

Dwayne Williams
ECE 4720 HW 1

2.3)

$$\begin{aligned} a) R_{mm} &= \lambda_{22} + (\lambda_{12} - \lambda_{22}) \int_{R1} p(\mathbf{x} | \omega_2) d\mathbf{x} = \lambda_{11} + (\lambda_{21} - \lambda_{11}) \int_{R2} p(\mathbf{x} | \omega_1) d\mathbf{x} \\ &= 0 + (1 - 0) \int_{R1} p(\mathbf{x} | \omega_2) d\mathbf{x} + 0 + (1 - 0) \int_{R2} p(\mathbf{x} | \omega_1) d\mathbf{x} \\ &= \int_{R1} p(\mathbf{x} | \omega_2) d\mathbf{x} + \int_{R2} p(\mathbf{x} | \omega_1) d\mathbf{x} \end{aligned}$$

b)

2.5)

$$p(\mathbf{x} | \omega_i) = T(\mu_i, \delta_i) = \{[(\delta_i - |x - \mu_i|) / \delta_i^2, \text{ for } |x - \mu_i| < \delta_i], [0, \text{ otherwise}]\}$$

2.7)

$$p(x | \omega_i) = (1/\pi b) * 1/(1 + ((x - a_i)/b)^2), \quad i=1,2$$

$$E = P(\text{error})$$

a)

ω_2 but actually ω_1

$$E_1 = E(x | \omega_1) = \int p(x | \omega_1) P(\omega_1)$$

$$P(\omega_1) = 1/2 \text{ (assumption)}$$

$$= 1/2 \int_{-\infty}^{\infty} (1/\pi b) * 1/(1 + ((x - a_1)/b)^2) dx$$

b)

ω_1 but actually ω_2

$$E_2 = \int p(x | \omega_2) P(\omega_2)$$

$$P(\omega_2) = 1/2 \text{ (assumption)}$$

$$= 1/2 \int_{-\infty}^{\infty} (1/\pi b) * 1/(1 + ((x - a_2)/b)^2) dx$$

c)

$$E_1 + E_2 = E$$

d)

$$E = .1 + 1/2 \pi \int_{-\infty}^{\infty} 1/(1 + (x-1)^2) dx$$

$$= .1 + 1/2 \pi \int_{-\infty}^{\infty} ((1 + (x-1)^2)^{-1}) dx$$

e)