

Part 1.1:

1. $R = ABC$
Functional Dependencies = $AB \rightarrow C, AC \rightarrow B, BC \rightarrow A$
Minimal Cover - YES
BCNF = YES - where AB, BC, AC are candidate keys for R.
2. $R = ABCD$
Functional Dependencies = $AB \rightarrow C, AC \rightarrow B, BC \rightarrow A, B \rightarrow D$
Minimal Cover = YES
BCNF = NO, decomposing it to BCNF as ABC, BD
3. $R = ABCEG$
Functional Dependencies = $AB \rightarrow C, AC \rightarrow B, BC \rightarrow A, E \rightarrow G$
Minimal Cover = YES
BCNF = NO, decomposing it to BCNF as
R1(ACB) with FDs: $AC \rightarrow B$
R2(ADEBG) with FDs: $AD \rightarrow E, E \rightarrow G$
4. $R = DCEGH$
Functional Dependencies = $E \rightarrow G$
Minimal Cover = YES
BCNF = NO, decomposing it to BCNF as DCEH, EG
5. $R = ACEH$
Functional Dependencies = $AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G$
Minimal Cover - YES
BCNF = YES

Part 1.2:

1. $R = ABCDEG$

We have following functional dependencies:
 $AB \rightarrow C$
 $BC \rightarrow A$
Because of which Decomposition {AB, BC, ABDE, EG} is lossy.
Functional Dependencies $AB \rightarrow C$ OR $AC \rightarrow B$ are not preserved by the decomposition.
2. $R = ABCDEG$
The decomposition {ABC, ACDE, ADG}: lossless and not dependency preserving.

Part 2: R (A, B,C,D)

1. $B \rightarrow C, D \rightarrow A$; Decomposes into BC and AD.

Candidate Key: BD

Decomposition: Lossy, hence decomposition is poor.

If we try to join AD and BC then we get result greater than ABCD.

2. $AB \rightarrow C, C \rightarrow A, C \rightarrow D$; decomposes into ACD and BC.

Candidate Key: AB

BC decomposition is lossless – because ACD intersects BD where $C \rightarrow ACD$.

As C is the Key to ACD, the projection on ACD includes $C \rightarrow A, C \rightarrow D$ and the projection on BC does not produce any non-trivial dependency.

3. $A \rightarrow BC, C \rightarrow AD$, decomposes into ABC and AD

Candidate Key: A, C there is no need to decompose as it is already in BCNF.

4. $A \rightarrow B, B \rightarrow C, C \rightarrow D$; decomposes into AB and ACD.

Candidate Key: A

Decomposition: Lossless – because A is the key, and it does not preserve dependency on $B \rightarrow C$