \text{Finite set.}$$

L_2 = Set of all strings of length 3.

$$= \{aaa, aab, aba, abb, baa, bba, bab, bbb\}$$

L_3 = Set of all strings of length 4.

— that begins with 'a'

$$= \{a, aa, aaa, ab, abb \dots\}$$

→ Power of Σ

Σ^0 = set of all strings over Σ of length 0.

= $\{\epsilon\}$ → empty set.

Σ^1 = Set of all strings over Σ of length 1
= $\{a, b\}$

Σ^2 = Set of all strings over Σ of length 2.

Σ^n = $\underbrace{u \quad u \quad u \quad u \quad \dots \quad u}_{n}$

↳ Mother of all Languages / Universal Set.

Σ^* = $\Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \Sigma^3 \cup \dots \cup \Sigma^n$.

= $\{\epsilon\} \cup \{a, b\} \cup \{ab, aa, ba, bb\} \cup \dots$

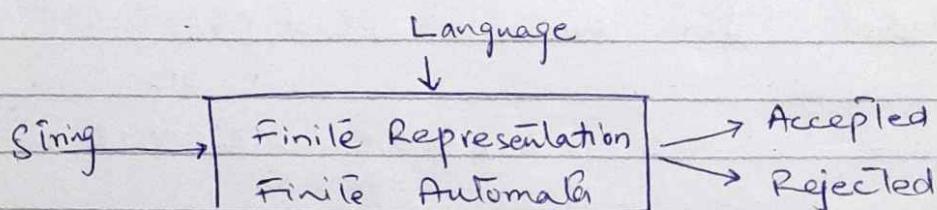
$L_1 \subseteq \Sigma^*$

Σ^* → infinite set.

$L_2 \subseteq \Sigma^*$

Every language is subset
of Σ^*

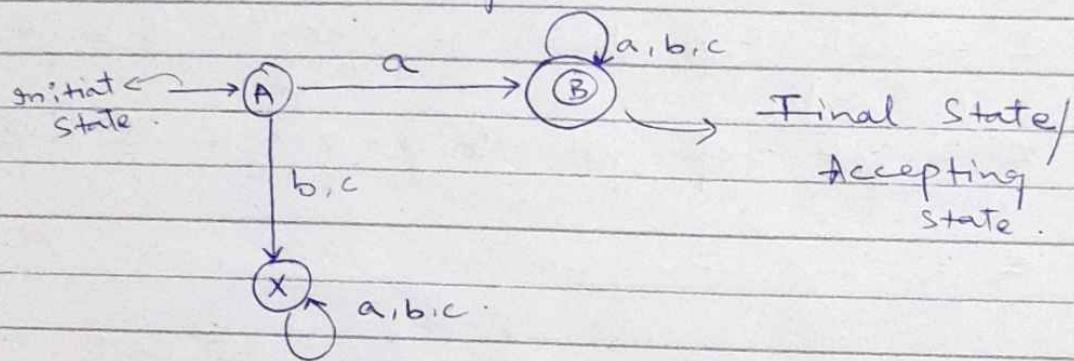
$L_3 \subseteq \Sigma^*$



$L = \text{Set of all strings that begins with 'a'}$.

$$= \{ a, aa, ab, \dots \}$$

State Transition Diagram



$$\Sigma = \{a, b\}$$

ab ab $A \xrightarrow{a} B \xrightarrow{b} B \xrightarrow{a} B \xrightarrow{b} B$.

babb $A \xrightarrow{b} X \xrightarrow{a} X \xrightarrow{b} X \xrightarrow{b} X$

~~abc~~

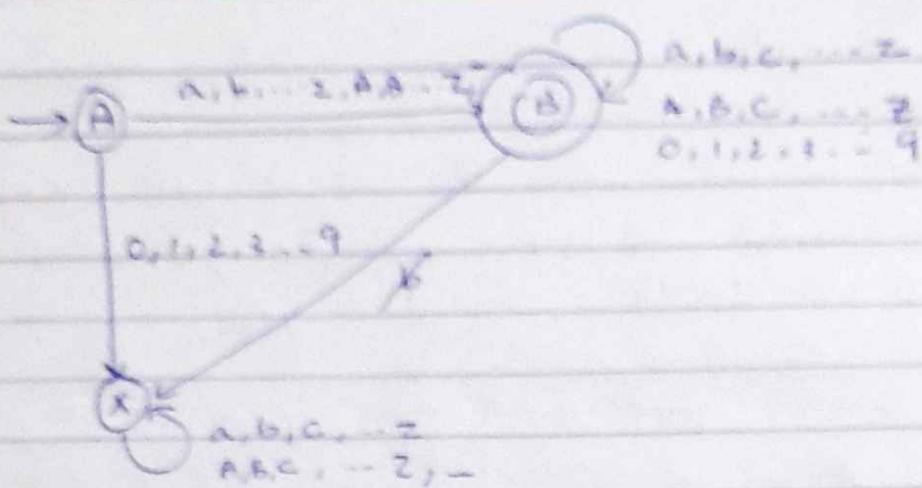
$$\Sigma = \{a, b, c\}.$$

abc.

Model for variable identifier.

$$\Sigma = \{a, b, c, -z, A, B, C, \dots, z, 0, 1, 2, 3, \dots, 9, -, \dots, \}$$

Predefined special characters
Not infinite



friday.

Lecture No. 2

→ DFA - Deterministic finite automata.

A DFA is represented by a 5-Tuple

$$(Q, \Sigma, \delta, q_0, F).$$

$Q \rightarrow$ Finite set of states

$\Sigma \rightarrow$ Alphabet

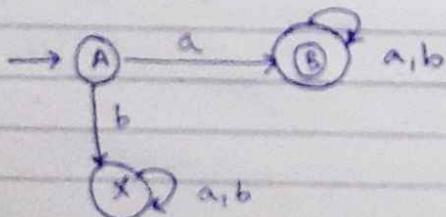
$q_0 \rightarrow$ Initial state

$F \rightarrow$ Accepting states

$\delta \rightarrow$ delta

↪ is a transition function.

$$\delta: Q \times \Sigma \rightarrow Q$$



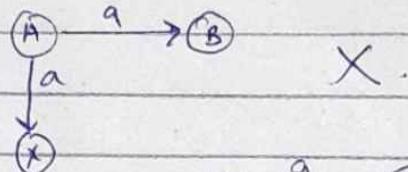
$$Q = \{A, B, X\}$$

$$\Sigma = \{a, b\}$$

Q1. ~~Har state sy har input symbol exhaust hona chahiye~~

2) Har symbol aik hi state par map hona chahiye. Multiple states par nahi map ho sakti.

Transition function



$$\delta : (A, a) \rightarrow B.$$

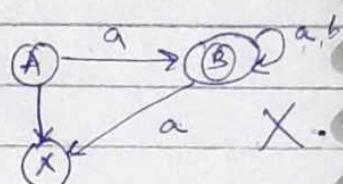
$$\delta : (A, b) \rightarrow X.$$

$$\delta : (B, a) \rightarrow B$$

$$\delta : (B, b) \rightarrow B$$

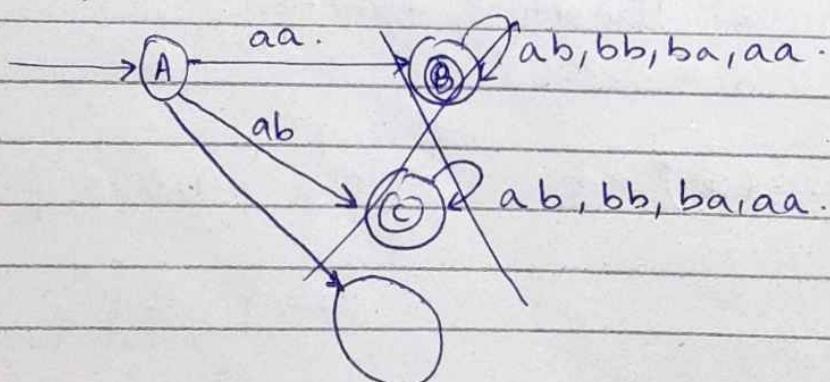
$$\delta : (X, a) \rightarrow X$$

$$\delta : (X, b) \rightarrow X.$$

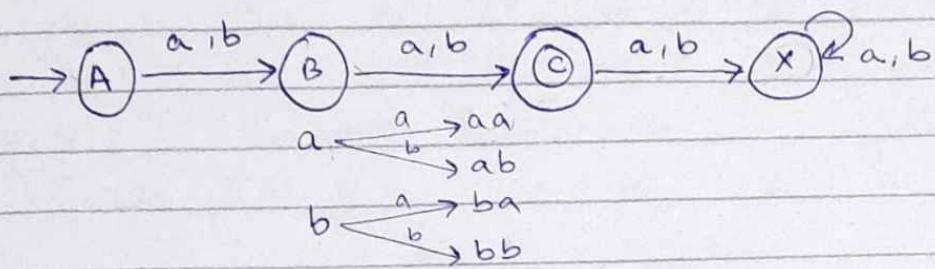


At least one accepting state should be in DFA. It is not possible that there is no accepting state. There can be more than one accepting state.

→ Construct a DFA that accepts set of all strings over $\Sigma = \{a, b\}$ of length 2.

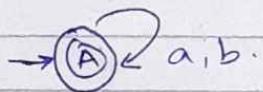
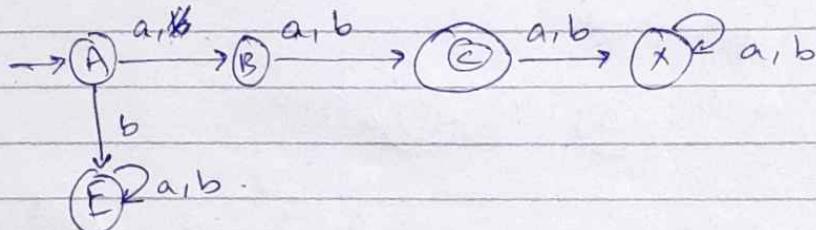


ab



There can be multiple DFA's for one computational problems But There is only one minimal DFA for a computational problem.

String of length-2 starting with a.



It accepts all the accepting strings of length-2. But it also accepts non-accepting strings. We should check for both.

ba ✓	A \xrightarrow{b} B \xrightarrow{a} C ✓
abb ✗	A \xrightarrow{a} B \xrightarrow{b} C \xrightarrow{b} ✗

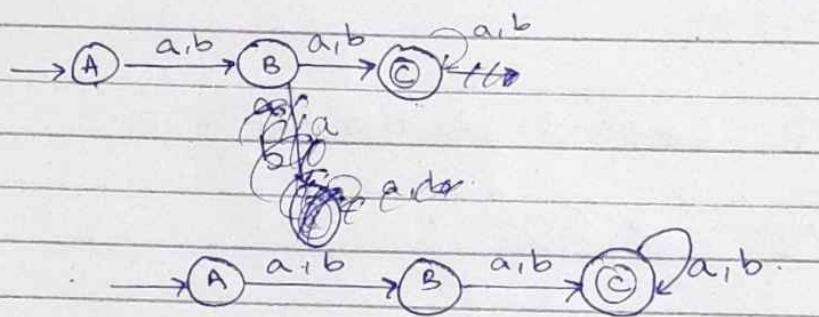
Finite set \rightarrow DFA always exists.
Infinite set \rightarrow Maybe DFA exists maybe not.

\rightarrow A Finite Automata is set to accept a Language if all the strings in the language are accepted and all the strings not in the language are not accepted.

\Rightarrow Set such

\Rightarrow Construct a DFA that accepts set of all strings $w \in \{a, b\}^*$ such that $|w| \geq 2$.

