### Chapter 11: Indexing and Hashing

- Basic Concepts
- Ordered Indices
- B<sup>+</sup>-Tree Index Files
- B-Tree Index Files
- Static Hashing
- Dynamic Hashing
- Comparison of Ordered Indexing and Hashing
- Index Definition in SQL
- Multiple-Key Access

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### **Basic Concepts**

- Indexing mechanisms used to speed up access to desired data.
  - E.g. author catalog in library
- Search key attribute or set of attributes used to look up records in a file.
- An index file consists of records (called index entries) of the form

search-key pointer

- Index files are typically much smaller than the original file
- Two basic kinds of indices:
  - Ordered indices: search keys are stored in sorted order
  - Hash indices: search keys are distributed uniformly across "buckets" using a "hash function".

#### **Index Evaluation Metrics**

Indexing techniques evaluated on basis of:

- Access types supported efficiently. E.g.,
  - records with a specified value in an attribute
  - or records with an attribute value falling in a specified range of values.
- Access time
- Insertion time
- Deletion time
- Space overhead

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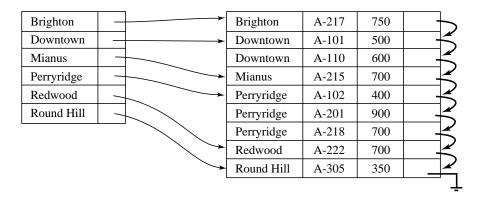
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### **Ordered Indices**

- In an **ordered index**, index entries are stored sorted on the search key value. E.g., author catalog in library.
- **Primary index**: in a sequentially ordered file, the index whose search key specifies the sequential order of the file.
  - Also called clustering index
  - The search key of a primary index is usually but not necessarily the primary key.
- **Secondary index**: an index whose search key specifies an order different from the sequential order of the file. Also called **non-clustering index**.
- Index-sequential file: ordered sequential file with a primary index.

### **Dense Index Files**

 Dense index – index record appears for every search-key value in the file.



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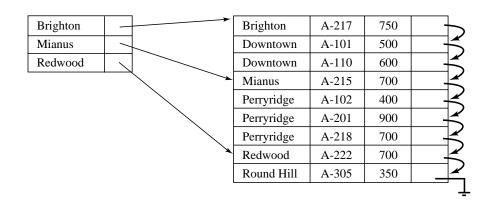
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### Sparse Index Files

- Index records for some search-key values.
- To locate a record with search-key value K we:
  - Find index record with largest search-key value < K</li>
  - Search file sequentially starting at the record to which the index record points
- Less space and less maintenance overhead for insertions and deletions.
- Generally slower than dense index for locating records.
- Good tradeoff: sparse index with an index entry for every block in file, corresponding to least search-key value in the block.

# **Example of Sparse Index Files**



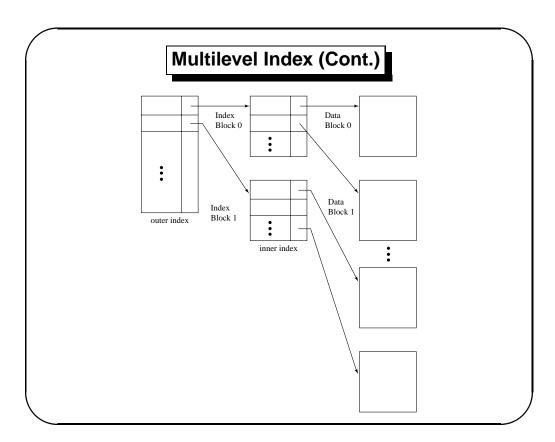
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# Multilevel Index

- If primary index does not fit in memory, access becomes expensive.
- To reduce number of disk accesses to index records, treat primary index kept on disk as a sequential file and construct a sparse index on it.
  - outer index a sparse index of primary index
  - inner index the primary index file
- If even outer index is too large to fit in main memory, yet another level of index can be created, and so on.
- Indices at all levels must be updated on insertion or deletion from the file.



