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①

ASSIGNMENT: 03

Q3.1) What is 5ED4-07A4 when these values represent unsigned 16-bit hexadecimal numbers?  
The result should be written in hexadecimal.  
Show your work.

Ans

First lets convert the hexadecimal Numbers  
to the binary number

$$(5ED4)_{16} = (0101\ 1110\ 1101\ 0100)_2$$

$$(07A4)_{16} = (0000\ 0111\ 1010\ 0100)_2$$

Taking 2's compliment of  $(07A4)_{16}$ , we get

$$\begin{array}{r} 0000\ 0111\ 1010\ 0100 \\ 1111\ 1000\ 0101\ 1011 \\ + 1 \\ \hline \end{array}$$

$$1111\ 1000\ 0101\ 1100)_2$$

Adding the Numbers we get

$$\begin{array}{r} 0101\ 1110\ 1101\ 0100 \\ 1111\ 1000\ 0101\ 1100 \\ \hline \end{array}$$

$$\boxed{\begin{array}{r} 0101\ 0111\ 0011\ 0000 \\ \hline \end{array}}_2$$

Hence, After converting to Hex, we get 5F30<sub>16</sub>

Q2.2 What is 5ED4-07A4 when these values represent signed 16-bit hexadecimal numbers stored in sign-magnitude format? The result should be written in hexadecimal. Show your work.

Ans Let us convert the Hexadecimcal to Binary.

$$5ED4 = 0101\ 1110\ 1101\ 0100$$

07A4 = 0000 0111 1010 0100.

Neither one have a sign bit set, so the math is same as unsigned math.

The subtraction will as follows:-

$$\begin{array}{r}
 \begin{array}{r} 5 \\ - 0 \\ \hline 5 \end{array} \quad \begin{array}{r} 0101 \\ 0000 \\ \hline 0101 \end{array} \quad \begin{array}{r} 1110 \\ 0111 \\ \hline 1010 \end{array} \quad \begin{array}{r} 1101 \\ 1010 \\ \hline 1010 \end{array} \quad \begin{array}{r} 0100 \\ 0000 \\ \hline 0 \end{array} \\
 \end{array}$$

After converting into Hex, we get  $(5730)_{16}$

(2)

Q3: Convert 5ED4 into a binary number. What makes base 16 (Hex) an attractive numbering system for representing values in computers?

Ans Converting the 5ED4 in Binary we get,

$$(5ED4)_{16} = (0101 \ 1110 \ 1101 \ 0100)_2$$

Base 16 is an attractive numbering system for representing values in computer because

- ①  $16 = 2^4$ , so each digit in a hexadecimal number displays 4 bits. Due to this, a byte (8 bits) can be specified by exactly 2 hex digits. This makes the representation easy & accurate.
- ② It allows large numbers to be displayed in less digits, for example, in binary the decimal No 1000 is written as 1111101000 which is 10 digits and the same number in hex is written as 3E8 which is just 3 digits.

Q3.8) Assume 185 and 122 are signed 8-bit decimal integers stored in sign magnitude format. calculate  $185 \cancel{+} 122$ . Is there overflow, underflow, or neither.

Ans

Let us convert the decimal in binary,

$$(185)_{10} = \begin{array}{r} 10010111_2 \\ - (122)_{10} = 01111010 \\ \hline (00111111)_2 \end{array}$$

$$(00111111)_2 = (63)_{10}$$

As, we are subtracting the operands of the same sign, we end up by adding operands of different sign. Hence overflow does not occur in this case.

(3)

Q3.9 Assume 151 and 214 are signed 8 bit decimal integers stored in two's complement format. Calculate  $151 + 214$  using saturating arithmetic. The result should be written in decimal. Show your work.