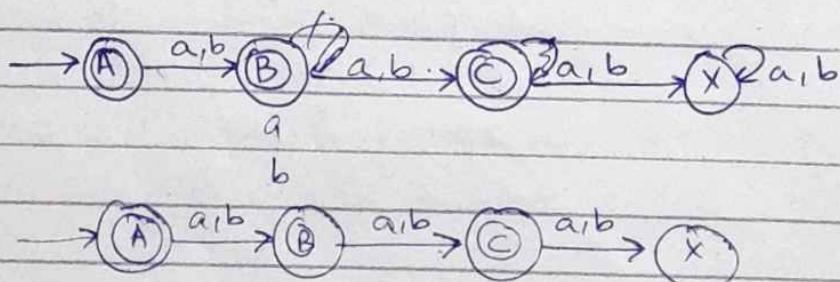
Fabric. d. 1, 2, 3) $b \geq 2$ length.



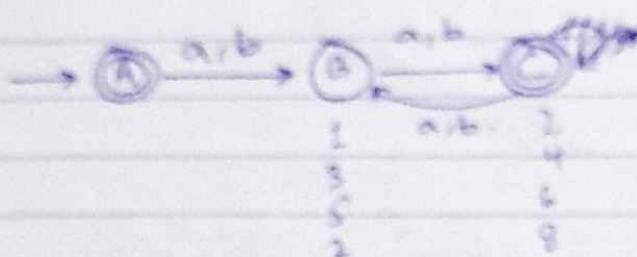
$|w|$

aaabbb \rightarrow A \xrightarrow{a} B \xrightarrow{a} C \xrightarrow{a} C \xrightarrow{b} C \xrightarrow{b} C \xrightarrow{b} C (accept)

\Rightarrow For $|w| \leq 2$.



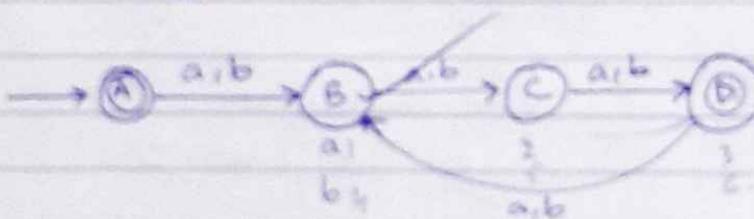
\Rightarrow construct a minimal DFA "not accepts set of all strings over $2 \times \{a,b\}$ such that $|w| \bmod 3 = 0$.



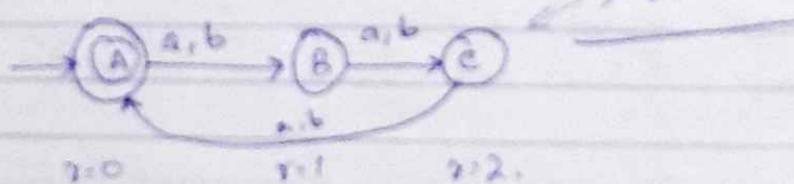
not minimal



$|w| \bmod 3 \neq 0$



$3 \nmid |w|$



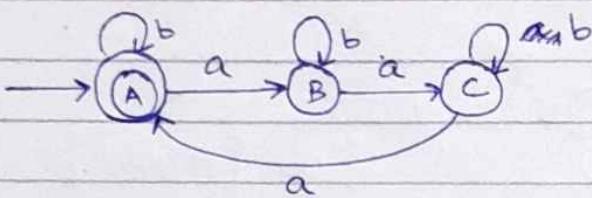
$3 \nmid |w|$

LECTURE NO. 4.

→ DFA's.

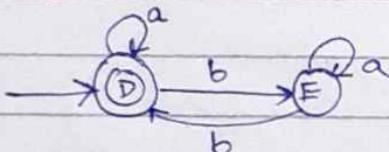
⇒ $n_a(w) \bmod 3 = 0$ & $n_b(w) \bmod 2 = 0$

$n_a(w) \bmod 3 = 0$.



$$n_a = \{A, B, C\}$$

$n_b(w) \bmod 2 = 0$.

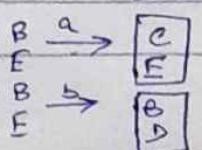
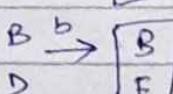
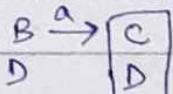
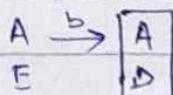
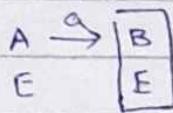
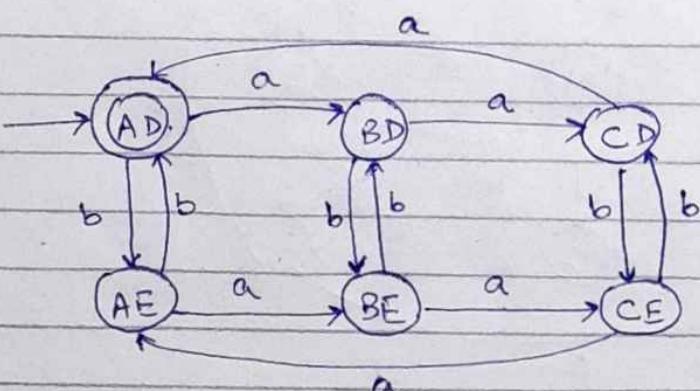


$$n_b = \{D, E\}$$

$$\Sigma = \{a, b\}$$

$$\mathcal{Q} = \{A, B, C\} \times \{D, E\}$$

$$= \{AD, AE, BD, BE, CD, CE\}$$

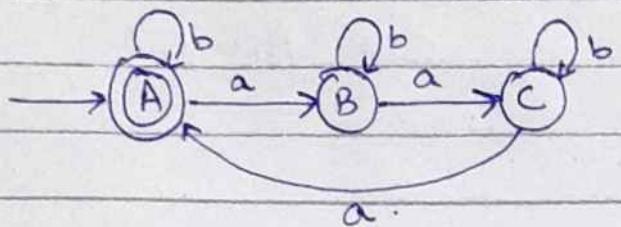


→ Construct a minimal DFA which accepts set of all strings over $\Sigma = \{a, b\}$ where number of a's & b's are divisible by 3.

Verifi

$$n_a(w) \bmod 3 = 0.$$

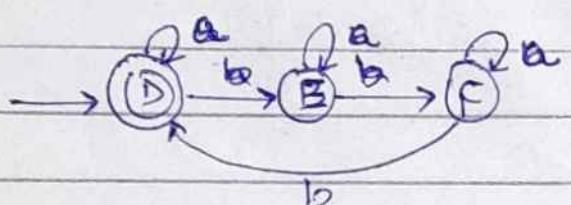
$$02/a$$



$$n_a = \{A, B, C\}$$

$$\rightarrow (0)$$

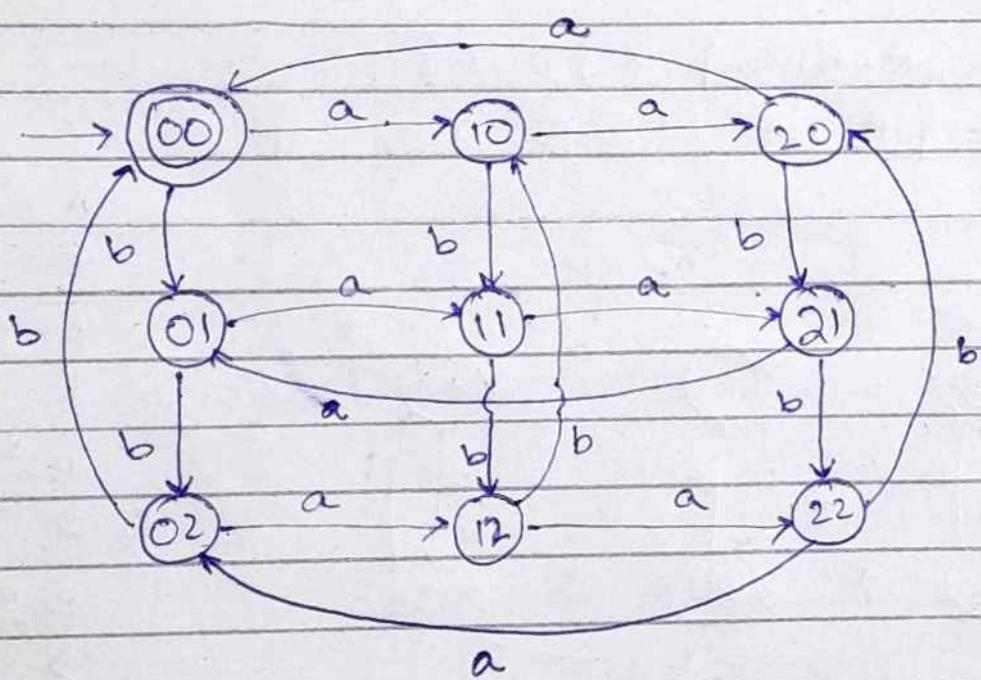
$$n_b(w) \bmod 3 = 0.$$



$$n_b = \{D, E, F\}$$

$$\rightarrow (0)$$

$$\rightarrow (1)$$

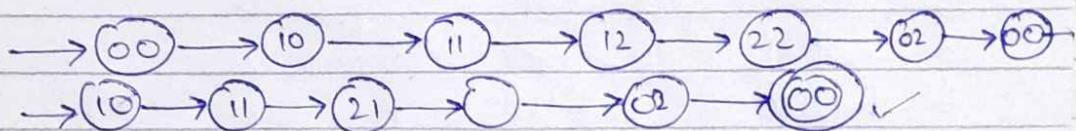
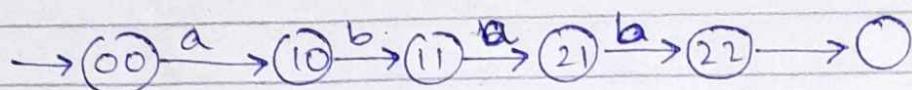


→ Cons
set
when
is d

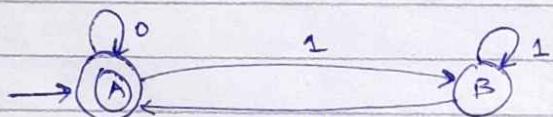
Verification:

02/ aba bbbab X Non-accepting.

00/ abbaabababab ✓ Accepting.



→ Construct a minimal DFA which accepts set of all strings over $\Sigma = \{0, 1\}$ which when interpreted as a binary number is divisible by 2.



$$0, 00, 0000 = 0$$

$$0001 = 1$$

$$10, 010, 0010 = 2$$

$$0011 = 3$$

$$100, 0100 = 4$$

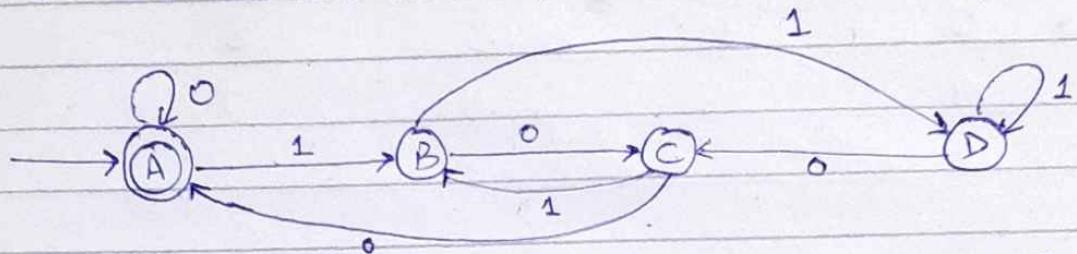
$$0101 = 5$$

Tuesday

LECTURE NO. 5

→ Construct a minimal DFA that accepts set of all strings over $\Sigma = \{0, 1\}$ which when interpreted as a binary number is divisible by 4.

Machine/Model/Automaton/State Transition Diagram.



