In this lab, you will:

examine the implementation and utilize the cost function for logistic regression.

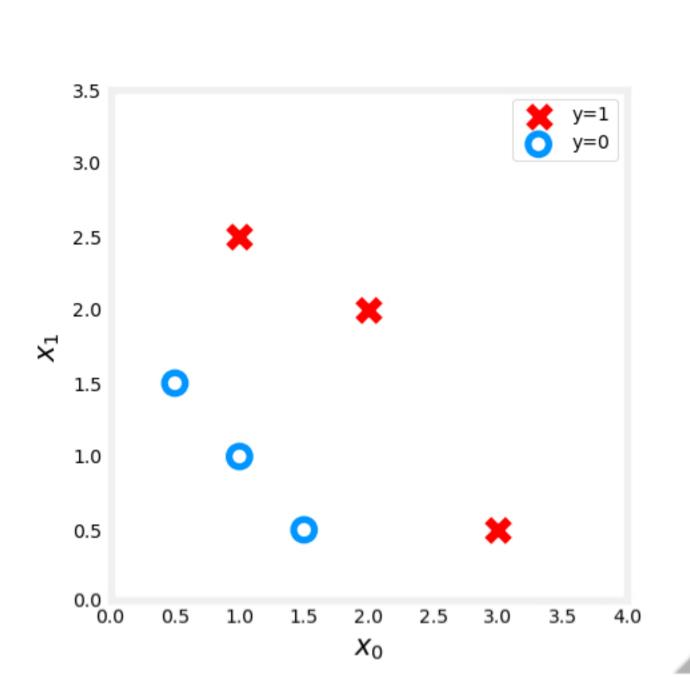
```
In [1]: import numpy as np
           %matplotlib widget
          import matplotlib.pyplot as plt
          from lab_utils_common import plot_data, sigmoid, dlc
plt.style.use('./deeplearning.mplstyle')
```

Dataset

Let's start with the same dataset as was used in the decision boundary lab.

We will use a helper function to plot this data. The data points with label y = 1 are shown as red crosses, while the data points with label y = 0 are shown as blue circles.

In [3]: fig,ax = plt.subplots(1,1,figsize=(4,4)) plot_data(X_train, y_train, ax) # Set both axes to be from 0-4 ax.axis([0, 4, 0, 3.5]) ax.set_ylabel('\$x_1\$', fontsize=12) ax.set_xlabel('\$x_0\$', fontsize=12) plt.show()



Cost function

In a previous lab, you developed the logistic loss function. Recall, loss is defined to apply to one example. Here you combine the losses to form the cost, which includes all the examples.

Recall that for logistic regression, the cost function is of the form

$$J(\mathbf{w}, b) = \frac{1}{m} \sum_{i=0}^{m-1} \left[loss(f_{\mathbf{w}, b}(\mathbf{x}^{(i)}), \mathbf{y}^{(i)}) \right]$$
(1)

where

• $loss(f_{\mathbf{w},b}(\mathbf{x}^{(i)}), \mathbf{y}^{(i)})$ is the cost for a single data point, which is:

$$loss(f_{\mathbf{w},b}(\mathbf{x}^{(i)}),y^{(i)}) = -y^{(i)}\log\left(f_{\mathbf{w},b}\left(\mathbf{x}^{(i)}\right)\right) - \left(1-y^{(i)}\right)\log\left(1-f_{\mathbf{w},b}\left(\mathbf{x}^{(i)}\right)\right)$$
• where m is the number of training examples in the data set and:
$$f_{\mathbf{w},b}(\mathbf{x}^{(i)}) = g(z^{(i)}) \tag{3}$$

$$f_{\mathbf{w},b}(\mathbf{x}^{(i)}) = g(z^{(i)})$$

$$z^{(i)} = \mathbf{w} \cdot \mathbf{x}^{(i)} + b$$
(4)

$$g(z^{(i)}) = \frac{1}{1 + e^{-z^{(i)}}}$$
 (5)

Code Description

The algorithm for compute_cost_logistic loops over all the examples calculating the loss for each example and accumulating the total.

number of training examples.

Note that the variables X and y are not scalar values but matrices of shape (m, n) and (m, n) respectively, where n is the number of features and m is the

```
In [4]: def compute_cost_logistic(X, y, w, b):
            Computes cost
            Args:
              X (ndarray (m,n)): Data, m examples with n features
              y (ndarray (m,)) : target values
              w (ndarray (n,)) : model parameters
              b (scalar)
                              : model parameter
            Returns:
              cost (scalar): cost
            m = X.shape[0]
            cost = 0.0
            for 1 in range(m):
                z_i = np.dot(X[i],w) + b
                f_{wb_i} = sigmoid(z_i)
                cost += -y[i]*np.log(f_wb_i) - (1-y[i])*np.log(1-f_wb_i)
            cost = cost / m
            return cost
        Check the implementation of the cost function using the cell below.
```

In [5]: w_tmp = np.array([1,1]) $b_{tmp} = -3$

```
print(compute_cost_logistic(X_train, y_train, w_tmp, b_tmp))
0.36686678640551745
```

Expected output: 0.3668667864055175

Example

Now, let's see what the cost function output is for a different value of w. • In a previous lab, you plotted the decision boundary for b=-3, $w_0=1$, $w_1=1$. That is, you had b=-3, w=np.array([1,1]).