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### **Index Update: Deletion**

- If deleted record was the only record in the file with its particular search-key value, the search-key is deleted from the index also.
- Single-level index deletion:
  - Dense indices deletion of search-key is similar to file record deletion.
  - Sparse indices if an entry for the search key exists in the index, it is deleted by replacing the entry in the index with the next search-key value in the file (in search-key order). If the next search-key value already has an index entry, the entry is deleted instead of being replaced.

#### **Index Update: Insertion**

- Single-level index insertion:
  - Perform a lookup using the search-key value appearing in the record to be inserted.
  - Dense indices if the search-key value does not appear in the index, insert it.
  - Sparse indices if index stores an entry for each block of the file, no change needs to be made to the index unless a new block is created. In this case, the first search-key value appearing in the new block is inserted into the index.
- Multilevel insertion (as well as deletion) algorithms are simple extensions of the single-level algorithms

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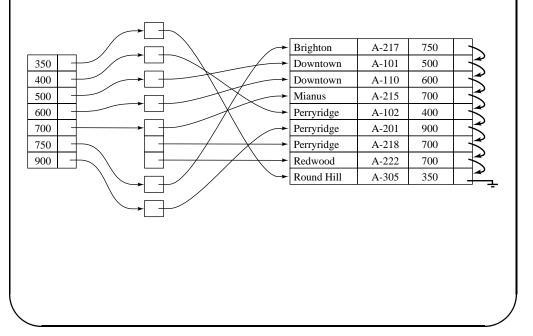
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### **Secondary Indices**

- Frequently, one wants to find all the records whose values in a certain field (which is not the search-key of the primary index) satisfy some condition.
  - Example 1: In the account database stored sequentially by account number, we may want to find all accounts in a particular branch
  - Example 2: as above, but where we want to find all accounts with a specified balance or range of balances
- We can have a secondary index with an index record for each search-key value; index record points to a bucket that contains pointers to all the actual records with that particular search-key value.

### Secondary Index on balance field of account



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### **Primary and Secondary Indices**

- Secondary indices have to be dense.
- Indices offer substantial benefits when searching for records.
- When a file is modified, every index on the file must be updated. Updating indices imposes overhead on database modification.
- Sequential scan using primary index is efficient, but a sequential scan using a secondary index is expensive (each record access may fetch a new block from disk.

### B<sup>+</sup>-Tree Index Files

B<sup>+</sup>-tree indices are an alternative to indexed-sequential files.

- Disadvantage of indexed-sequential files: performance degrades as file grows, since many overflow blocks get created. Periodic reorganization of entire file is required.
- Advantage of B<sup>+</sup>-tree index files: automatically reorganizes itself with small, local, changes, in the face of insertions and deletions. Reorganization of entire file is not required to maintain performance.
- Disadvantage of B<sup>+</sup>-trees: extra insertion and deletion overhead, space overhead.
- Advantages of B<sup>+</sup>-trees outweigh disadvantages, and they are used extensively.

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# B<sup>+</sup>-Tree Index Files (Cont.)

A B+-tree is a rooted tree satisfying the following properties:

- All paths from root to leaf are of the same length
- Each node that is not a root or a leaf has between  $\lceil n/2 \rceil$  and n children.
- A leaf node has between  $\lceil (n-1)/2 \rceil$  and n-1 values
- Special cases: if the root is not a leaf, it has at least 2 children. If the root is a leaf (that is, there are no other nodes in the tree), it can have between 0 and (n-1) values.

### B<sup>+</sup>-Tree Node Structure

Typical node

$  P_1   K_1   P_2   \dots   P_{n-1}   K_{n-1}   P_n$	$P_1$	<i>K</i> <sub>1</sub>	$P_2$		$P_{n-1}$	<i>K</i> <sub>n-1</sub>	$P_n$
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- K<sub>i</sub> are the search-key values
- P<sub>i</sub> are pointers to children (for non-leaf nodes) or pointers to records or buckets of records (for leaf nodes).
- The search-keys in a node are ordered

$$K_1 < K_2 < K_3 < ... < K_{n-1}$$

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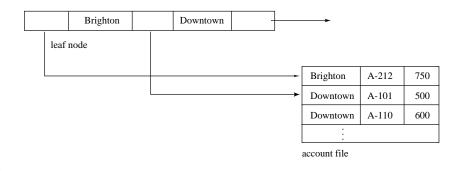
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# Leaf Nodes in B<sup>+</sup>-Trees