$0000 = 0$	$0001 = 1$	$0010 = 2$	$0011 = 3$
$0100 = 4$	$0101 = 5$	$0110 = 6$	$0111 = 7$
$1000 = 8$	$1001 = 9$	$1010 = 10$	$1011 = 11$
:	:	:	:

→ State Transition Table:

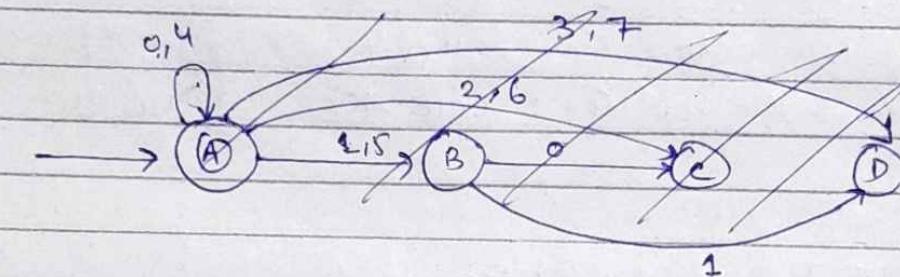
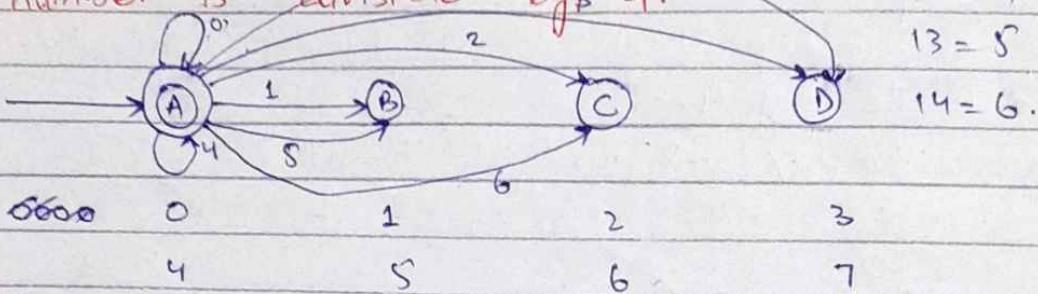
	0	1
A	A	B
B	C	D
C	A	B
D	C	D

* → Represents Accepting State.

" → Represents initial state.

+ 6 9 10 11 12
 7 8 11 3 4
 2 || 0
 u-2

→ Construct a minimal DFA that accepts set of all strings over $\Sigma = \{0, 1, 2, 3, 4, 5, 6, 7\}$ which when interpreted as an octal number is divisible by 4.



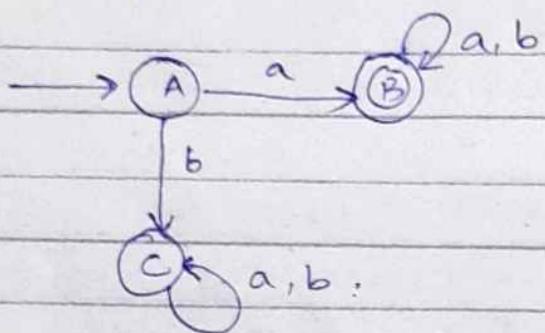
State Transition Table:

	0	1	2	3	4	5	6	7
A	A	B	C	D	A	B	C	D
B	A	B	C	D	A	B	C	D
C	A	B	C	D	A	B	C	D
D	A	B	C	D	A	B	C	D.

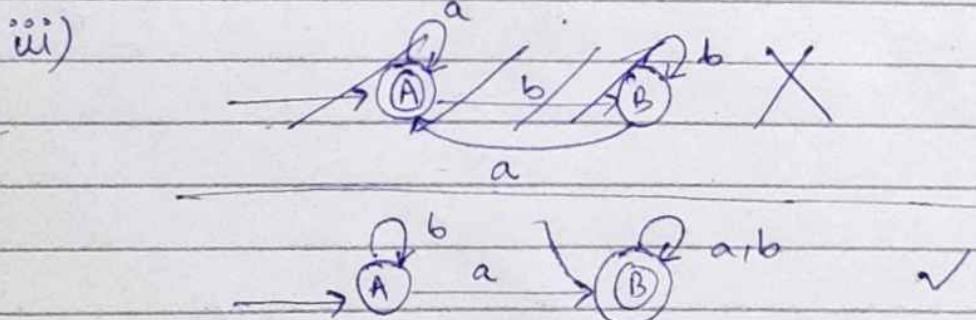
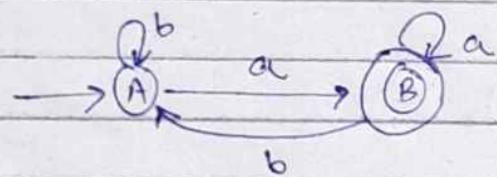
→ Construct a minimal DFA that accepts
set of all strings over $\Sigma = \{a, b\}$

- Starting with 'a'
- Ending with 'a'
- Containing 'a'

(i) Language: $\{a, aa, ab, abb, \dots\}$.



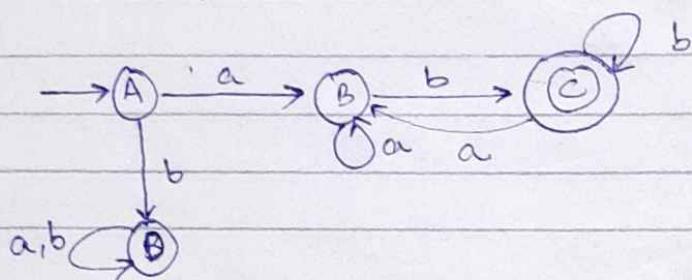
(ii) Language = $\{a, aa, ba, aba, bba, \dots\}$.



Lecture No. 6

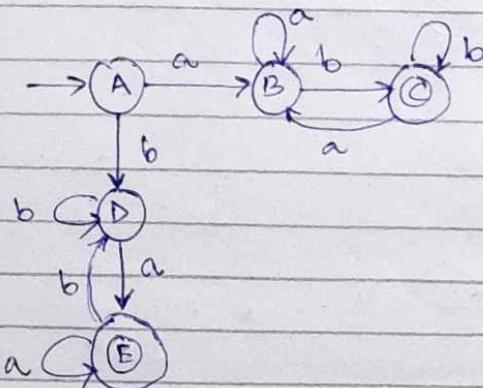
→ Construct a DFA which accepts set of all strings over $\Sigma = \{a, b\}$ - that starts with 'a' and ends with 'b'

Language = { ab, abb, --- }



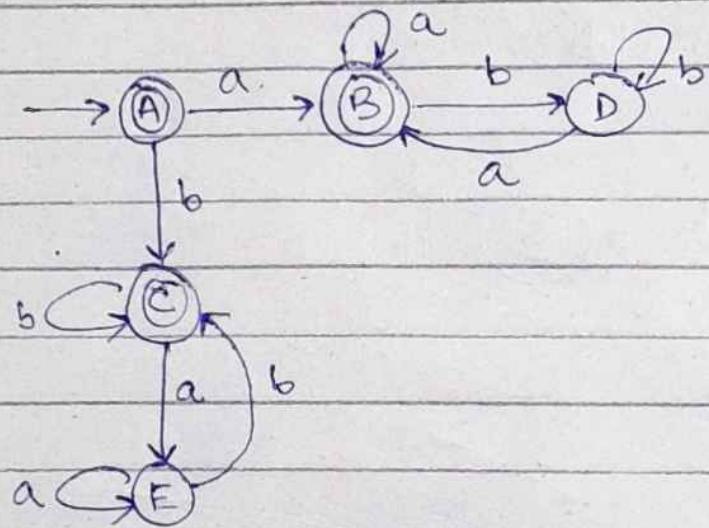
→ starts and ends with the different symbol..

Language = { ab, ba, abb, baa --- }



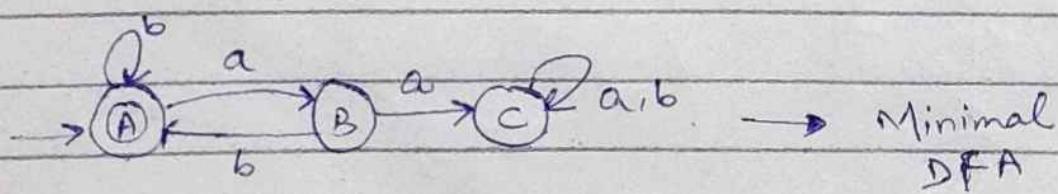
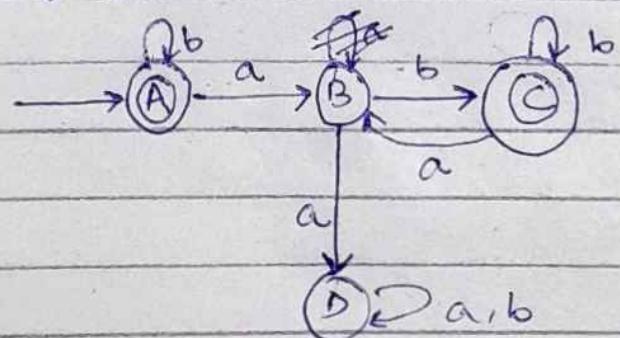
→ That starts and ends with same symbol. → 71

Language = { ε, a, aa, bb, b, aba, bab, ... }



→ That accepts set of all strings where every 'a' is followed by a 'b'.

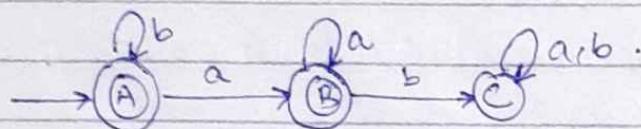
Language = { ε, ab, abab, aab, b, bb, abb, ... }



→ Minimal DFA

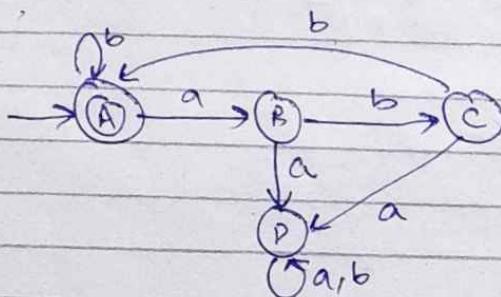
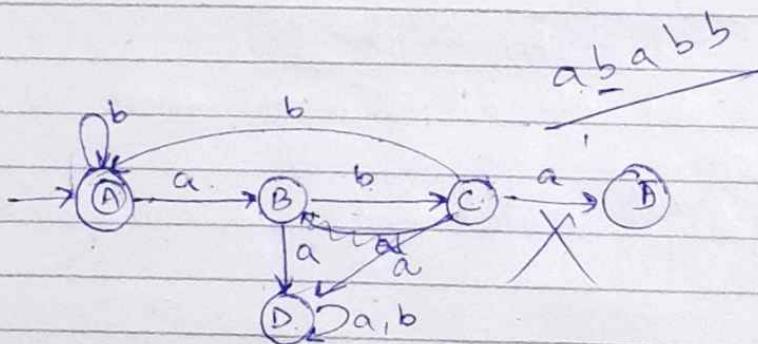
→ That accepts set of all strings where every 'a' is never followed by a 'b'.

Language: { ϵ , a, aa, ba, bbb, bba...}.



→ where every 'a' is followed by a 'bb'

Language: { ϵ , b, bb, bbb, abb, abbabb, babb...}.

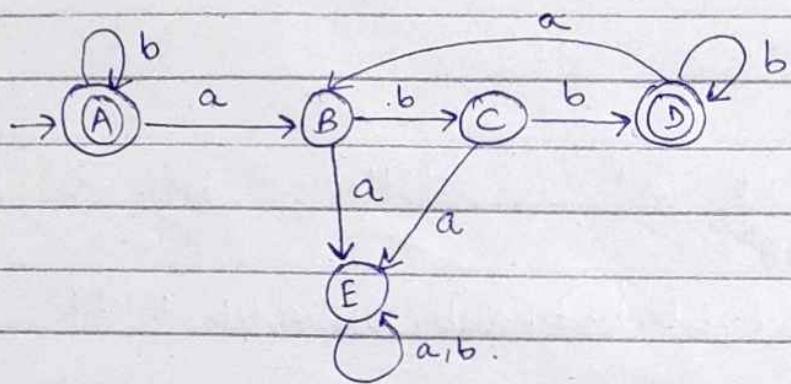


Tuesday.
12/03/2024

Lecture No. 7

→ Construct a DFA over $\Sigma = \{a, b\}$ that accepts set of all strings where every 'a' is followed by a 'bb'.

