CIS 419 – Homework 1

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Problem 1

a) At the root node for a decision tree in this domain, what are the information gains associated with the Outlook and Humidity attributes? (Use a threshold of 75 for humidity (i.e., assume a binary split: humidity ≤ 75 / humidity > 75). Be sure to show your computations.

$H(Root) = -\frac{9}{14}\log(\frac{9}{14}) - \frac{5}{14}\log(\frac{5}{14}) = .94$
$H(Humidity) = \frac{5}{14}(-\frac{4}{5}\log(\frac{4}{5}) - \frac{1}{5}\log(\frac{1}{5})) + \frac{9}{14}(-\frac{5}{9}\log(\frac{5}{9}) - \frac{4}{9}\log(\frac{4}{9}))= .895$
$H(Outlook) = \frac{5}{14}(-\frac{2}{5}\log(\frac{2}{5}) - \frac{3}{5}\log(\frac{3}{5})) + (\frac{4}{14}(0)) + \frac{5}{14}(-\frac{3}{5}\log(\frac{3}{5}) - \frac{2}{5}\log(\frac{2}{5}))= .694$

$$InformationGain(Humidity) = .94 - .895 = .045$$

$$InformationGain(Outlook) = .94 - .694 = .247$$

b) Again at the root node, what are the gain ratios associated with the Outlook and Humidity attributes (using the same threshold as in (a))? Be sure to show your computations.

$SplitInfo(Humidity) = -\frac{9}{14}\log(\frac{9}{14}) - \frac{5}{14}\log(\frac{5}{14}) = .94$
$SplitInfo(Outlook) = -\frac{5}{14}\log(\frac{5}{14}) - \frac{4}{14}\log(\frac{4}{14}) - \frac{5}{14}\log(\frac{5}{14}) = 1.58$

$$InformationRatio(Humidity) = \frac{.045}{.94} = .048$$

$$InformationRatio(Outlook) = \frac{.247}{1.58} = .156$$

c) Draw the complete (unpruned) decision tree, showing the class predictions at the leaves.