

1. a)  $u \cdot v = (-2 \times 1) + (3 \times 0) = -2$  ✓

b)  $u \cdot v = \left(\frac{1}{10} \times \frac{70}{3}\right) + \left[(-1) \times \left(-\frac{1}{3}\right)\right] + \left(\frac{2}{3} \times \frac{1}{2}\right) = 1$  ✓

c)  $u \cdot v = 1 \times 1 + 0 \times 1 + 1 \times 0 + 1 \times 0 + 1 \times 0 = 1.$  ✓

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2. a). Namely  $u \cdot v = 0.$

For  $v (x, y).$

$$u \cdot v = (1 \times \cancel{x}) + (1 \times \cancel{y}) = \cancel{x+y} = 0.$$

∴ Example  $v = (2, -2).$  ✓

b).  ~~$a+b+c+d$~~   $= a+3b+2c$

$$u \cdot v = a \times 1 + 3 \times y + 2 \times z = a \cdot x + 3y + 2z = 0.$$

Example  $v = (-2, 1, -1)$  ✓

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c).  $u \cdot v = a + (-1) \times b + (-1) \times c + 2d = 0.$

$$a - b - c + 2d = 0.$$

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Example  $v = (0, 1, 1, 1).$  ✓

3.  $A^T = \begin{bmatrix} 3 & -1 & 0 \\ 2 & -1 & 1 \end{bmatrix}, \quad v = \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix}$

$$A^T v = [3 \times 1 + 2 \times 1; (-1) \times 1 + (-1) \times 1; 0 \times (-1) + 1 \times (-1)] \\ = (5, -2, -1).$$

4.  $AB = \begin{bmatrix} 4 & 4 & 5 \\ 6 & 7 & 6 \\ 6 & 4 & 2 \end{bmatrix} - \quad BA = \begin{bmatrix} 4 & 3 & 6 \\ 4 & 7 & 6 \\ 4 & 4 & 2 \end{bmatrix} \quad \wedge$

Answer is No.