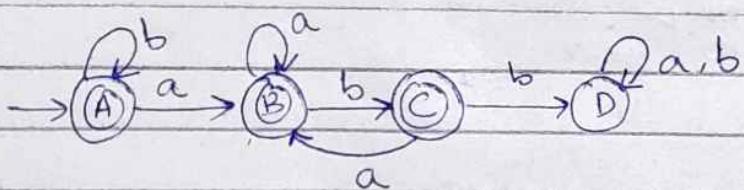
Language = { $\epsilon, b, bb, bbb, abb, abbbb, bbaabb,$
 $abbbabb, \dots$ }



→ 3rd

→ accepts set of all strings where 'a' is never followed by a "bb"

Language = { $\epsilon, b, bb, bbb, ab, aab, aa, baa, abab$ }

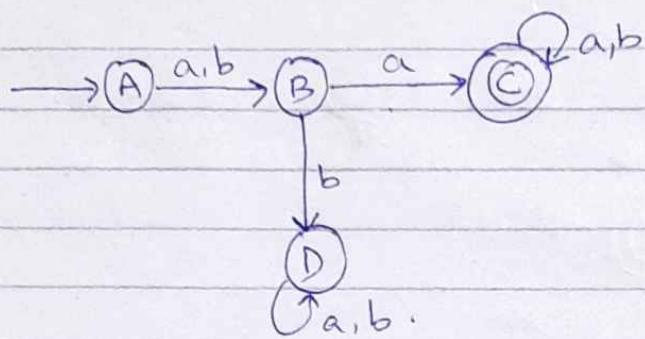


→ where
language

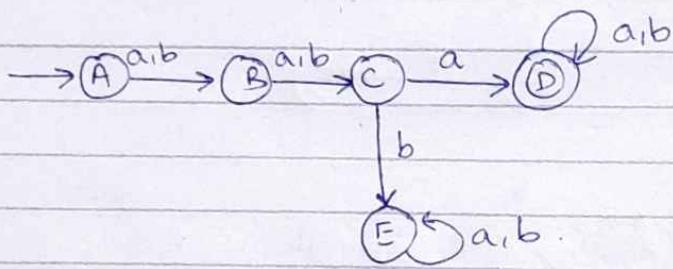
day.
3/2024

→ That accepts set of all strings where the second symbol is 'a'.

Language: { aa, ba, aab, bab, baaba... }

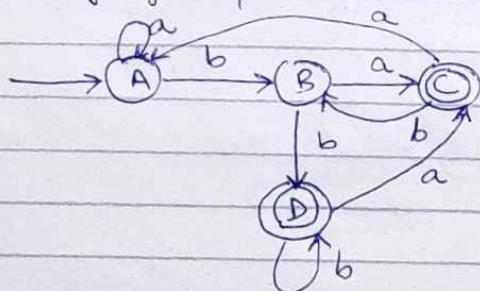


→ 3rd Symbol is 'a'



→ where the 2nd last symbol is "b"

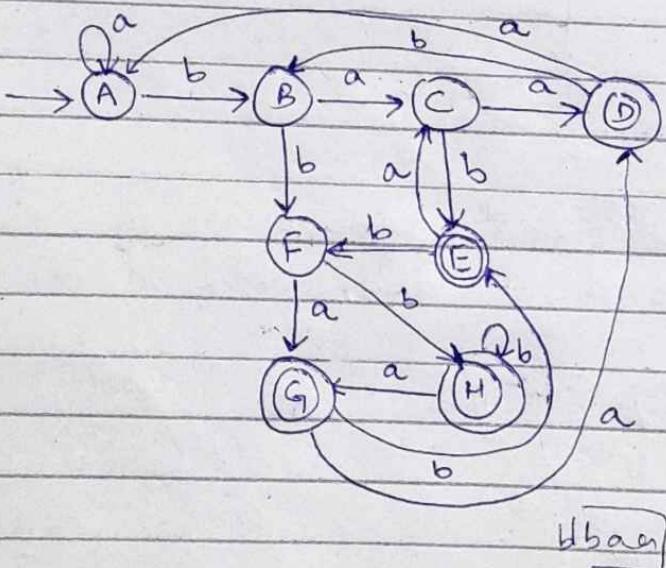
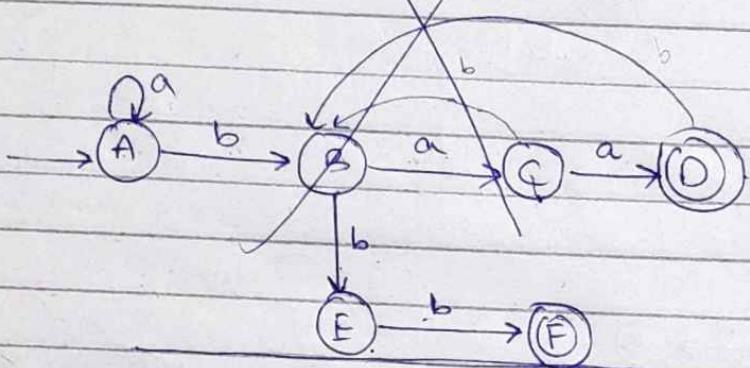
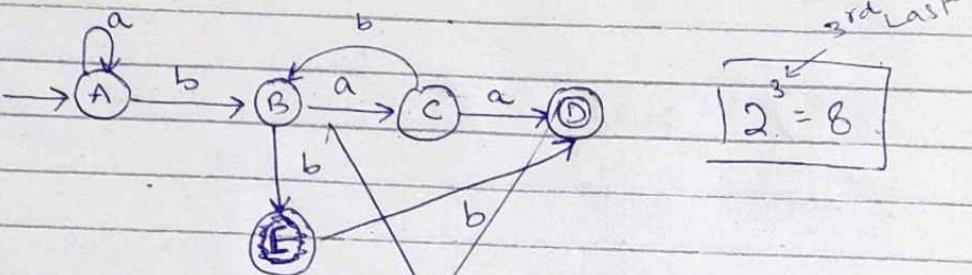
Language = { ba, bb, bba, abb, abbba, ababb }



$\begin{matrix} bab & aa \\ ab & ab \\ bb & ba \\ ba & ab \\ ab & bb \\ bb & ba \end{matrix}$

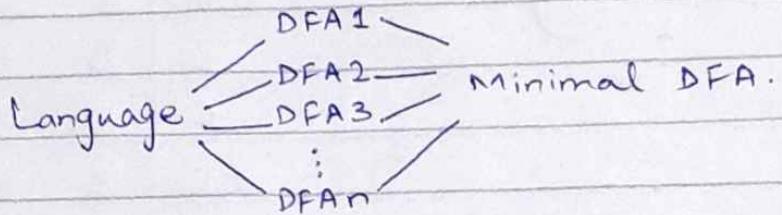
→ 3rd Last symbol is 'b'.

Language = { abab, a bbb, baa, abb b, babab
abaa, bbb, bab, bba }



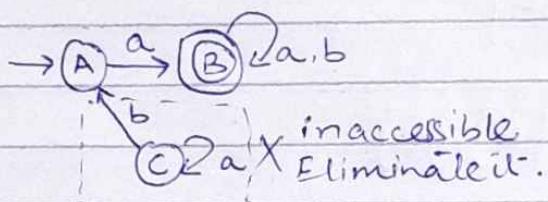
LECTURE NO. 8

→ Minimization of DFA:



Step No. 1 :

→ Eliminate inaccessible states. (which can't be reached from initial state).



→ Partitioning Method :

- Two states can be combined if both are equivalent.

Two states are equivalent if.

$$\begin{array}{ll} \delta(A, x) \rightarrow F & \delta(A, x) \rightarrow F \\ \checkmark \quad \delta(B, x) \rightarrow F & \text{OR} \quad \delta(B, x) \rightarrow F \end{array}$$

A on input string x
maps on F state
which is accepting state.

where x is an input string.

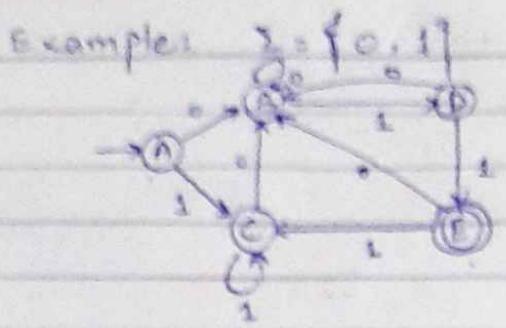
if $|x|=0$, Then A & B are 0-Equivalent.

if $|x|=1$, Then A & B are 1-Equivalent.

if $|x|=2$; Then A & B are 2-Equivalent.

⋮

if $|x|=n$, Then A & B are n-Equivalent.



	0	1
A	B	C
B	B	D
C	B	C
D	B	E
E	B	C

0-Equivalence: Non-Accepting $\{A, B, C, D\}$, Accepting: $\{E\}$.

1-Equivalence:

$\{A, B, C\} \{D\} \{E\}$

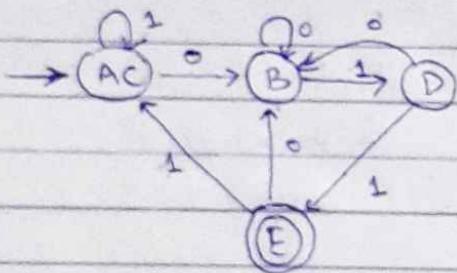
2-Equivalence:

$\{A, C\} \{B\} \{D\} \{E\}$

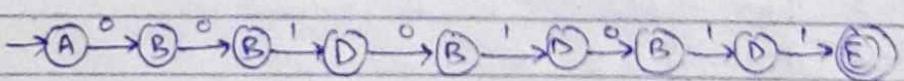
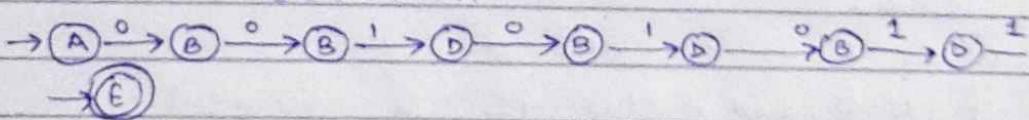
3-Equivalence:

$\{A, C\} \{B\} \{D\} \{E\}$

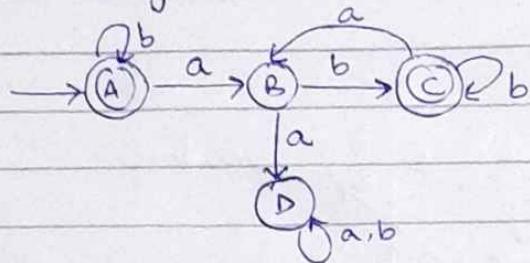
Now Merge



Verifications: 00101011



Example: Every 'a' has to be followed by a 'b'



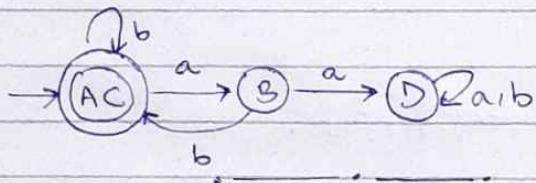
	a	b
1	B	A
C	D	C
D	B	C
E	D	D
C	D	D

No, inaccessible states.

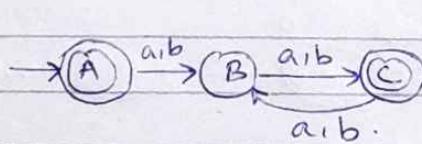
0-Equivalence: $\{B, D\} \{A, C\}$.