Properties of a leaf node:

- For i = 1, 2, ..., n 1, pointer  $P_i$  either points to a file record with search-key value  $K_i$ , or to a bucket of pointers to file records, each record having search-key value  $K_i$ . Only need bucket structure if search-key does not form a primary key.
- If  $L_i$ ,  $L_j$  are leaf nodes and i < j,  $L_i$ 's search-key values are less than  $L_i$ 's search-key values
- P<sub>n</sub> points to next leaf node in search-key order



#### Non-Leaf Nodes in B<sup>+</sup>-Trees

- Non leaf nodes form a multi-level sparse index on the leaf nodes. For a non-leaf node with m pointers:
  - All the search-keys in the subtree to which  $P_1$  points are less than  $K_1$
  - For  $2 \le i \le n 1$ , all the search-keys in the subtree to which  $P_i$  points have values greater than or equal to  $K_{i-1}$  and less than  $K_i$
  - All the search-keys in the subtree to which  $P_m$  points are greater than or equal to  $K_{m-1}$

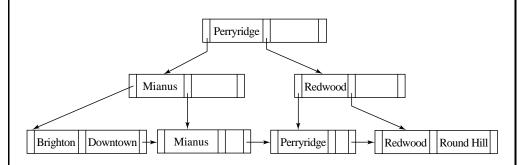
$P_1$ $K_1$ $P_2$		$P_{n-1}$	<i>K</i> <sub>n-1</sub>	Pn
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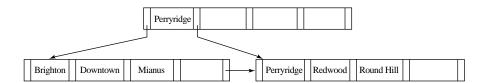
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# Example of a B<sup>+</sup>-tree



B<sup>+</sup>-tree for *account* file (n = 3)

# Example of a B<sup>+</sup>-tree



B<sup>+</sup>-tree for account file (n = 5)

- Leaf nodes must have between 2 and 4 values ( $\lceil (n-1)/2 \rceil$  and n-1, with n=5).
- Non-leaf nodes other than root must have between 3 and 5 children ( $\lceil n/2 \rceil$  and n with n = 5).
- Root must have at least 2 children

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### Observations about B<sup>+</sup>-trees

- Since the inter-node connections are done by pointers, there is no assumption that in the B<sup>+</sup>-tree, the "logically" close blocks are "physically" close.
- The non-leaf levels of the B<sup>+</sup>-tree form a hierarchy of sparse indices.
- The B<sup>+</sup>-tree contains a relatively small number of levels (logarithmic in the size of the main file), thus searches can be conducted efficiently.
- Insertions and deletions to the main file can be handled efficiently, as the index can be restructured in logarithmic time (as we shall see).

#### **Queries on B<sup>+</sup>-Trees**

- Find all records with a search-key value of k.
  - Start with the root node
    - \* Examine the node for the smallest search-key value > k.
    - \* If such a value exists, assume it is  $K_i$ . Then follow  $P_i$  to the child node
    - \* Otherwise  $k \geq K_{m-1}$ , where there are m pointers in the node. Then follow  $P_m$  to the child node.
  - If the node reached by following the pointer above is not a leaf node, repeat the above procedure on the node, and follow the corresponding pointer.
  - Eventually reach a leaf node. If key  $K_i = k$ , follow pointer  $P_i$  to the desired record or bucket. Else no record with search-key value k exists.

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# Queries on B<sup>+</sup>-Trees (Cont.)

- In processing a query, a path is traversed in the tree from the root to some leaf node.
- If there are K search-key values in the file, the path is no longer than [log<sub>[n/2]</sub>(K)].
- A node is generally the same size as a disk block, typically 4 kilobytes, and *n* is typically around 100 (40 bytes per index entry).
- With 1 million search key values and n = 100, at most  $log_{50}(1,000,000) = 4$  nodes are accessed in a lookup.
- Contrast this with a balanced binary tree with 1 million search key values — around 20 nodes are accessed in a lookup
  - above difference is significant since every node access may need a disk I/O, costing around 30 millisecond!

