

RBT23MX096

PRN No.	Total No. of Questions: 09
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QP Code:

JSPM's

Rajarshi Shahu College of Engineering, Tathawade, Pune- 411033

(An autonomous institute affiliated to Savitribai Phule Pune University)

END SEMESTER EXAMINATION (ESE), DEC./JAN. -2023

Academic Year: 2023-24(SEM-I)

Class: F.Y. B. Tech.(Civil, Mechanical, E&TC, Electrical, A&R)

Subject Name and pattern: ENGINEERING MATHEMATICS-I
[ES1201]

Duration: Hours

Max. Marks: 50 Marks

Instructions to the Candidates

1. Q.1, Q. 2 and Q.3 is compulsory.
2. Attempt Q.4 or Q.5, Q.6 or Q.7, Q.8 or Q.9.
3. Figures to the right indicates full marks.
4. Use of nonprogrammable electron pocket calculator is allowed.
5. Assume suitable and necessary data wherever required.

Q. No.		Marks	BL	CO
1	Attempt (Any One)			
a	Find the value of k so that the equations $2x - y + 3z = 2$; $x + y + 2z = 2$; $5x - y + 8z = k$ have infinite number of solutions. Hence find the solution.	4	BL3	CO1
b	Determine the values of l, m, n when $\begin{bmatrix} 0 & 2m & n \\ l & m & -n \\ l & -m & n \end{bmatrix}$ is orthogonal	4	BL3	CO1
2	Attempt (Any One)			
a	Find the Eigen values and Eigen vector corresponding to smallest eigen value of the matrix $A = \begin{bmatrix} 0 & 0 & -2 \\ 1 & 2 & 1 \\ 1 & 0 & 3 \end{bmatrix}$	4	BL3	CO1
b	Find the modal matrix P which diagonalize the matrix $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$	4	BL3	CO1
3	Attempt (Any One)			
a	Using Taylors theorem, expand $3x^3 - 2x^2 + x - 6$ in power of $(x-2)$	4	BL3	CO2
b	Evaluate: $\lim_{x \rightarrow 0} \left(\frac{1}{x} \right)^{2 \sin x}$	4	BL3	CO2

- 4 a Obtain the Fourier series expansion for $f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ x, & 0 < x < \pi \end{cases}$ in $(-\pi, \pi)$ where $f(x+2\pi) = f(x)$ 4 BL3 CO3

- b Find the Fourier series to represent the function $f(x) = |x|$ in $-\pi < x < \pi$ and $f(x+2\pi) = f(x)$ 4 BL3 CO3

- c The turning moment T units of the crank shaft of a steam engine is given for a series of values of the crank angle θ in degrees. 4 BL3 CO3

θ	0	30	60	90	120	150
T	0	5224	8097	7850	5499	2626

Find the coefficients of first two terms b_1 and b_2 in a series of sines to represent T. (Take $L = \pi$)

OR

- 5 A Express y as a Fourier series upto first harmonic where y is given as 4 BL3 CO3

x	0	$\frac{\pi}{3}$	$\frac{2\pi}{3}$	π	$\frac{4\pi}{3}$	$\frac{5\pi}{3}$
y	1.0	1.4	1.9	1.7	1.5	1.2

- b Find the constant term a_0 and coefficient of first two terms a_1 and a_2 of series of cosines to represent y where y is given in the following table 4 BL3 CO3

x	0	1	2	3	4	5
y	9	18	24	28	26	20

(Take $L = 6$)

- c Obtain the half range sine series expansion of $f(x) = e^x$ in $0 < x < 1$ 4 BL3 CO3

- 6 a Verify $\frac{\partial^2 u}{\partial x \partial y} = \frac{\partial^2 u}{\partial y \partial x}$ for $u = \log(x^2 + y^2)$ 4 BL3 CO4

- b If $u = \sin^{-1}(x^3 + y^3)^{\frac{2}{5}}$, then find the value of $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$ 5 BL3 CO4

- c If $u = x^2 - y^2$; $v = 2xy$ and $z = f(u, v)$, 4 BL3 CO4

then show that $\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 = 4(u^2 + v^2)^{\frac{1}{2}} \left[\left(\frac{\partial z}{\partial u}\right)^2 + \left(\frac{\partial z}{\partial v}\right)^2 \right]$

OR

- 7 a If $x = r \cos \theta$; $y = r \sin \theta$; show that $\left(\frac{\partial y}{\partial r}\right)_x \cdot \left(\frac{\partial y}{\partial r}\right)_\theta = 1$ 4 BL3 CO4
- b If $u = \tan^{-1}\left(\frac{x^3 + y^3}{x - y}\right)$, then prove that 5 BL3 CO4
- $$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = \sin 2u (2 \cos 2u - 1)$$
- c If $z = f(x, y)$ where, $x = e^u + e^{-v}$; $y = e^{-u} - e^v$, then prove that 4 BL3 CO4
- $$\frac{\partial z}{\partial u} - \frac{\partial z}{\partial v} = x \frac{\partial z}{\partial x} - y \frac{\partial z}{\partial y}$$
- 8 a If $x + y + z = u$, $y + z = uv$, $z = uvw$ then find $\frac{\partial(x, y, z)}{\partial(u, v, w)}$ 4 BL3 CO5
- b Examine whether the functions 5 BL3 CO5
- $$u = \sin^{-1} x + \sin^{-1} y, v = x\sqrt{1-y^2} + y\sqrt{1-x^2}$$
- are functionally dependent. If dependent then find the relation between them.
- c Find the minimum value of $xy + a^3\left(\frac{1}{x} + \frac{1}{y}\right)$. 4 BL3 CO5
- OR**
- 9 a If $x = uv$, $y = \frac{u+v}{u-v}$ then find $\frac{\partial(u, v)}{\partial(x, y)}$ 4 BL3 CO5
- b Examine whether the functions $u = \frac{x-y}{x+y}$, $v = \frac{x+y}{x}$ are functionally 5 BL3 CO5
- dependent. If dependent then find the relation between them.
- c The volume V of right circular cone is given by $V = \frac{1}{3}\pi r^2 h$ where r is 4 BL3 CO5
- radius of base and h is height. In calculating the volume, an errors of 2% and 1% are made in measuring the height and radius of base respectively. Find the percentage error in calculating volume.
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