1-Equivalence: $\{B\} \{D\} \{A, C\}$

2-Equivalence: $\{B\} \{D\} \{A, C\}$



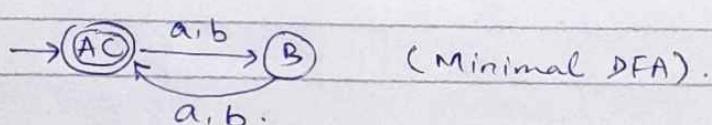
Example: $\Sigma = \{a, b\}$ all strings such that $|w| \bmod 2 = 0$.



	a	b
1	B	B
2	C	C
3	B	B
4	C	B

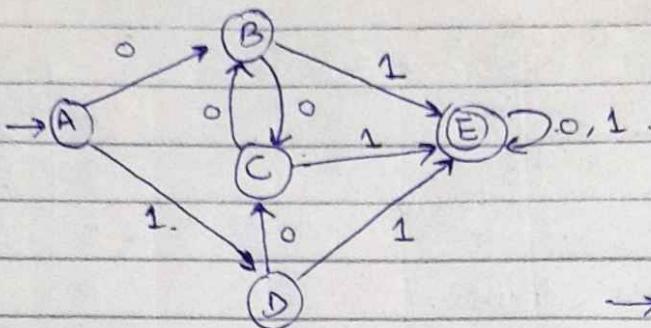
0-Equivalence: $\{A, C\} \{B\}$

1-Equivalence: $\{A, C\} \{B\}$



(Minimal DFA).

Example: $\Sigma = \{0, 1\}$



0-Equivalence:

$$\{A, B, C, D\} \quad \{E\}$$

	0	1
A	B	D
B	C	E
C	B	E
D	C	E
*E	E	E

1-Equivalence:

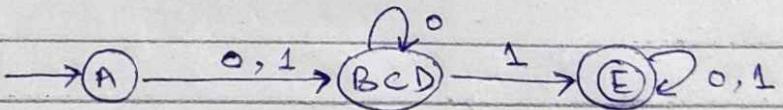
$$\{A\}$$

$$\{B, C, D\} \quad \{E\}$$

2-Equivalence:

$$\{A\} \quad \{B, C, D\} \quad \{E\}.$$

Minimized DFA:



LECTURE NO. 9

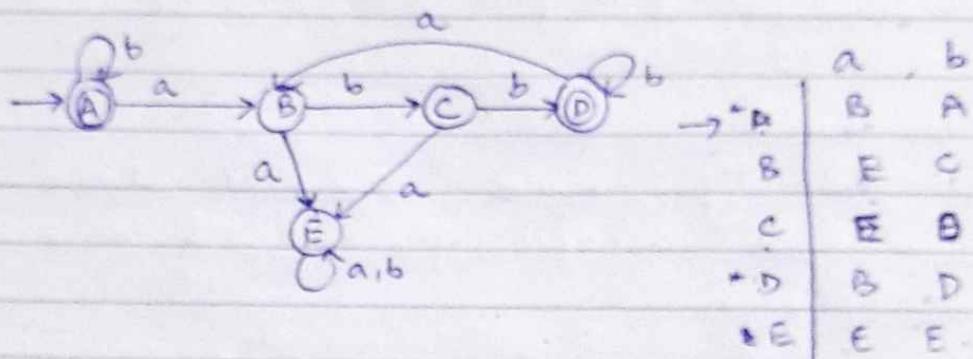
→ Minimization of DFA:

• Partitioning Method:

Example #2

→ 'a' is followed by a 'bb'.

Language = { abb, babb, ... }

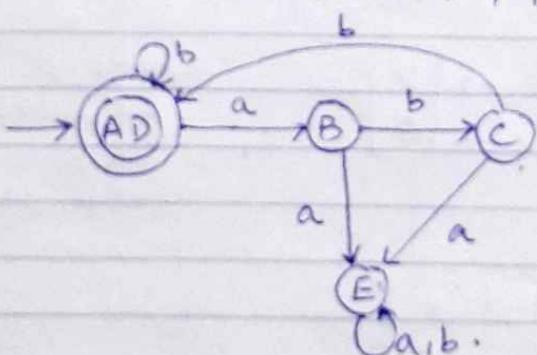


0. Equivalence: { B, C, E } { A, D }

1. Equivalence: { B, E } { C } { A, D }

2. Equivalence: { B } { E } { C } { A, D }

3. Equivalence: { B } { E } { C } { A, D }



Verification: abbab ab X

$\rightarrow AD \xrightarrow{a} B \xrightarrow{b} C \xrightarrow{b} AD \xrightarrow{a} B \xrightarrow{b} C$

- Table Filling Method:

Example #1.

	A	B	C	D	E
A					
B	✓				
C	✓	✓			
D	-	✓	✓		
E	✓	✓	✓	✓	

- Iteration-1:

- Initially choose a pair where 1 state is accepting and 1 is non-accepting.

- Iteration-2:

$$\underline{C, B} \quad \delta(C, a) \rightarrow \boxed{E}$$

$$\delta(B, b) \rightarrow \boxed{E}$$

$$\delta(C, b) \rightarrow \boxed{D}$$

$$\delta(B, b) \rightarrow \boxed{C}$$

check (D, C) cell
if marked then
mark C, B other
wise leave empty.

$$D, A \quad \delta(D, a) \rightarrow \boxed{B}$$

$$\delta(A, a) \rightarrow \boxed{B}$$

$$\delta(D, b) \rightarrow \boxed{D}$$

$$\delta(A, b) \rightarrow \boxed{A}$$

will remain unmarked

$$\underline{E, B} \quad \begin{array}{l} \delta(E, a) \rightarrow \boxed{E} \\ \delta(B, a) \rightarrow \boxed{E} \end{array}$$

$$\begin{array}{l} \delta(E, b) \rightarrow \boxed{E} \\ \delta(B, b) \rightarrow \boxed{C} \end{array}$$

$$\underline{E, C} \quad \begin{array}{l} \delta(E, a) \rightarrow \boxed{E} \\ \delta(C, a) \rightarrow \boxed{E} \end{array}$$

$$\begin{array}{l} \delta(E, b) \rightarrow \boxed{E} \\ \delta(C, b) \rightarrow \boxed{D} \end{array}$$

- Iteration-3:

$$\underline{D, A}: \begin{array}{l} \delta(D, a) \rightarrow \boxed{B} \\ \delta(A, a) \rightarrow \boxed{B} \end{array}$$

$$\begin{array}{l} \delta(D, b) \rightarrow \boxed{D} \\ \delta(A, b) \rightarrow \boxed{A} \end{array}$$

unmarked

E, B:

$$\begin{array}{l} \delta(E, a) \rightarrow \boxed{E} \\ \delta(B, a) \rightarrow \boxed{E} \end{array}$$

$$\begin{array}{l} \delta(E, b) \rightarrow \boxed{E} \\ \delta(B, b) \rightarrow \boxed{C} \end{array}$$

Mark E, B bcz E, C
is Marked.

- Iteration-4:

$$\underline{D, A}: \begin{array}{l} \delta(D, a) \rightarrow \boxed{B} \\ \delta(A, a) \rightarrow \boxed{B} \end{array}$$

$$\begin{array}{l} \delta(D, b) \rightarrow \boxed{D} \\ \delta(A, b) \rightarrow \boxed{A} \end{array}$$

unmarked

LECTURE NO. 12

→ E-NFA (Epsilon NFA)

- Extended Type of NFA.
 - E-NFA is easier to construct.
 - $E\text{-NFA} \rightarrow NFA \rightarrow DFA \rightarrow \text{Minimal DFA}$.
 - Can be more than one E-NFA, DFA, NFA.
 - But there is only one minimal DFA.
- E-NFA is a 5-Tuple set.

$$\{Q, \Sigma, q_0, F, \delta\}$$

$Q \rightarrow$ Finite set of states

$\Sigma \rightarrow$ Input Alphabet.

$q_0 \rightarrow$ Initial state

$F \rightarrow$ Accepting States

E-NFA

$$\delta: Q \times (\Sigma \cup \{\epsilon\}) \rightarrow 2^Q$$

NFA

$$\delta: Q \times \Sigma \rightarrow 2^Q$$

DFA

$$\delta: Q \times \Sigma \rightarrow Q$$

Example:

$$\text{Language} = \{a^m b^n c^p \mid m, n, p \geq 0\}$$

$a^0 \rightarrow 0$ occurrences of a.

$a^1 \rightarrow 1$ occurrence of a.

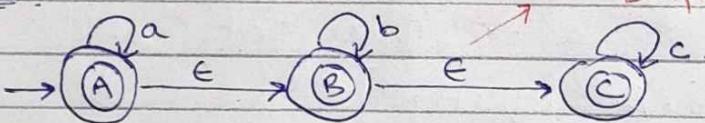
$$a^0 b^0 c^1 = c.$$

$$a^1 b^0 c^1 = ac$$

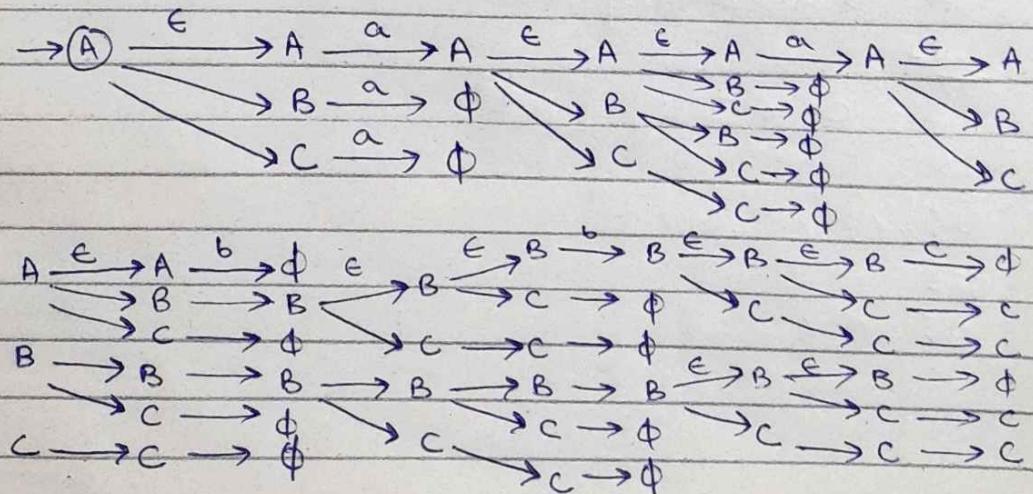
$$a^2 b^2 c = aabbcc.$$

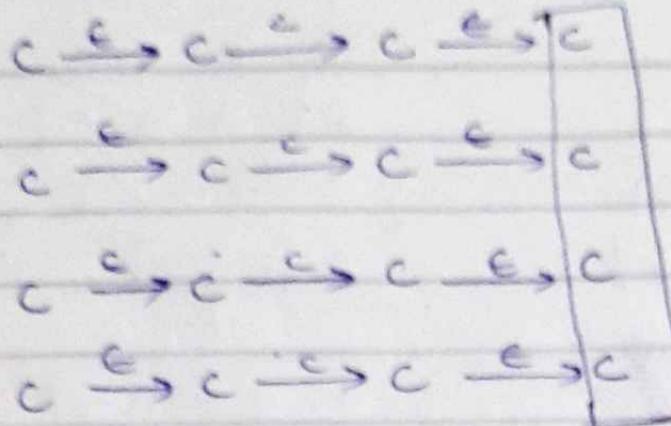
SOLUTION: ϵ -NFA.

This is
 ϵ -move.
Empty string is
passed.