#### Updates on B<sup>+</sup>-Trees: Insertion

- Find the leaf node in which the search-key value would appear
- If the search-key value is already there in the leaf node, record is added to file and if necessary pointer is inserted into bucket.
- If the search-key value is not there, then add the record to the main file and create bucket if necessary. Then:
  - if there is room in the leaf node, insert (search-key value, record/bucket pointer) pair into leaf node at appropriate position.
  - if there is no room in the leaf node, split it and insert (search-key value, record/bucket pointer) pair as discussed in the next slide.

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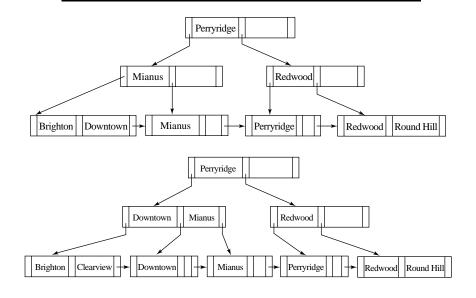
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# Updates on B<sup>+</sup>-Trees: Insertion (Cont.)

- Splitting a node:
  - take the n (search-key value, pointer) pairs (including the one being inserted) in sorted order. Place the first  $\lceil n/2 \rceil$  in the original node, and the rest in a new node.
  - let the new node be p, and let k be the least key value in p.
     Insert (k, p) in the parent of the node being split. If the parent is full, split it and propagate the split further up.
- The splitting of nodes proceeds upwards till a node that is not full is found. In the worst case the root node may be split increasing the height of the tree by 1.

### Updates on B<sup>+</sup>-Trees: Insertion (Cont.)



B+-Tree before and after insertion of "Clearview"

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# Updates on B+-Trees: Deletion

- Find the record to be deleted, and remove it from the main file and from the bucket (if present)
- Remove (search-key value, pointer) from the leaf node if there is no bucket or if the bucket has become empty
- If the node has too few entries due to the removal, and the entries in the node and a sibling fit into a single node, then
  - Insert all the search-key values in the two nodes into a single node (the one on the left), and delete the other node.
  - Delete the pair  $(K_{i-1}, P_i)$ , where  $P_i$  is the pointer to the deleted node, from its parent, recursively using the above procedure.

### **Updates on B<sup>+</sup>-Trees: Deletion**

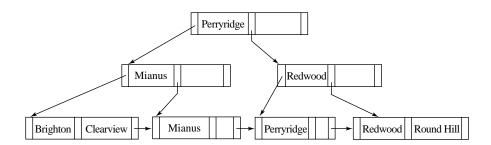
- Otherwise, if the node has too few entries due to the removal, and the entries in the node and a sibling fit into a single node, then
  - Redistribute the pointers between the node and a sibling such that both have more than the minimum number of entries.
  - Update the corresponding search-key value in the parent of the node.
- The node deletions may cascade upwards till a node which has \[ n/2 \] or more pointers is found. If the root node has only one pointer after deletion, it is deleted and the sole child becomes the root.

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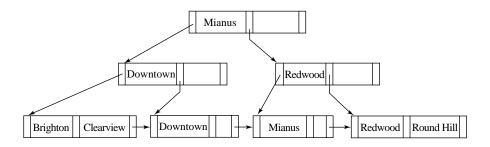
# **Examples of B<sup>+</sup>-Tree Deletion**



Result after deleting "Downtown" from account

• The removal of the leaf node containing "Downtown" did not result in its parent having too little pointers. So the cascaded deletions stopped with the deleted leaf node's parent.

### Examples of B<sup>+</sup>-Tree Deletion (Cont.)



Deletion of "Perryridge" instead of "Downtown"

 The deleted "Perryridge" node's parent became too small, but its sibling did not have space to accept one more pointer. So redistribution is performed. Observe that the root node's search-key value changes as a result.

