

$$\begin{aligned}
 a) \quad l_{i1}: LR &= -2(-149.521 - (-134.178)) = 30.69 \\
 l_{i2}: LR &= -2(-139.747 - (-134.178)) = 11.14 \\
 l_{i1}, l_{i2}: LR &= -2(-152.763 - (-134.178)) = 37.17
 \end{aligned}
 \left. \begin{array}{l} \chi^2(1) \quad \alpha = 5\% \\ C_d = 3.8 \\ \chi^2(2) \\ C_d = 6.0 \end{array} \right\}$$

$\Rightarrow l_{i1}, l_{i2}$ individually significant
and jointly significant

b) McFadden R^2 can be used: - explained variable the same
- number of coefficients the same

$$McFadden R^2 = 1 - \frac{\log(L(b_1))}{\log(L(b_0))} \quad \log(L(b_1)) = -152.763$$

$$\text{first value } R^2 = 1 - (-134.178) / (-152.763) = 1 - 0.8783 = 0.1217$$

	$l_{i1}(-1)$	$l_{i2}(-1)$	$l_{i1}(-2)$	$l_{i2}(-2)$
$l_{i1}(-1)$	0.1217	0.1217		
$l_{i1}(-2)$	0.1461	0.1460		

best performing model

$$c) \quad \hat{p}_{\text{growth}} = \frac{e^{0.746 - 0.429 \times l_{i1}(-2) - 0.131 \times l_{i2}(-1)}}{1 + e^{0.746 - 0.429 \times l_{i1}(-2) - 0.131 \times l_{i2}(-1)}}$$

Quarter	GDPIMPR	PredProb	Pred01
2011Q1	1	0.242872	0
2011Q2	0	0.219600	0
2011Q3	0	0.084092	0
2011Q4	0	0.084092	0
2012Q1	1	0.159628	0
2012Q2	0	0.225832	0
2012Q3	1	0.376366	0
2012Q4	1	0.555273	1
2013Q1	1	0.596042	1
2013Q2	1	0.522734	1
2013Q3	1	0.555273	1
2013Q4	0	0.713614	1
2014Q1	0	0.739621	1
2014Q2	1	0.649081	1
2014Q3	1	0.764048	1
2014Q4	1	0.850051	1
2015Q1	1	0.850051	1
2015Q2	1	0.832577	1
2015Q3	1	0.713614	1
2015Q4	0	0.346151	0



	Predicted		Total
	0	1	
Realization:0	5	2	7
Realization:1	3	10	13
Total:	8	12	20



relative

	Predicted		Total
	0	1	
Realization:0	5/20	2/20	7/20
Realization:1	3/20	10/20	13/20
Total:	8/20	12/20	20/20

the hitrate = $5/20 + 10/20 = 0.75 \Rightarrow 75\%$ of the cases the model gives the correct prediction

d)

Dependent variable: $\text{GrowthRate} = \Delta \log \text{GDP}$

Sample size: 240

	Coefficient	Standard error	t-value
Constant	0.090	0.037	2.400
<u>LOGGDP(-1)</u>	-0.019	0.008	<u>-2.371</u>
GrowthRate(-1)	0.613	0.050	12.236
T	6.23×10^{-5}	2.59×10^{-5}	2.407

Critical value of Augmented Dickey Fuller test with constant and trend
 $C_1 = -3.7$

$\Rightarrow H_0$ of unit root not rejected $\Rightarrow \log \text{GDP}$ non-stationary

e)

<u>$Li(-1)$</u>	<u>$Li(-2)$</u>	best performing model
$Li(-1)$ 0.5086	0.5077	
$Li(-2)$ 0.4772	0.4771	



Dependent variable: GrowthRate

Sample size: 240

	Coefficient	Standard error	t-value
C	0.001737	0.000320	5.433
GrowthRate(-1)	0.461579	0.048302	9.556
LI1(-1)	-0.001023	0.000130	-7.880
LI2(-1)	-0.000149	6.421×10^{-5}	-2.326

f)

Dependent variable: RESID (Residuals from model in (e) with $k_1 = k_2 = 1$)