- aabbcc → Verification string



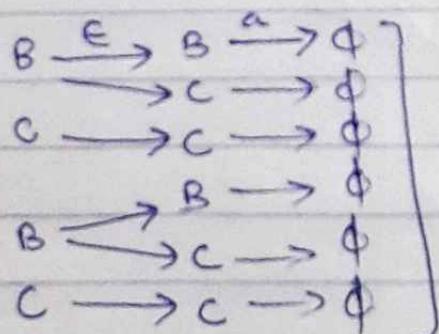
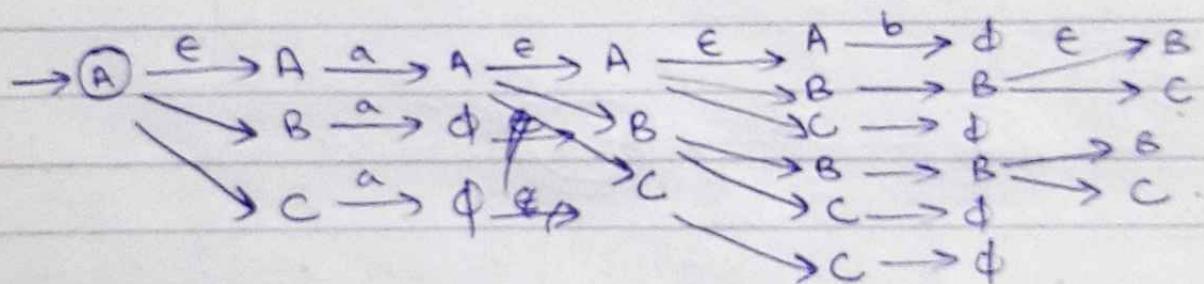


If atleast
one of them
is accepting
state then
string is accepted

Mathematical Formula:

$$\epsilon\text{-closure}(\delta(\epsilon\text{-closure}(A), x))$$

. abac



Not accepted.

• ϵ -NFA to NFA:

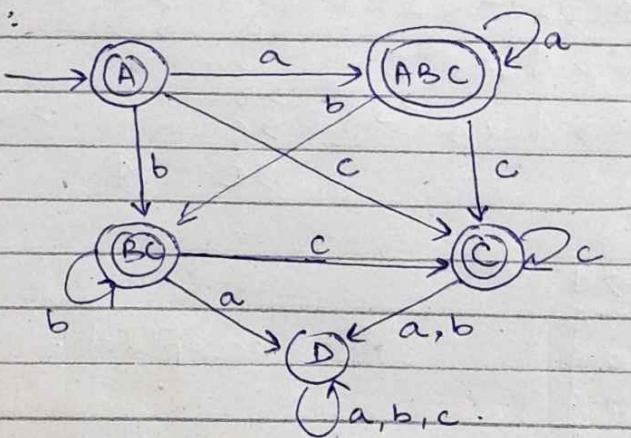
NFA	a	b	c
$\rightarrow *A$	$\{A, B, C\}$	$\{B, C\}$	$\{C\}$
$*B$	\emptyset	$\{B, C\}$	$\{C\}$
$*C$	\emptyset	\emptyset	$\{C\}$

E-Closure.	A	$\{A, B, C\}$
B	$\{B, C\}$	
C	$\{C\}$	

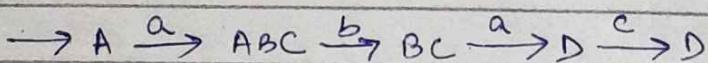
• NFA \rightarrow DFA.

	a	b	c
$\rightarrow *A$	[ABC]	[BC]	[C]
$*[ABC]$	[ABC]	[BC]	[C]
$*[BC]$	[D]	[BC]	[C]
$*[C]$	[D]	[D]	[C]
[D]	[D]	[D]	[D]

DFA:



abac:



DFA \Rightarrow Min DFA.

0-Equivalence: $\{A, ABC, BC, C\} \neq \{D\}$.

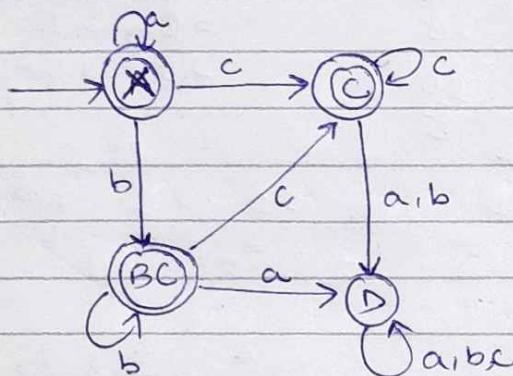
1-Equivalence:

$\{A, ABC\} \neq \{BC\} \neq \{C\} \neq \{D\}$

2-Equivalence:

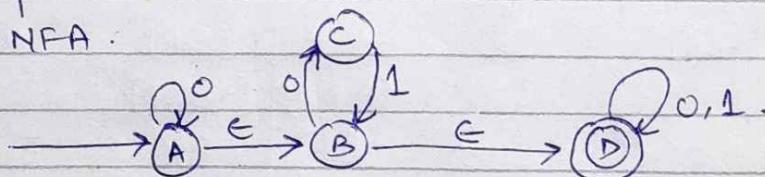
$\{A, ABC\} \neq \{BC\} \neq \{C\} \neq \{D\}$.

	a	b	c
$\rightarrow^* A$	ABC	BC	C
ABC	ABC	BC	C
BC	D	BC	C
C	D	D	C
D	D	D	D



Example - 2:

ϵ -NFA.



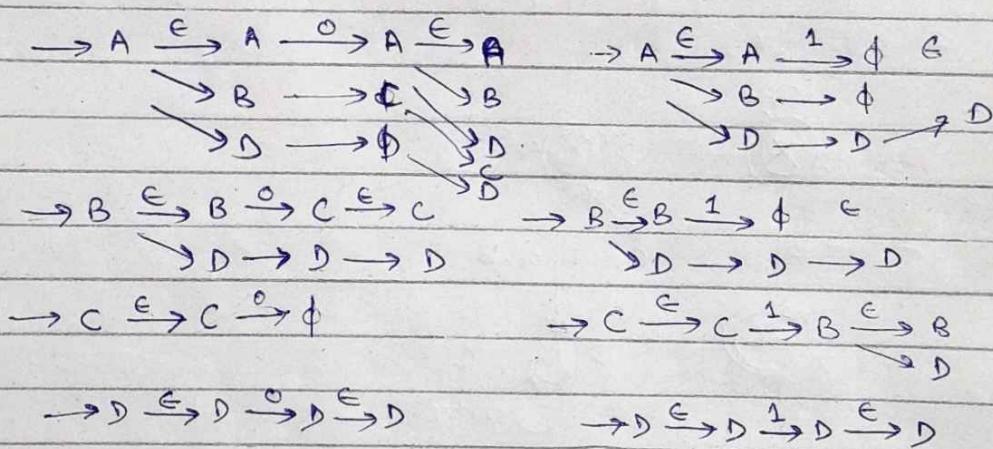
$$0^*(01)^*(0+1)$$

101101?

Imp.
 * All those states in NFA will be accepting states through which we can reach accepting state of ϵ -NFA via epsilon move.

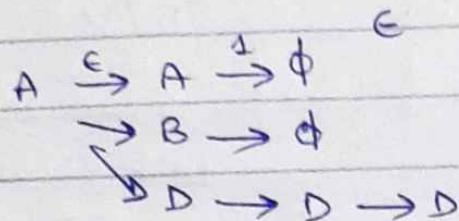
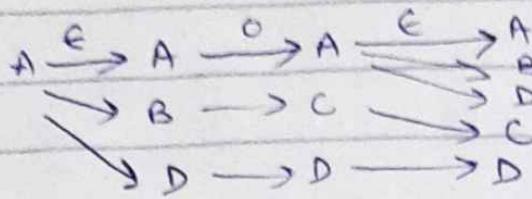
• ENFA to NFA. So A, B will ^{also} be accepting states in NFA

	0	1	<u>ϵ-closure.</u>
* A	$\{A, B, D\}$	$\{D\}$	A $\{A, B, D\}$
* B	$\{B, D\}$	$\{D\}$	B $\{B, D\}$
C	\emptyset	$\{B, D\}$	C $\{C\}$
* D	$\{D\}$	$\{D\}$	D $\{D\}$.

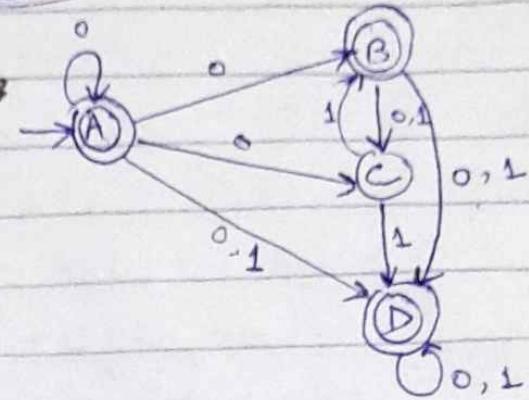


• NFA to DFA.

	0	1	
$\rightarrow A$	$[ABD]$	$[D]$	$\rightarrow A$
$[ABD]$	$[ABC]$	$[D] \times [ABD]$	$[ABD]$
D	$[ABCD]$	$[BD] \times [D]$	$[D]$
$[ABC]$	$[BCD]$	$[BD] \times [ABC]$	$[BD]$
$[BD]$		$[BD] \times [CD]$	$[D]$
		$*[CD]$	$[BD]$



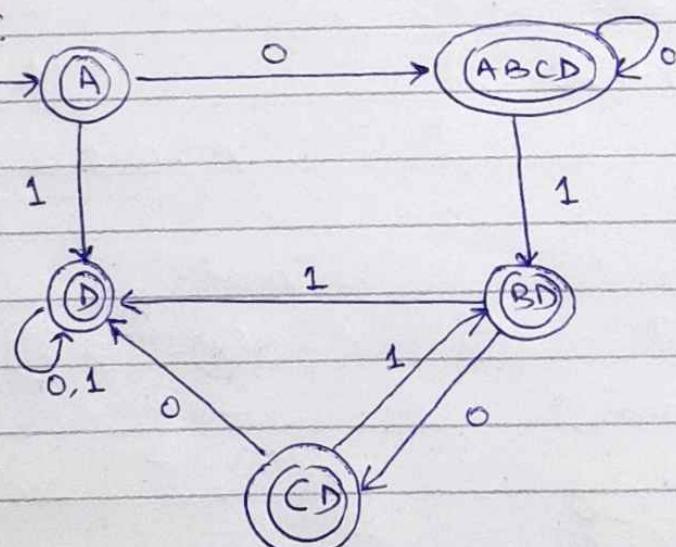
NFA



• NFA to DFA.

	0	1
$\rightarrow [A]$	[ABCD]	[D]
$*[ABCD]$	[ABC'D]	[BD]
$*[D]$	[D]	[D]
$*[BD]$	[CD]	[D]
$*[CD]$	[D]	[BD]

DFA



\rightarrow DFA + Minimal DFA.

→ Regular Language:

A Language is said to be regular if it can be described by a Finite Automata.

For Ex: Non-Regular Language. → Context Free Grammer
 $\text{Language} = \{0^n 1^n \mid n \geq 1\}$

finite automata → Push Down Automata.
 Does not exist.

→ Finite Automata with Output.

Moore's Machine.

$Q, \Sigma, \delta, q_0, \Delta, \lambda$.

$Q \rightarrow$ Finite set of states

$\Sigma \rightarrow$ Input alphabet.

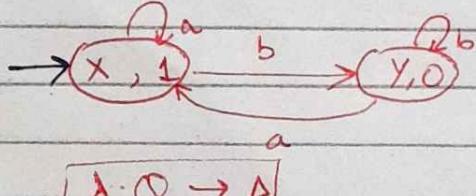
$\delta \rightarrow$ Transition function.

