	Assignment - 4
	CS 5084
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١.	Given,
	G is an arbitrary connected,
	Undirected graph with distinct cost ((e) on
	every edge e'
	e* is cheapest edge & ((e*)<((e) for
	every edge e = e*
	If we consider kruskal's aborithm, et is the 1st adge
	. Hwill be included in the minimum spanning
	tree.
	: Statement is True.
	costs
2٠	a) If we replace ce by ce & consider
	Kruskal's algorithm
	we're it will sort in the same order
	and further by putting same subjet of edges in the Minimum spanning True
	edges in the Minimum spanning True
	: the statement is True.

lets say company hasto ship 7 packages from NY to Buston let Package weights be: 2,3,1,6,4,2,5 let max. wt. limit of each truck: 8 The company wants to use fewert no of trucks possible to transport all packages from NY to Routen They use Greedy Algorithm where they pack the packages in order they drive, whenever the next package does not fit in current truck, they send truck on its way. => if package does not fit to current truck it is assigned to next truck. To answer the given question we need to prove the Greedy Algorithm company currently wing is actually minimizing the no of trucks need To prove that we need to show Greedy Algorithm is optimal than any other solution. IF Greedy algorithm tits package=1,2,...j in first x truck & another solution fits packages = 1,2, ... in first x truck To support our claim apply induction on 'x' For base case x=1, greedy algorithm tits as many packages as possible into first touck In our example it package 1,2,3 (with wt.

Now, lets assume our claim for 2=72-1
we want to show that it holds also for a.
Suppose the greedy algorithm fit i parkages into
First >c-1 trucks &
 another solution tits i Packages into x-1
 trucks where i's j'
So, here we want to show that the Greedy
Agorithm can fit at least as many packages
as the other solution in the xm truck &
it can putentially fit more,
In our example by Greedy Algorithm
boxes would go asper their order as:
Truck 1: 2,3,1 = 2+3+1=6 wt. <8
Truck 2: 6 wt. 48
Truck 3: 4, 2 = 6 wt. 68.
Truck 4: 5 Wt. 68.
it would use by trycks.
However in alternate solution,
if boxes send in the order of
= 2,6,1,3,4,2,5 then,
Truck 1: 2+6=8
Trud 2: 1+3+4=8
Truck 3: 2+5=7
10 HAI (9/6/30/00/100/100/00/00/00/00/00/00/00/00/00/
Greedy Algorith is optimal solution here.

lets start at the western end & start moving east until we reach to some house h' at umiles. miles. We cannot go further as given condition every house within 4 miles is one of base station. Now, au houses covered by base station are deleted an we have to repeat process on the remaining houses. we deleted the houses to avoid redyndent base stations, this will reduce the no-of remaining houses that need to be covered & ensure that the Final set of base station position is as small as possible while still averige all houses. We can also consider as follow: we can put first base station at the eastern most position that covers all houses from western end up to that position.

Inen we can iteratively place base station at largest position that covers all houses between the previous base station and new one.

Proof by contradiction, Suppose, Til Tz are 2 distinct minimum spanning trees of G. "T, & Tz have the same no of edges, but are not equal there some edge 'e'in Tz exist but not in Ti. If we add e to T, We form cycle. -> (1) let ez be the most expensive edge on this cycle of and in By cycle property ez does not belong to Which contradicts our assumption is a line 9. Given, G = (V, E) connected graph n- vertices m - edges T = (V, E') > spanning tree of G Defined bottleneck edge of T be the edger of T with greatest cost (1) Every minimum-bottleneck tree of G is not a minimum Spannig tree of G. let verifices of G be 4, 12, 1344 withe edge between each pair of vertices

	let weight of their edge = sum of endpoints.
	The tree consisting of path through vertices vz, vz, vz, vy has bottle neck edge of weight 5. Which is smallest possible, but its not minimum tree
	:. a'is fayse
Ь	b' is true. let T ₁ be minimum spanning tree of G & T ₂ be spanning tree with lighter
	POTTONORY POUR.
	T, has an edge e that is heavier
	than every edge in Tz -I) if we add e to Tz then it forms cycle.
	: au other edges in cycle belongs to Tz
	it becomes heaviest edge.
	:. By Cut propert of Graph
	e should not be belonging to any minimum
	spanning tree. >> contradicts eq ? (1).
21.	Given tree is connected graph with at most (n+8)
	edges. To find minimum spanning tree we have
	to follow following steps:
	- We need to apply cycle property 9 times
	by performing BFS until we find cycle in
	the graph G.
	V · · ·

Since, We know the minimum Spanning tree	•
of graph with in vertices has exactly in-1 edges,	
if we can reduce the no-of edges in the	•
	t
given near-tree G to n-1 by deleting edges without changing MST, we'll have found the	6
MST of G	C
- Starting With n+8 edges, deleting one edge at a time	C
We can reduce the no. of edges to n-1 in	
exactly '9'steps.	
5 0 0	
- Every time we need to make sure we delete	
heaviest edge on cycle.	4
- After g steps we'll have connected graph	_ d
with 'n-1' edges & the same minimum	
spanning tree as 'G'	
. It is minimum spanning tre.	
# Running time:-	
- For each iteration it is o(m+n) For BFS	(
l for corresponding Cycle.	(
# n-no. of vertice, m - edges.	•
" m is at most n+8 & we applied cycle	-
ghimes : -::)	
Running time is O(yn) working	
1.e. O(n)	