9.2 - Algoritma pada Graf (part 2)

[KOMS120403]

Desain dan Analisis Algoritma (2022/2023)

Dewi Sintiari

Prodi S1 Ilmu Komputer Universitas Pendidikan Ganesha

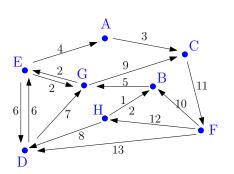
Week 12 (April 2023)

Daftar isi

- Shortest path problem (masalah jarak terpendek)
 - ► Algoritma Dijkstra

Bagian 1. Shortest Path

Masalah: diberikan graf berarah berbobot sisi. Temukan jalur terpendek dari s ke t.



8

Pohon jalur terpendek (shortest-path tree) yang berakar pada simpul v adalah pohon rentang (spanning tree) T dari graf G, sedemikian sehingga jarak jalur dari akar v ke simpul lain mana pun u di T adalah jalur terpendek jarak dari v ke u di G.

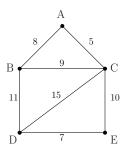


Figure: Graf G

Pohon jalur terpendek (shortest-path tree) yang berakar pada simpul v adalah pohon rentang (spanning tree) T dari graf G, sedemikian sehingga jarak jalur dari akar v ke simpul lain mana pun u di T adalah jalur terpendek jarak dari v ke u di G.

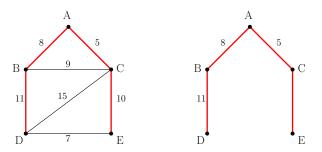


Figure: Yang berwarna merah adalah pohon jalur terpendek dari G berakar pada A

Pohon jalur terpendek (shortest-path tree) yang berakar pada simpul v adalah pohon rentang (spanning tree) T dari graf G, sedemikian sehingga jarak jalur dari akar v ke simpul lain mana pun u di T adalah jalur terpendek jarak dari v ke u di G.

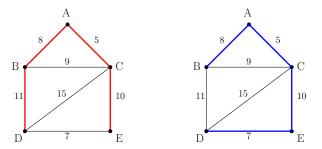


Figure: Yang berwarna merah merupakan pohon jalur terpendek, dan yang biru merupakan MST dari G

Varian dari shortest path

Berdasarkan titik

- Sumber tunggal (single source): dari satu simpul s ke setiap simpul lainnya
- Source-sink: dari simpul sumbery s ke suatu simpul akhir t
- Semua pasangan: antara semua pasangan simpul

Batasan pada bobot sisi?

- Bobot yang tak-negatif
- Bobot yang merupakan jarak Euclid
- Bobot sebarang

Sirkuit?

- Tanpa sirkuit berarah
- Tanpa "sirkuit negatif"



Penerapan dari shortest path

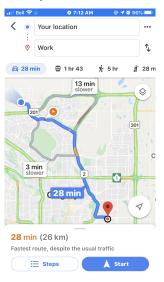


Figure: Mencari rute terpendek pada Google maps

Penerapan dari shortest path



Figure: Sistem navigasi pada mobil

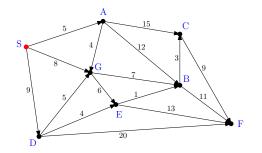
Bagian 2. Algoritma Dijkstra



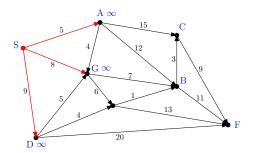
Figure: Edsger W. Dijkstra

Single-source shortest path:

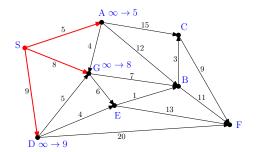
Tujuan: Temukan jalur terpendek dari sumber s ke setiap simpul lainnya.



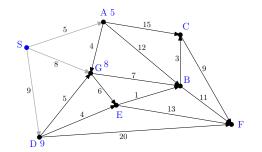
v	distTo[]	$\mathrm{edgeTo}[\]$
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



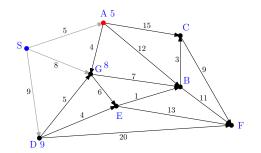
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B}\to\mathrm{F}$
G	8.0	$S \to G$



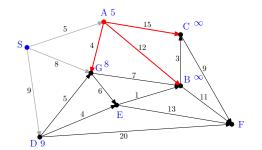
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



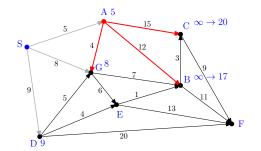
v	distTo[]	$\rm edgeTo[~]$
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