$\delta: Q \times \Sigma \rightarrow Q$

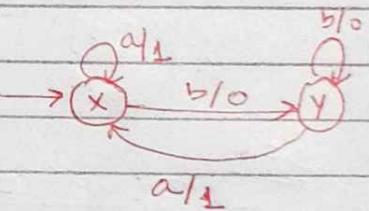
$q_0 \rightarrow$ Initial state

$\Delta \rightarrow$ Output Alphabet.

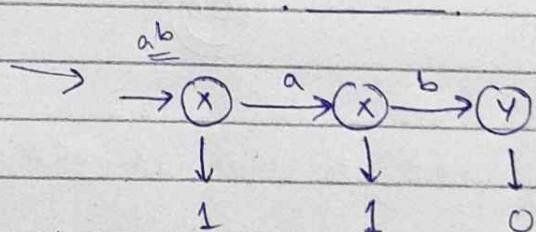
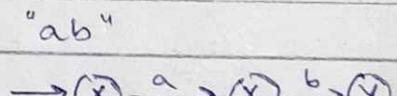
$\lambda \rightarrow$ Output function.



Each state is associated to an output symbol.



$$\boxed{\lambda: Q \times \Sigma \rightarrow \Delta}$$

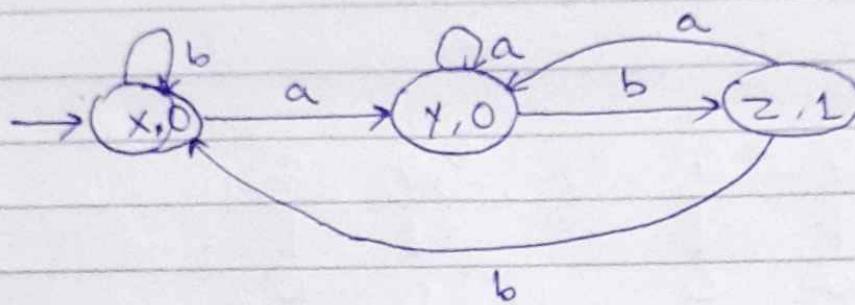


→ Moore's Machine:

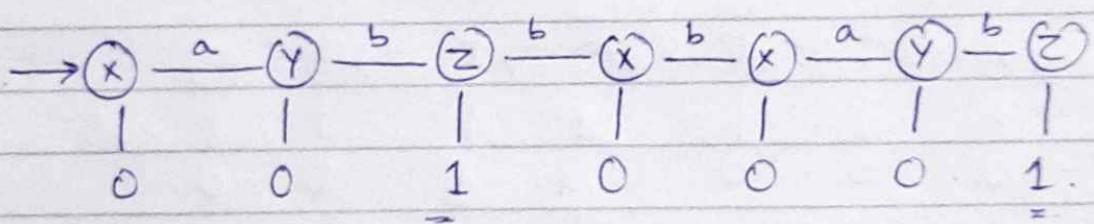
Construct a Moore's Machine that takes set of all strings over $\Sigma = \{a, b\}$ and prints "1" as output for every occurrence of "ab".

Input Alphabet : $\Sigma = \{a, b\}$

Output Alphabet : $\Delta = \{0, 1\}$

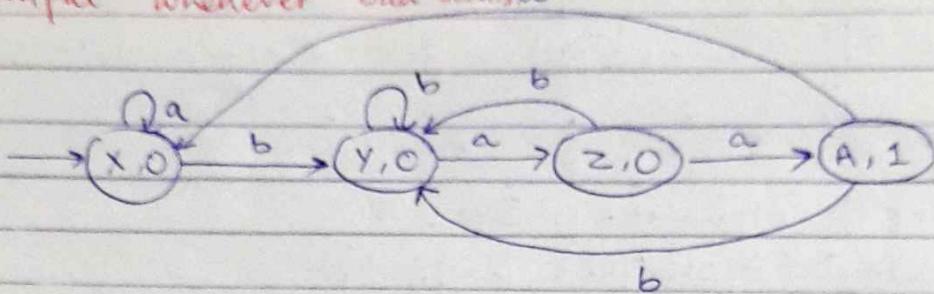


abbb ab

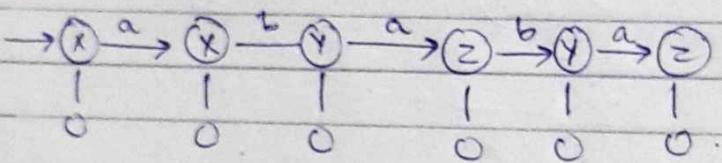


Moore's Machine is not for Accepting String or Non-Accepting String. It is an output generator.

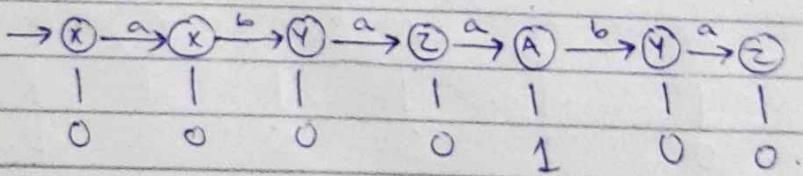
Construct a Moore's Machine that takes set of all strings over $\Sigma = \{a, b\}$ & prints '1' as output whenever "baa" occurs



ababa

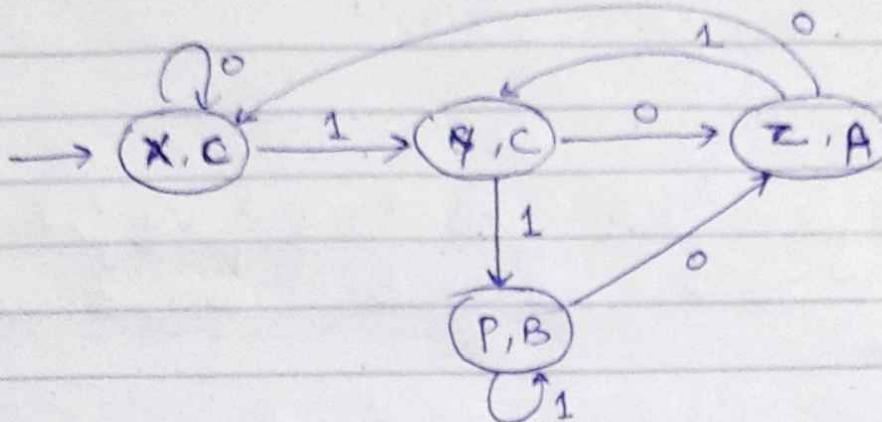


abaaba.

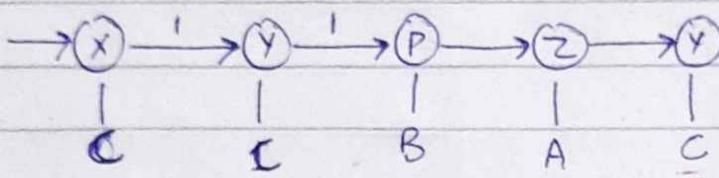


Construct a Moore's Machine that takes set of all strings over $\Sigma = \{0, 1\}$ & prints 'A' as output if the input ends with "10", produces "B" if the strings end with 11 otherwise produces "C".

Input Alphabet $\Sigma = \{0, 1\}$
 Output Alphabet $\Delta = \{A, B, C\}$



• 1101 (Not Ending at 10 or 11)



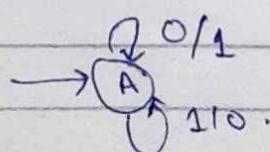
→ Mealy's Machine:

Construct a Mealy's Machine that takes binary number as input and produces 2's Compliment of that number as output.

$$\Sigma = \{0, 1\} \quad \Delta = \{0, 1\}$$

1's Compliment.

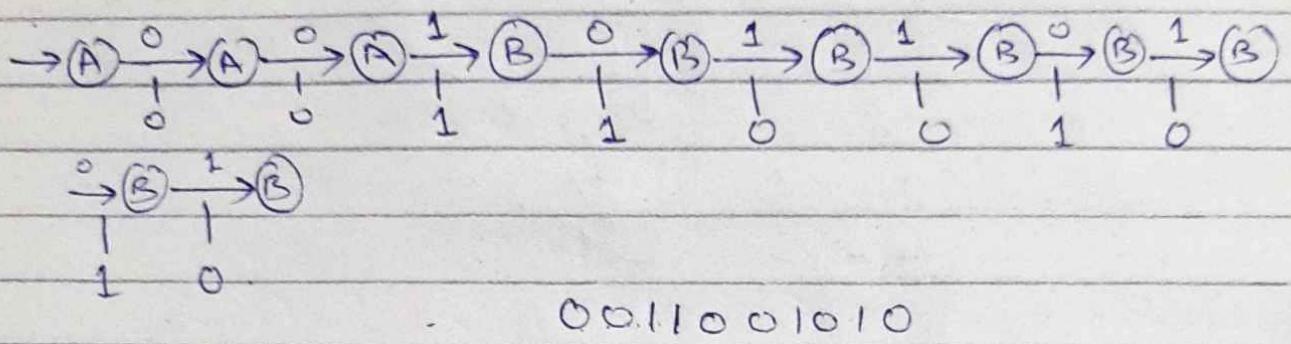
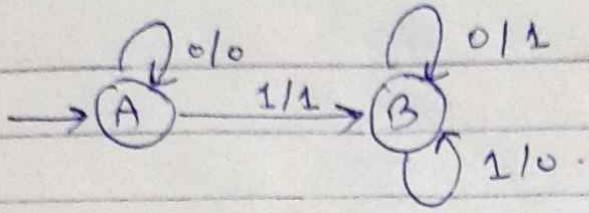
$$101011 \rightarrow \underline{0}10100$$



2's Compliment.

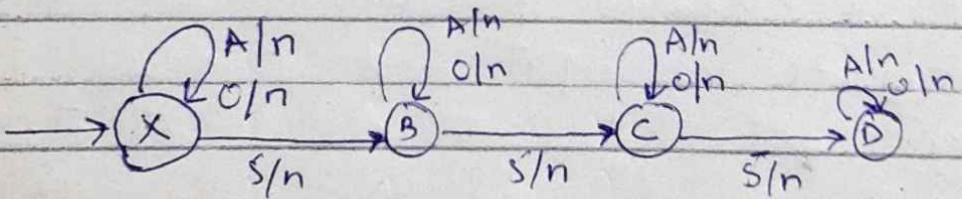
$$101011\underline{0100} \leftarrow \text{Binary}$$