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# B<sup>+</sup>-Tree File Organization

- Index file degradation problem is solved by using B<sup>+</sup>-Tree Indices. Data file degradation problem is solved by using B<sup>+</sup>-Tree File Organization.
- The leaf nodes in a B<sup>+</sup>-tree file organization store records, instead of pointers.
- Since records are large than pointers, the maximum number of records that can be stored in a leaf node is less than the number of pointers in a nonleaf node.
- Leaf nodes are still required to be half full.
- Insertion and deletion are handled in the same way as insertion and deletion of entries in a B<sup>+</sup>-tree index.
- Good space utilization is important since records use more space than pointers. To improve space utilization, involve more sibling nodes in redistribution during splits and merges.

### **B-Tree Index Files**

- Similar to B<sup>+</sup>-tree, but B-tree allows search-key values to appear only once; eliminates redundant storage of search keys.
- Search keys in nonleaf nodes appear nowhere else in the B-tree; an additional pointer field for each search key in a nonleaf node must be included.
- Generalized B-tree leaf node

<i>P</i> <sub>1</sub>	<i>K</i> <sub>1</sub>	$P_2$		$P_{n-1}$	$K_{n-1}$	Pn
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 Nonleaf node – pointers B<sub>i</sub> are the bucket or file record pointers.

<i>P</i> <sub>1</sub>	$B_1$	<i>K</i> <sub>1</sub>	$P_2$	$B_2$	$K_2$		$P_{m-1}$	$B_{m-1}$	$K_{m-1}$	$P_{m}$
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# B-Tree Index Files (Cont.)

- Advantages of B-Tree indices:
  - May use less tree nodes than a corresponding B<sup>+</sup>-Tree.
  - Sometimes possible to find search-key value before reaching leaf node.
- Disadvantages of B-Tree indices:
  - Only small fraction of all search-key values are found early
  - Non-leaf nodes are larger, so fan-out is reduced. Thus
     B-Trees typically have greater depth than corresponding
     B+-Tree
  - Insertion and deletion more complicated than in B<sup>+</sup>-Trees
  - Implementation is harder than B+-Trees.
- Typically, advantages of B-Trees do not outweigh disadvantages.

### Static Hashing

- A bucket is a unit of storage containing one or more records (a bucket is typically a disk block). In a hash file organization we obtain the bucket of a record directly from its search-key value using a hash function.
- Hash function *h* is a function from the set of all search-key values *K* to the set of all bucket addresses *B*.
- Hash function is used to locate records for access, insertion as well as deletion.
- Records with different search-key values may be mapped to the same bucket; thus entire bucket has to be searched sequentially to locate a record.

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### **Hash Functions**

- Worst hash function maps all search-key values to the same bucket; this makes access time proportional to the number of search-key values in the file.
- An ideal hash function is *uniform*, i.e. each bucket is assigned the same number of search-key values from the set of *all* possible values.
- Ideal hash function is *random*, so each bucket will have the same number of records assigned to it irrespective of the *actual distribution* of search-key values in the file.
- Typical hash functions perform computation on the internal binary representation of the search-key. For example, for a string search-key, the binary representations of all the characters in the string could be added and the sum modulo number of buckets could be returned.

bucket 0			bucket 5		
			Perryridge	A-102	400
			Perryridge	A-201	900
			Perryridge	A-218	700
bucket 1			bucket 6		
bucket 2			bucket 7		
			Mianus	A-215	700
bucket 3			bucket 8		
Brighton	A-217	750	Downtown	A-101	500
Round Hill	A-305	350	Downtown	A-110	600
bucket 4			bucket 9		
Redwood	A-222	700			

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# **Example of Hash File Organization (Cont.)**

Hash file organization of *account* file, using *branch-name* as key. (See figure in previous slide.)

- There are 10 buckets,
- The binary representation of the *i*th character is assumed to be the integer *i*.
- The hash function returns the sum of the binary representations of the characters modulo 10.