Sample size: 239

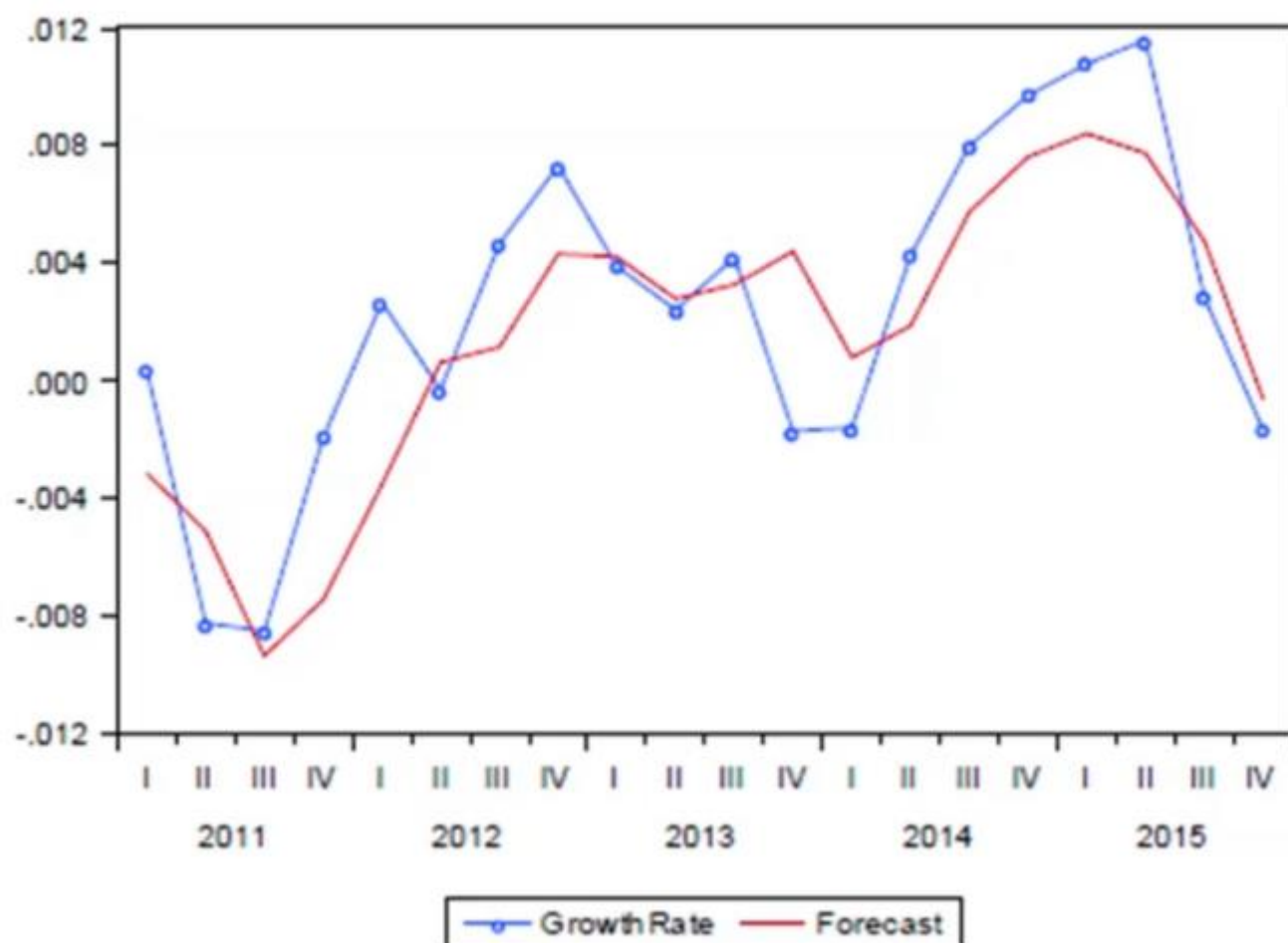
	Coefficient
C	-0.0001
GROWTHRATE(-1)	0.0291
LI1(-1)	3.14×10^{-5}
LI2(-1)	2.77×10^{-6}
RESID(-1)	-0.0500
R^2	0.0010

Breusch - Godfrey test statistic $240 \times 0.0010 = 0.24$ $\chi^2(1)$ $C_{\alpha} = 3.8$
 $\alpha = 5\%$

$\Rightarrow H_0$ not rejected

↳ of no residual serial correlation

g) $RMSE = 0.008156$ 0.3% on quarterly basis



=> graph shows predictions are reasonably accurate