Ans Convert the decimal in binary.

$$151 = (10010111)_2$$

$$214 = (11010110)_2$$

Now, taking two's complements of each, we get

$$\begin{array}{r} 151 = 10010111 \\ \text{1's complement} = 01101000 \\ \text{Add 1} \qquad \qquad \qquad | \\ \hline \text{2's complement} = \overline{01101001} \end{array} \qquad \begin{array}{r} 214 = 11010110 \\ \text{00101001} \\ + \qquad \qquad \qquad | \\ \hline \overline{00101010} \end{array}$$

Now adding  $151 + 214$

$$\begin{array}{r} 01101001 \\ 00101010 \\ \hline 10010011 \end{array}$$

Since, the sign bit set it means the result is negative. In  $A+B$ , when  $A \geq 0$  and  $B \geq 0$  and the result is negative means there is overflow. So the result cannot be determined correctly in decimal.

Q3.10 Assume 151 and 214 are signed 8-bit integers calculate 151 stored in 2's complement format. Calculate  $151 - 214$  using saturating arithmetic. The result should be written in decimal. Show your work?

Ans. Converting decimal into binary we get,

$$(151)_{10} = 10010111$$

$$(214)_{10} = 11010110$$

Now taking 2's complement of each,

$$(151)_{10} = 10010111$$

$$\text{1's complement} = 01101000$$

$$\text{Add } 1 \quad +$$

$$\begin{array}{r} \\ \hline \text{2's complement} & 01101001 \end{array}$$

$$(214)_{10} = 11010110$$

$$\begin{array}{r} 00101001 \\ + 1 \\ \hline \end{array}$$

$$00101010$$

Now performing subtraction we get,

$$\begin{array}{r} 151 & 01101001 \\ - 214 & 00101010 \\ \hline 00111111 \end{array}$$

The sign bit is not set. Hence it is a positive No. The decimal No is  $(63)_{10}$

Q3.11 Assume 151 and 214 are unsigned 8 bit integers. Calculate  $151 + 214$  using saturating arithmetic. The result should be written in decimal. Show your work? (4)

Converting Decimal to binary we get,

$$(151)_{10} = (10010111)_2$$

$$(214)_{10} = (11010110)_2$$

Performing the Addition we get.

$$(151)_{10} = 10010111$$

$$\begin{array}{r} (214)_{10} = 11010110 \\ \hline \end{array}$$

As it is the unsigned bit, the overflow are ignored.

Hence the result is  $(109)_{10}$

Q3.20

What decimal number does the bit pattern represent  $0x0C000000$ , if it is ~~an~~ a 2's complement integer? An unsigned integer?

Ans First we need to convert the No. in binary.

$$0x0C000000 = 00001100\ 0000\ 0000\ 0000\ 0000\ 0000$$

(a) Taking 2's complement we get.

$$0x0C000000 = 0000\ 1100\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000$$

$$\text{1}^{\text{st}} \text{ complement} = 1111\ 0011\ 1111\ 1111\ 1111\ 1111\ 1111 \\ + 1$$

$$\text{Add } 1 = \overline{1111\ 0100\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000}$$

As the sign bit is set it is a -ve No.

The decimal equivalent is =  $-(4093640704)_{10}$

(b) If it is an unsigned Integer, we get

$$0x0C000000 = 0000\ 1100\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000$$

$$= (201326592)_{10}$$

Q3.21 If the bit Patter 0x0000000 is placed into the Instruction Register, what MIPS instruction will be executed?

Ans To place 0x00000 into the instruction

Register, the MIPS instruction is

add \$t1, \$t1, 0x0C000000

Q 3.22 What decimal No. does the bit pattern 0x00000 represent if it is a floating point number? Use IEEE 754 standard.

Ans) Convert 0x0000000 into binary we get  
= 0000 0000 0000 0000 0000 0000 0000

By using IEEE 754 standard-  
 $= (-1^{\text{sign}}) * (1 + \text{fraction}) * 2^{\text{Exponent - bias}}$

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$$= (-1)^{\circ} * (1 \pm 0) * ?$$

$$= (-1) * (1+0) * \angle$$

$$(-1) * (1) * 2^{-103}$$

$$= (-1)^0 * (1) * 2^{-105}$$

Decimal value = 9.8607613e-32