### Handling of Bucket Overflows

- Bucket overflow can occur because of
  - Insufficient buckets
  - Skew in distribution of records. This can occur due to two reasons:
    - \* multiple records have same search-key value
    - chosen hash function produces non-uniform distribution of key values
- Although the probability of bucket overflow can be reduced, it cannot be eliminated; it is handled by using *overflow buckets*.
- Overflow chaining the overflow buckets of a given bucket are chained together in a linked list
- Above scheme is called closed hashing. An alternative, called open hashing, is not suitable for database applications.

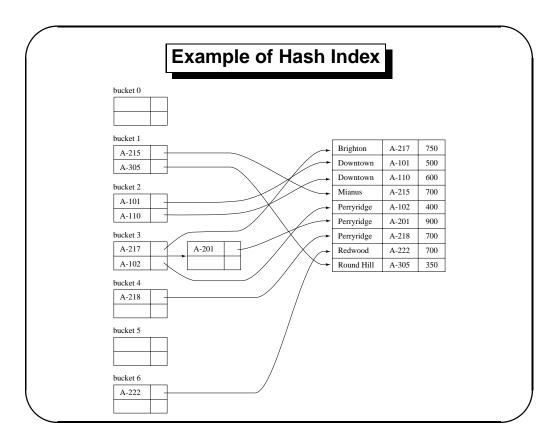
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### Hash Indices

- Hashing can be used not only for file organization, but also for index-structure creation. A hash index organizes the search keys, with their associated record pointers, into a hash file structure.
- Hash indices are always secondary indices if the file itself is organized using hashing, a separate primary hash index on it using the same search-key is unnecessary. However, we use the term hash index to refer to both secondary index structures and hash organized files.



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### **Deficiencies of Static Hashing**

- In static hashing, function *h* maps search-key values to a fixed set *B* of bucket addresses.
  - Databases grow with time. If initial number of buckets is too small, performance will degrade due to too much overflows.
  - If file size at some point in the future is anticipated and number of buckets allocated accordingly, significant amount of space will be wasted initially.
  - If database shrinks, again space will be wasted.
  - One option is periodic re-organization of the file with a new hash function, but it is very expensive.
- These problems can be avoided by using techniques that allow the number of buckets to be modified dynamically.

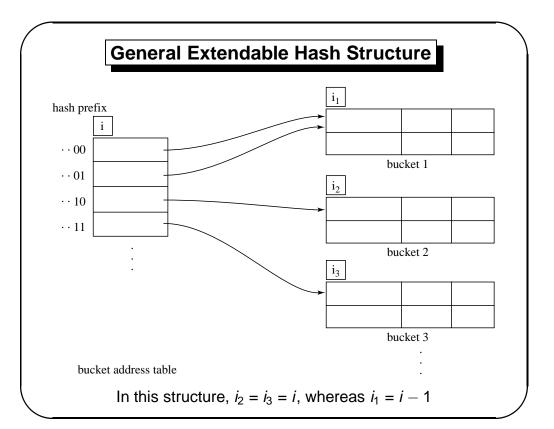
### Dynamic Hashing

- Good for database that grows and shrinks in size
- Allows the hash function to be modified dynamically
- Extendable hashing one form of dynamic hashing
  - Hash function generates values over a large range typically b-bit integers, with b = 32.
  - At any time use only a prefix of the hash function to index into a table of bucket addresses. Let the length of the prefix be i bits,  $0 \le i \le 32$
  - Initially i = 0
  - Value of *i* grows and shrinks as the size of the database grows and shrinks.
  - Actual number of buckets is  $< 2^i$ , and this also changes dynamically due to coalescing and splitting of buckets.

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#### **Use of Extendable Hash Structure**

- Multiple entries in the bucket address table may point to a bucket. Each bucket j stores a value i<sub>j</sub>; all the entries that point to the same bucket have the same values on the first i<sub>i</sub> bits.
- To locate the bucket containing search-key K<sub>i</sub>:
  - 1. Compute  $h(K_i) = X$
  - 2. Use the first *i* high order bits of *X* as a displacement into bucket address table, and follow the pointer to appropriate bucket
- To insert a record with search-key value K<sub>I</sub>, follow same procedure as look-up and locate the bucket, say j.
   If there is room in the bucket j insert record in the bucket. Else the bucket must be split and insertion re-attempted. (See next slide.)