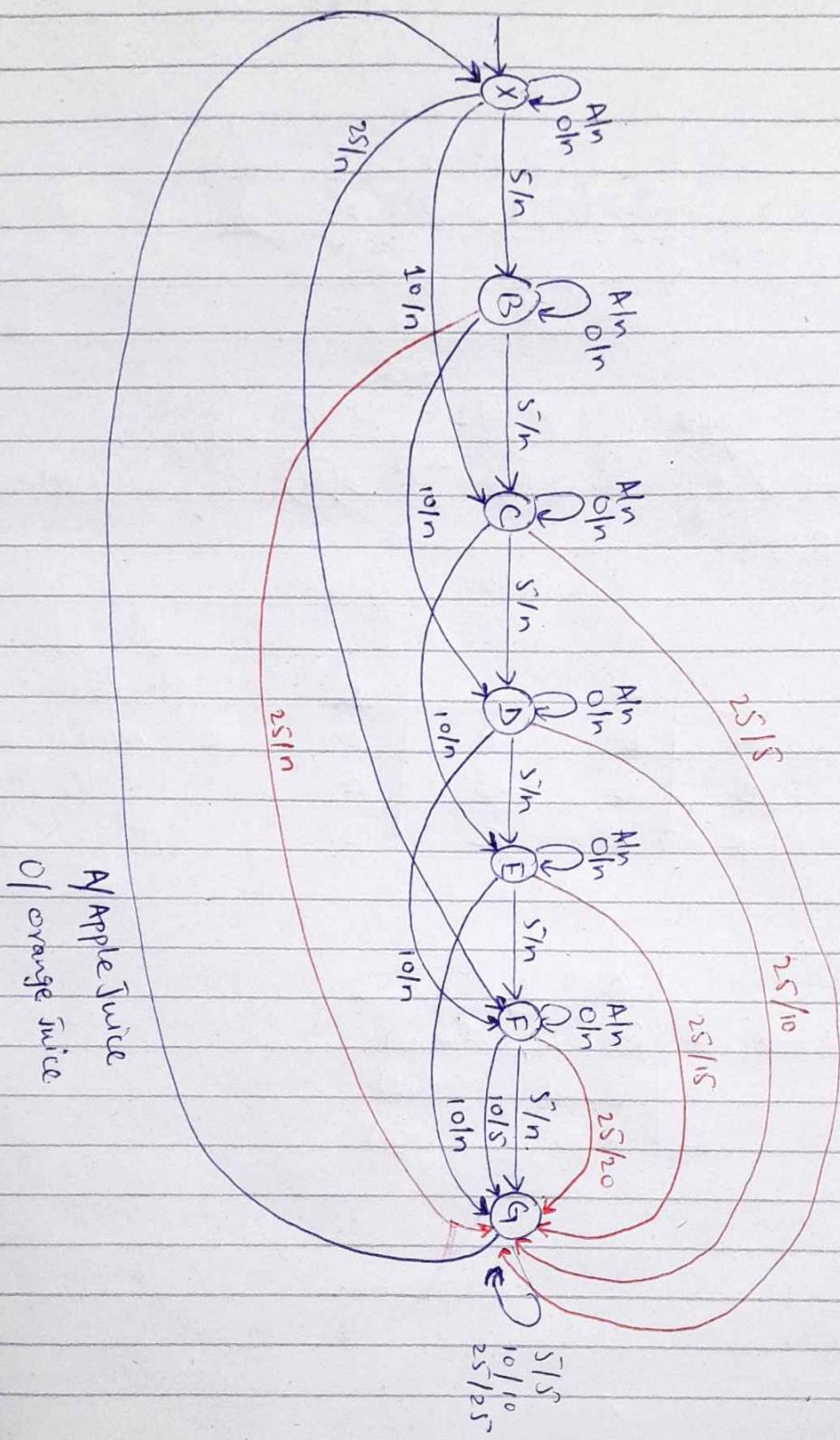
$$0101001\underline{100} \leftarrow \begin{array}{l} 2's \\ \text{Comp.} \end{array}$$



A → Apple Juice
 O → Orange Juice = 30 cents

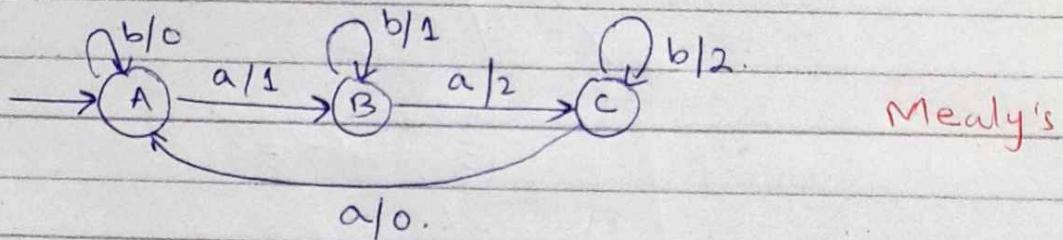
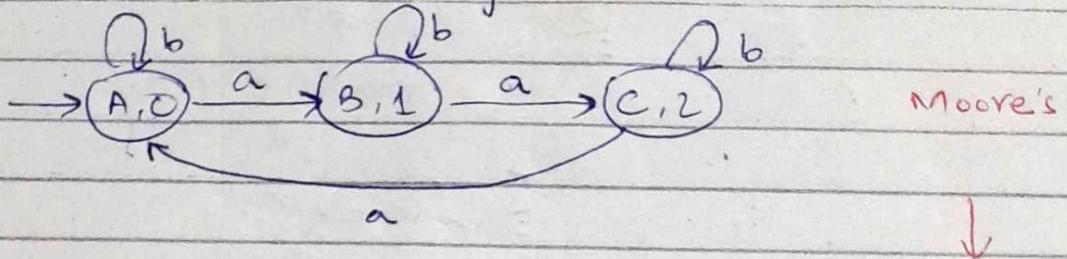
Coin → 5, 10, 25 cents. n → Nothing





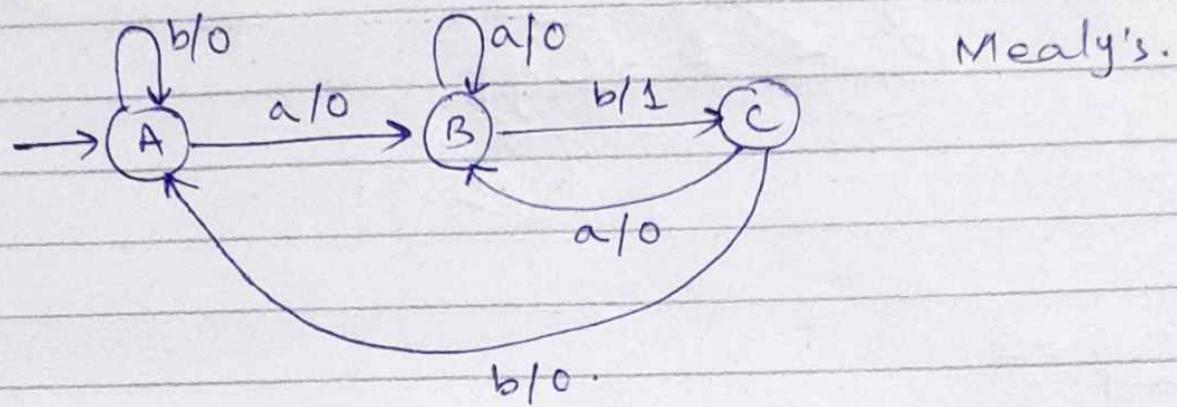
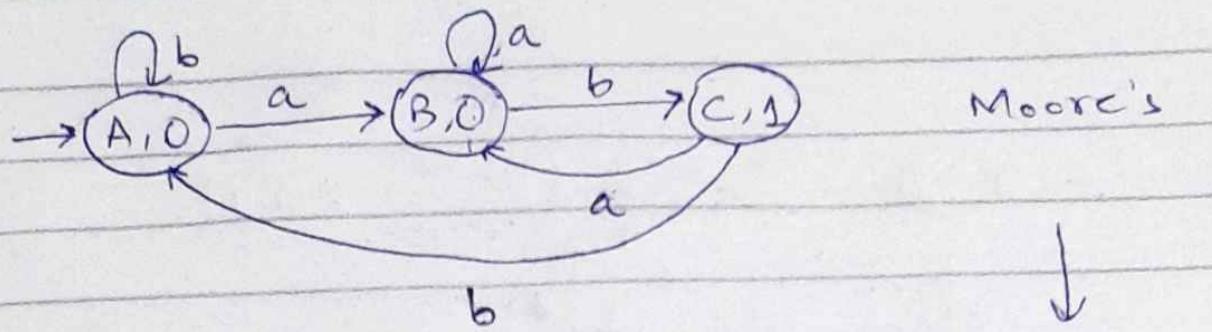
\rightarrow Moore's \leftrightarrow Mealy's.

• Moore's \rightarrow Mealy's.



	a	b	Δ	Moore's Machine Table
\rightarrow A	B	A	0	
B	C	B	1	
C	A	C	2.	

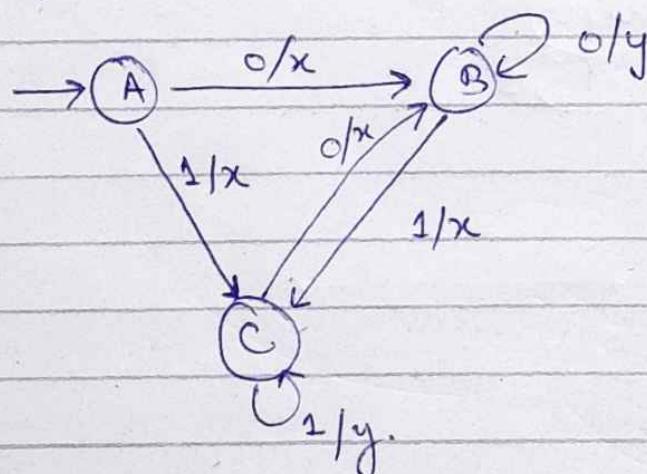
	a	b
\rightarrow A	(B, 1)	(A, 0)
B	(C, 2)	(B, 1)
C	(A, 0)	(C, 2)

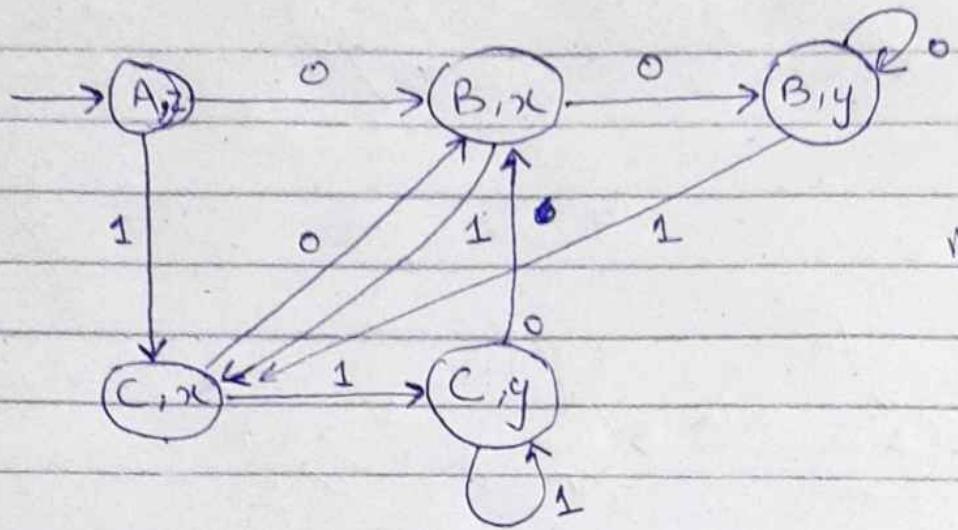


	a	b	Δ
$\rightarrow A$	B	A	0
B	B	C	0
C	B	A	1

	a	b
$\rightarrow A$	(B, 0)	(A, 0)
B	(B, 0)	(C, 1)
C	(B, 0)	(A, 0)

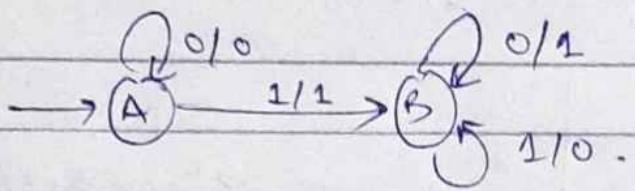
Mealy's \rightarrow Moore's.



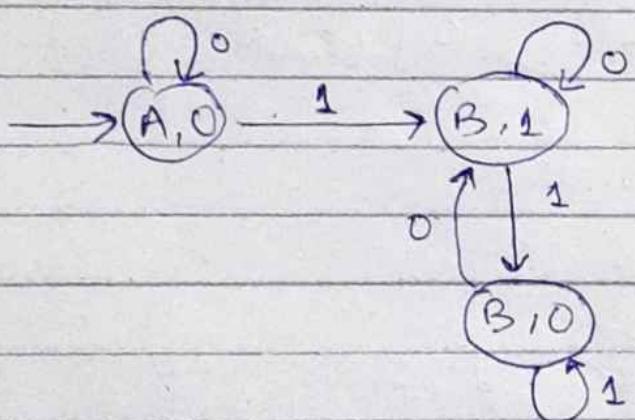


Moore's
Machine.

Exp #2



Mealy's
Machine



↓
Moore's
Machine.