

$$C(s) = K_p + \frac{K_i}{s} + \frac{K_d N s}{s + N}$$

Bilinear transform

$$s \rightarrow \frac{z(z-1)}{T(z+1)}$$

$$C(z) = K_p + \frac{K_i T(z+1)}{2(z-1)} + \frac{2K_d N(z-1)}{T(z+1) + N}$$

$$C(z) = K_p + \frac{0.5 K_i T(z+1)}{(z-1)} + \frac{2K_d N(z-1)}{2(z-1) + NT(z+1)}$$

$$U(z) = C(z)R(z) = \underbrace{K_p R(z)}_{U_p(z)} + \underbrace{\frac{0.5 K_i T(z+1)}{(z-1)} R(z)}_{U_i(z)} + \underbrace{\frac{2K_d N(z-1)}{2(z-1) + NT(z+1)} R(z)}_{U_d(z)}$$

$$U(z) = U_p(z) + U_i(z) + U_d(z)$$

$$U_p(z) = K_p R(z)$$

$$\rightarrow \boxed{U_p[k] = K_p r[k]} \quad *$$

$$U_i(z) = \frac{0.5 K_i T(1+z^{-1})}{1-z^{-1}} R(z)$$

$$\frac{2z^{-2} + NTz + NT}{(z+NT)z^{-2} + NT}$$

$$U_i(z) = z^{-1} U_i(z) = 0.5 K_i T(R(z) + z^{-1} R(z))$$

$$U_i[k] - U_i[k-1] = 0.5 K_i T(r[k] + r[k-1])$$

$$\boxed{U_i[k] = U_i[k-1] + 0.5 K_i T(r[k] + r[k-1])} \quad *$$

$$U_d(z) = \frac{2K_d N(R(z) - z^{-1} R(z))}{(z+NT) + (NT-z)z^{-1}}$$

$$(z+NT)U_d(z) + (NT-z)z^{-1}U_d(z) = 2K_d N(R(z) - z^{-1} R(z))$$

$$\boxed{U_d[k] = -\frac{(NT-z)}{z+NT} U_d[k-1] + \frac{2K_d N}{z+NT} (r[k] - r[k-1])} \quad *$$