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### **Updates in Extendable Hash Structure**

To split a bucket j when inserting record with search-key value  $K_l$ :

- If  $i > i_j$  (more than one pointer to bucket j)
  - allocate a new bucket z, and set  $i_j$  and  $i_z$  to the old  $i_j$ +1.
  - make the second half of the bucket address table entries pointing to j to point to z
  - remove and reinsert each record in bucket j.
  - recompute new bucket for  $K_l$  and insert record in the bucket (further splitting is required if the bucket is still full)
- If  $i = i_j$  (only one pointer to bucket j)
  - increment *i* and double the size of the bucket address table.
  - replace each entry in the table by two entries that point to the same bucket.
  - recompute new bucket address table entry for K<sub>I</sub>. Now
     i<sub>i</sub>, so use the first case above.

### Updates in Extendable Hash Structure (Cont.)

- When inserting a value, if the bucket is full after several splits (that is, i reaches some limit b) create an overflow bucket instead of splitting bucket entry table further.
- To delete a key value, locate it in its bucket and remove it. The bucket itself can be removed if it becomes empty (with appropriate updates to the bucket address table). Coalescing of buckets and decreasing bucket address table size is also possible.

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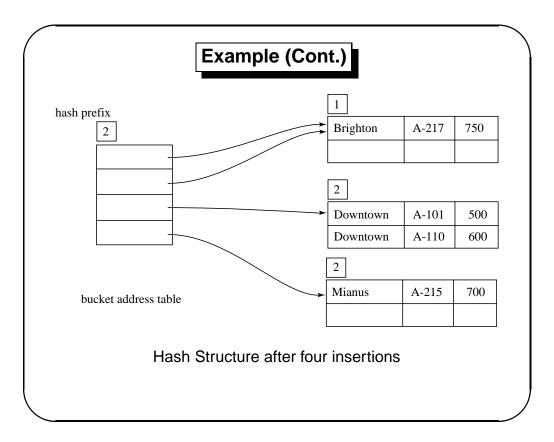
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### **Use of Extendable Hash Structure: Example**

h(branch-name) branch-name 0010 1101 1111 1011 0010 1100 0011 0000 Brighton Downtown 1010 0011 1010 0000 1100 0110 1001 1111 Mianus 1100 0111 1110 1101 1011 1111 0011 1010 Perryridge 1111 0001 0010 0100 1001 0011 0110 1101 Redwood 0011 0101 1010 0110 1100 1001 1110 1011 Round Hill 1101 1000 0011 1111 1001 1100 0000 0001 hash prefix 0 bucket 1 bucket address table

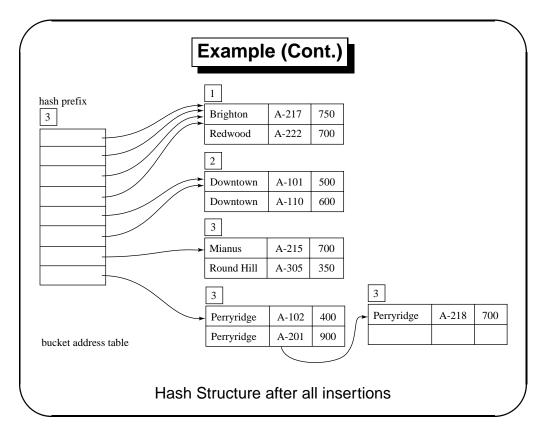
Initial Hash Structure, Bucket size = 2



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### Comparison of Ordered Indexing and Hashing

#### Issues to consider:

- Cost of periodic re-organization
- Relative frequency of insertions and deletions
- Is it desirable to optimize average access time at the expense of worst-case access time?
- Expected type of queries:
  - Hashing is generally better at retrieving records having a specified value of the key.
  - If range queries are common, ordered indices are to be preferred

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# **Index Definition in SQL**