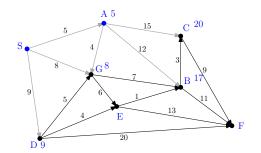
v	distTo[]	$\rm edgeTo[\]$
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



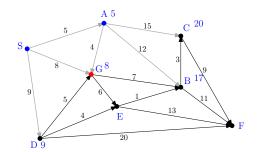
v	distTo[]	$\rm edgeTo[\]$
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



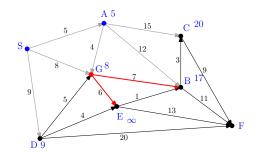
v	distTo[]	$\rm edgeTo[\]$
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



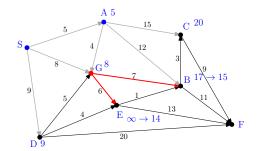
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B}\to\mathrm{F}$
G	8.0	$S \to G$



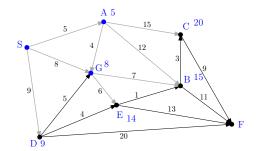
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



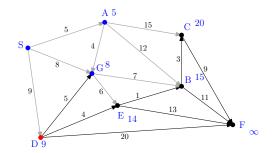
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



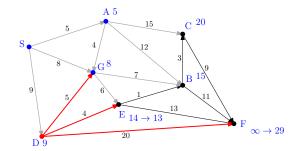
v	distTo[]	$\rm edgeTo[~]$
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



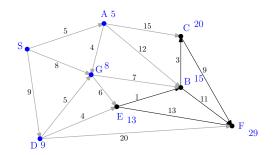
v	distTo[]	${\rm edgeTo}[\]$
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B}\to\mathrm{F}$
G	8.0	$S \to G$



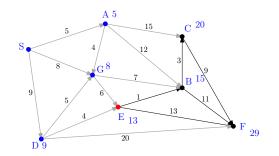
v	distTo[]	edgeTo[]
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



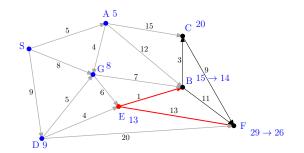
v	distTo[]	edgeTo[]
	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



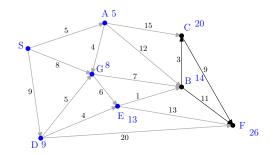
v	distTo[]	$\mathrm{edgeTo}[\]$
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



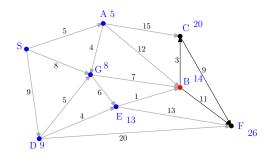
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



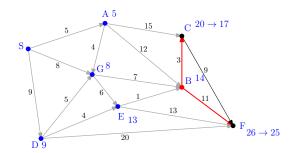
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} o \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



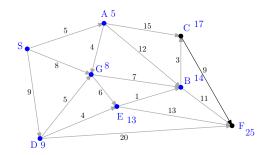
v	distTo[]	$\mathrm{edgeTo}[\]$
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



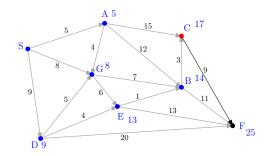
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} o \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



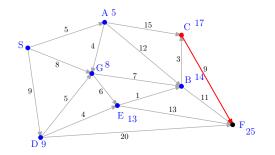
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



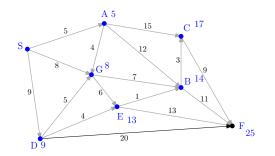
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



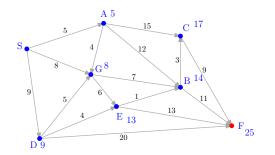
v	distTo[]	edgeTo[]
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



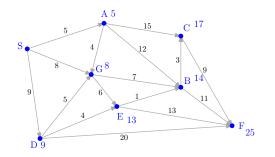
v	distTo[]	edgeTo[]
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



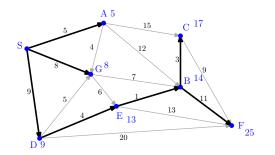
v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
С	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



v	distTo[]	edgeTo[]
S	0	-
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
E	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$



v	distTo[]	edgeTo[]
S	0	_
A	5.0	$S \to A$
В	14.0	$\mathrm{E} \to \mathrm{B}$
\mathbf{C}	17.0	$\mathrm{B} \to \mathrm{C}$
D	9.0	$S \to D$
\mathbf{E}	13.0	$\mathrm{D} \to \mathrm{E}$
F	25.0	$\mathrm{B} \to \mathrm{F}$
G	8.0	$S \to G$

end of slide...