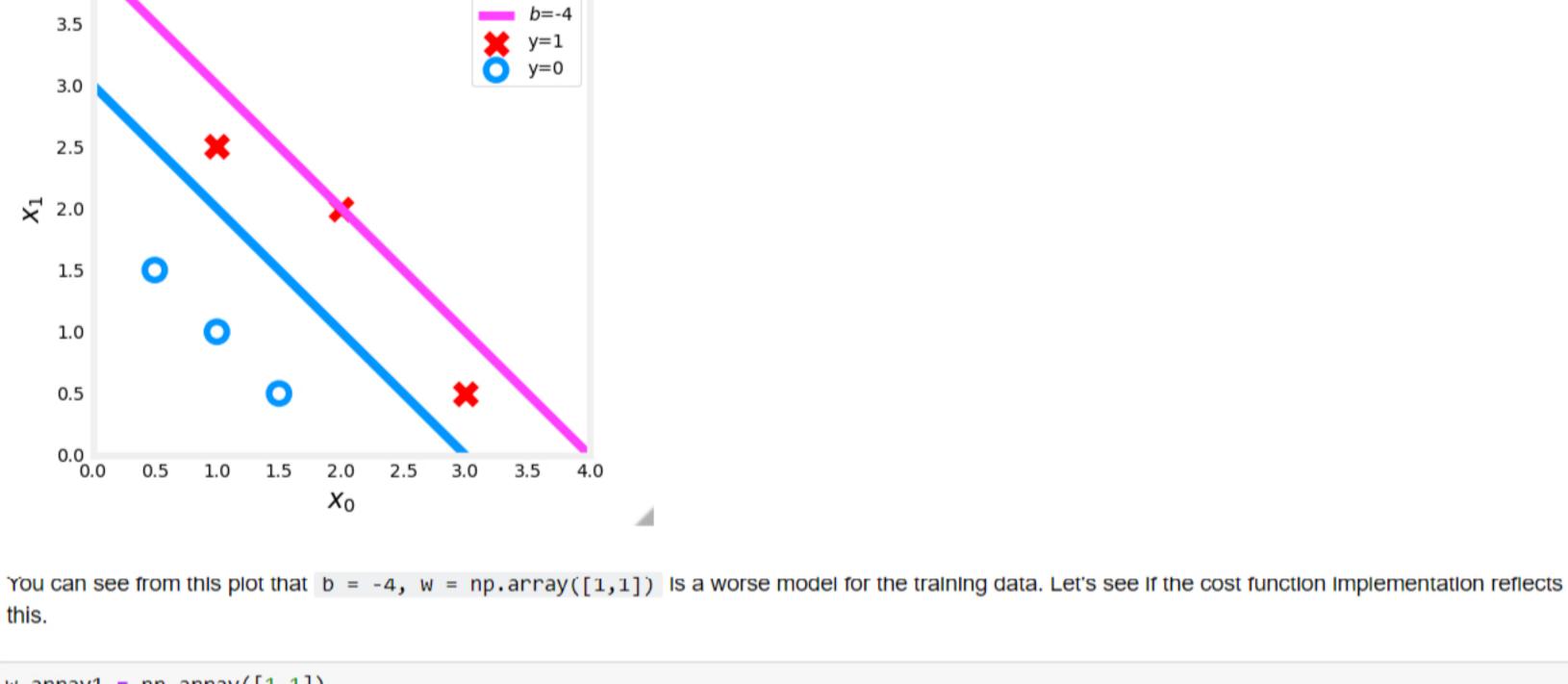
- Let's say you want to see if b = -4, $w_0 = 1$, $w_1 = 1$, or b = -4, w = np.array([1,1]) provides a better model.
- Let's first plot the decision boundary for these two different *b* values to see which one fits the data better. • For b = -3, $w_0 = 1$, $w_1 = 1$, we'll plot $-3 + x_0 + x_1 = 0$ (shown in blue)
- In [6]: import matplotlib.pyplot as plt

• For b = -4, $w_0 = 1$, $w_1 = 1$, we'll plot $-4 + x_0 + x_1 = 0$ (shown in magenta)

Choose values between 0 and 6 x0 = np.arange(0,6)# Plot the two decision boundaries x1 = 3 - x0x1 other = 4 - x0fig,ax = plt.subplots(1, 1, figsize=(4,4)) # Plot the decision boundary ax.plot(x0,x1, c=dlc["dlblue"], label="\$b\$=-3") ax.plot(x0,x1_other, c=dlc["dlmagenta"], label="\$b\$=-4") ax.axis([0, 4, 0, 4]) # Plot the original data plot_data(X_train,y_train,ax) ax.axis([0, 4, 0, 4]) ax.set_ylabel('\$x_1\$', fontsize=12) ax.set_xlabel('\$x_0\$', fontsize=12) plt.legend(loc="upper right") plt.title("Decision Boundary") plt.show()

Decision Boundary

b=-3



In [8]: w_array1 = np.array([1,1])

Expected output Cost for b = -3 : 0.3668667864055175

Cost for b = -4 : 0.5036808636748461

You can see the cost function behaves as expected and the cost for b = -4, w = np.array([1,1]) is indeed higher than the cost for b = -3, w = np.array([1,1])np.array([1,1])

Congratulations!

In this lab you examined and utilized the cost function for logistic regression.