Create an index

E.g.: **create index** *b-index* **on** *branch(branch-name)* 

- Use create unique index to indirectly specify and enforce the condition that the search key is a candidate key.
- To drop an index

drop index <index-name>

### **Multiple-Key Access**

- Use multiple indices for certain types of queries.
- Example:

select account-number
from account
where branch-name = "Perryridge" and balance = 1000

- Possible strategies for processing query using indices on single attributes:
  - 1. Use index on *branch-name* to find Perryridge records; test *balance* = 1000.
  - 2. Use index on *balance* to find accounts with balances of \$1000; test *branch-name* = "Perryridge."
  - Use branch-name index to find pointers to all records pertaining to the Perryridge branch. Similarly use index on balance. Take intersection of both sets of pointers obtained.

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### **Indices on Multiple Attributes**

Suppose we have an index on combined search-key (*branch-name*, *balance*).

With the where clause
 where branch-name = "Perryridge" and balance = 1000
 the index on the combined search-key will fetch only records
 that satisfy both conditions.
 Using separate indices is less efficient — we may fetch many

records (or pointers) that satisfy only one of the conditions.

- Can also efficiently handle
   where branch-name = "Perryridge" and balance < 1000</li>
- But cannot efficiently handle
   where branch-name < "Perryridge" and balance = 1000</li>
   May fetch many records that satisfy the first but not the second condition.

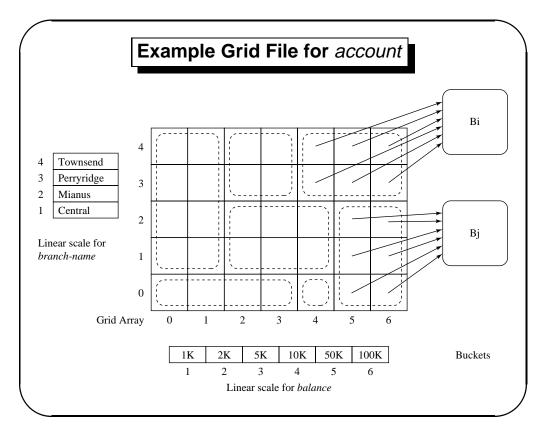
# **Grid Files**

- Structure used to speed the processing of general multiple search-key queries involving one or more comparison operators.
- The grid file has a single grid array and one linear scale for each search-key attribute. The grid array has number of dimensions equal to number of search-key attributes.
- Multiple cells of grid array can point to same bucket
- To find the bucket for a search-key value, locate the row and column of the its cell using the linear scales and follow pointer
- If a bucket becomes full, new bucket can be created if more than one cell points to it. If only one cell points to it, overflow bucket needs to be created

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# **Grid Files (Cont.)**

- A grid file on two attributes A and B can handle queries of the form (a<sub>1</sub> ≤ A ≤ a<sub>2</sub>), (b<sub>1</sub> ≤ B ≤ b<sub>2</sub>) as well as (a<sub>1</sub> ≤ A ≤ a<sub>2</sub> ∧ b<sub>1</sub> ≤ B ≤ b<sub>2</sub>) with reasonable efficiency.
- E.g., to answer  $(a_1 \le A \le a_2 \land b_1 \le B \le b_2)$ , use linear scales to find candidate grid array cells, and look up all the buckets pointed to from those cells.
- Linear scales must be chosen to uniformly distribute records across cells. Otherwise there will be too many overflow buckets.
- Periodic re-organization will help. But reorganization can be very expensive.
- Space overhead of grid array can be high.
- R-trees (Chapter 21) are an alternative

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# **Partitioned Hashing**

 Hash values are split into segments that depend on each attribute of the search-key.

 $(A_1, A_2, ..., A_n)$  for n attribute search-key

• Example: n = 2, for *customer*, search-key being (*customer-street*, *customer-city*)

search-key value	hash value
(Main, Harrison)	101 111
(Main, Brooklyn)	101 001
(Park, Palo Alto)	010 010
(Spring, Brooklyn)	001 001
(Alma, Palo Alto)	110 010

• To answer equality query on single attribute, need to look up multiple buckets. Similar in effect to grid files.