PRN No.

Total No. of Questions: 09 QP Code:

JSPM's

RajarshiShahu College of Engineering, Tathawade, Pune- 411033

(An autonomous institute affiliated to SavitribaiPhule Pune University

End Semester Examinations (ESE) May/June23-24

Class: F. Y. B. Tech. (IT)

Semester: I Ac

Academic Year: 2023-24

Department: Engineering Sciences and Humanities

Course Code: ES1204

Course Name and pattern: Discrete Mathematics (2023)

Duration: 2 Hours 30 Mins.

Max. Marks: 50 Marks

Instructions to the Candidates

1. Q.1, Q.2 and Q.3 are compulsory.

- 2. Solve Q.4 or Q.5, Q.6 or Q.7, Q.8 or Q.9.
- 3. Assume suitable data if necessary.
- 4. Use of non-programmable electronics pocket calculator is allowed.

Q.1 Solve any one

- a Obtain the principal conjunctive normal form (PCNF) and principal 4 BL3 CO1 disjunctive normal form (PDNF) of the statement $p \to (p \to q) \land \sim (p \land q)$ by using the Truth table method.
- b Translate each of the statement into symbols, using quantifiers, 4 BL3 CO1 variables and predicate symbols:
 - Every electrical engineering student must take an electronics course.
 - There are some electrical engineering students who have not taken electronics courses.

Q.2 Solve any one

- a In a town of 10000 families it was found that 40% of families buy newspaper A, 20% family buy newspaper B, 10% family buy newspaper C, 5% family buy newspaper A and B, 3% family buy newspaper B and C and 4% family buy newspaper A and C. If 2% family buy all the newspaper. Find
 - 1. Number of families which buy none of A, B, C
 - 2. Number of families which buy newspaper A and B only

BL3 CO2

- **b** Let $A = \{1,2,3,4,5\}$ and R be relation defined on A whose M_R is
- 4 BL3 CO2

$$M_R = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix}.$$

Draw Hasse diagram of relation R on A.

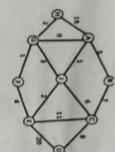
- Q.3 Solve any one
 - a Let $Z_n = \{0, 1, 2, ..., n-1\}$. Let \bigoplus_n be a binary operation such that $a \bigoplus_5 b$ = remainder of a + b divided by n. Construct a table for n = 5. Is $(Z_4, 5)$ an abelian group?
 - b Given the generator matrix $G = \begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 1 \end{bmatrix}$ corresponding to the encoding function $e: B^3 \to B^6$, find the corresponding parity check matrix. Use it to decode the following received words i) 000101 ii) 110001 and hence, find the original message.
- Q.4 a i) From a word containing 5 vowels and 12 consonants, how many 8 4 BL3 CO4 letter words can be formed by using 3 vowels and 5 consonants?
 - ii) In how many ways can the letters in the word 'MISSISSIPPI' be arranged so that 'S' are always together?
 - b Use mathematical induction to prove that $n^3 + 2n$ is divisible by 3 for 4 BL3 CO4 all integers $n \ge 1$.
 - c Solve the recurrence relation $a_n 12a_{n-1} + 36a_{n-2} = 39$, where 4 BL3 CO4 $a_0 = 0$ and $a_1 = 2$.
 - OR
- Q.5 a In how many ways can 20 students out of a class of 32 be chosen to 4 BL3 CO4 attend class on a Thursday afternoon if
 - Paul refuses to go to class?
 - ii) Michelle insists on going?
 - iii) Jim and Michelle insist on going?
 - b Find the generating functions of the sequence $a_n = 2(-3)^n + 3(5)^n$, 4 BL3 CO4 where n = 0,1,2,3,...
 - e Solve the recurrence relation $a_n 7a_{n-1} + 12a_{n-2} = 36$, where 4 BL3 CO4 $a_0 = 1$ and $a_1 = 3$.

- 0.6 22 Suppose that a connected planar graph has eight vertices, each of degree three. Using Euler's formula, find how many regions are in that planar graph? Draw such a graph.

BL3

CO5

- -Determine whether the graphs k_5 and $k_{2,3}$ are isomorphic or not. Justify your answer. 4 BL3 CO5
- 0 Use Dijkstra's algorithm, to find the shortest path and its between vertex H and vertex D in the following weighted graph. length th. CO5



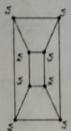
Q.7 a Determine whether the following graph is i) Complete

BL3

C05

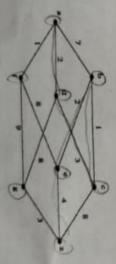
ii) Bipartite, If yes, draw the graphiii) Complete Bipartite. Justify your answer

5 Determine whether Eulerian path, Eulerian circuit, Hamiltonian path, Hamiltonian circuit, if it exists in the following graph. If it does not exist, explain why? 4 BL3 CO5

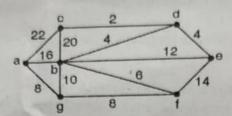


Use Dijkstra's algorithm, to find the shortest path and its length between vertex a and vertex z in the following weighted graph. Un BL3 C05

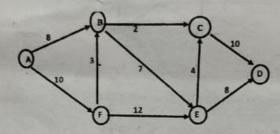
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Q.8 a Find the minimal spanning tree and its minimum weight using 4 BL3 CO6 Kruskal's algorithm.



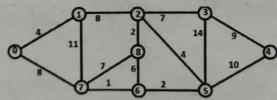
b Find maximum flow in the transport network using labeling procedure. 4 BL3 CO6
Determine the corresponding minimum cut set.



- c A file contains the string "DATAMINNING". If Huffman Coding is 5 BL3 CO6 used for data compression, determine the following:
 - i) Huffman Code for each character.
 - ii) Average code length.
 - iii) Length of Huffman encoded message (in bits).

OR

Q.9 a Find the minimal spanning tree and its minimum weight using Prim's 4 BL3 CO6 algorithm.



- b 19 lamps are to be connected to a single electrical outlet, using extension cords, each of which has 4 outlets. Find the number of extension cords needed and draw the corresponding tree.
- e A file contains the string "ENGINEERING". If Huffman Coding is 5 BL3 CO6 used for data compression, determine the following:

CO6

- i) Huffman Code for each character.
- ii) Average code length.
- iii) Length of Huffman encoded message (in bits).