



1. for each  $i \geq 0$ ,  $xy^i$  is in  $L$

2.  $|y| > 0$

3.  $|xy| \leq p$

assume for contradiction  $L$  is regular  
& let  $p$  be the pumping length.

Given by the Pumping Lemma. Consider  
the string  $s = a^p b^p c^p d^p$  in  $L$  where

$$u = a^k b^r, v = c^p d^p \text{ \& } n(u) = n(v)$$

$$n_a(u) + n_c(u) = n_b(v) + n_d(v) = p. \quad 2p$$

According to pumping lemma  $s$   
can be written as  $xyz$  where  $|xy| \leq p$   
 $|y| > 0$  &  $xy^i$  is in  $L$  for all  $i \geq 0$

Since  $|xy| \leq p$  & consists only of 'a's

Let's say  $y = a^k$  for some  $k > 0$



Now if we pump  $y$  for  $i=0$  we get  
string

$$s = xy^0z = xz = a^{p-k} b^p c^p d^p \text{ in } L$$

$$\therefore n_a(u) + n_c(u) = (p-k) + p = 2p-k$$

$$\text{but } n_b(v) + n_d(v) = 2p$$

$$\therefore k > 0, 2p-k < 2p$$

$$\text{So } n_a(u) + n_c(u) \neq n_b(v) + n_d(v)$$

which means  $s$  is not in  $L$ .

This contradicts the Pumping Lemma.

$\therefore$  Our assumption was wrong.

So  $L$  is not regular.

Pretty well written.