

# Prediction of multidimensional drug dose responses based on measurements of drug pairs

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**Finding potent multidrug combinations against cancer and infections is a pressing therapeutic challenge; however, screening all combinations is difficult because the number of experiments grows exponentially with the number of drugs and doses. To address this, we present a mathematical model that predicts the effects of three or more antibiotics or anticancer drugs at all doses based only on measurements of drug pairs at a few doses, without need for mechanistic information. The model provides accurate predictions on available data for antibiotic combinations, and on experiments presented here on the response matrix of three cancer drugs at eight doses per drug. This approach offers a way to search for effective multidrug combinations using a small number of experiments.**

drug combinations | drug cocktails | cancer treatment | mechanism-free formula | predictive formula

To kill cancer cells or bacteria, combination therapy can be more effective than individual drugs (1–6). Combination therapy is thought to allow increased efficacy at low doses, thus reducing side effects and toxicity; it is also believed to minimize the chances of resistance (7–9), a pressing problem in treating cancer and infectious diseases.

Much work has been devoted to classifying how pairs of drugs interact (10–14). Across systems, a good first approximation is the Bliss independence model (15, 16), in which the pair effect is the product of the individual drug effects: If the effect of the drugs are  $g_1$  and  $g_2$ , the effect of the combination is  $g_{12} = g_1 \cdot g_2$ . The Bliss model ignores interactions in which drugs enhance each other effects—synergism—or inhibit each other's effects—antagonism. Some drugs even inhibit each other so much that the combined effect is lower than either drug alone, an effect called hyperantagonism (17–21).

Going beyond drug pairs has been difficult. Experimentally testing high-order combinations beyond pairs in a systematic way is challenging because it requires an exponentially large number of experiments (22–25): For  $N$  drugs at  $D$  doses, one needs  $D^N$  experiments. For  $N = 10$  drugs and  $D = 8$  doses, this means  $\sim 10^9$  measurements. The combinatorial explosion makes exhaustive testing of drug dose combinations unfeasible. This problem is especially acute in cases where material is scarce, such as testing of patient-derived samples (26–29). Hence, models for predicting high-order effects are essential.

Apart from detailed simulations of particular systems (22, 30, 31), there has been little study of general mechanism-independent models for multiple drugs. An exception is the elegant study by Wood et al. (32) that showed that combinations of antibiotics can be predicted by an Iseliss-like formula that uses pair effects to predict the effects of higher-order mixtures. For example, the effect of a drug triplet is modeled as  $g_{123} = g_{12}g_3 + g_{13}g_2 + g_{23}g_1 - 2g_{12}g_3$ . This formula has not been tested on cancer drug mixtures, to the best of our knowledge.

Another line of research uses machine learning algorithms to make predictions based on a small number of measurements (23, 33–37). Such approaches use regression to extrapolate from data, and often require iteration cycles of prediction and experiment to home in on solutions. Such machine learning approaches can benefit from a predictive formula that can make the search less prone to experimental error and can help avoid local maxima.

Here we study how multiple cancer drugs interact to affect cells by measuring the response matrix of three cancer drugs at eight doses per drug. We find that existing approaches do not accurately predict the response matrix. We therefore introduce a relatively simple model for drug mixtures. This model predicts high-order combination effects at all doses, based on measurements on single drugs and drug pairs at a small number of doses. The model provides accurate predictions for the three anticancer drug dose–response matrix measured in this study, and available data on antibiotic effects on bacterial growth rate (32), even in cases where synergy and antagonism is strong. This model is especially noise-resistant because it interpolates between dose measurements. The present model may be used to make accurate predictions of multiple drugs, based on only a few measurements of single and pair effects, thus bypassing the need for an exponentially large number of measurements.

## Results

**Current Approaches Do Not Describe the Response Matrix of Three Cancer Drugs.** We experimentally measured the dose–response matrix for eight doses of three commonly used chemotherapy drugs—doxorubicin, taxol, and cisplatin—on survival of A549 human lung cancer cells. Survival was measured using a cell viability assay (*Methods*).

The single-drug dose curves are given by the response matrix when the dose of the two other drugs is zero. The dose–response curves were well fit by Hill curves (10, 38, 39), characterized by a steepness parameter (Hill coefficient)  $n$  and a half-way point  $D_{0.5}$  equal to the drug concentration of 50% effect

$$g_i = \frac{1}{1 + (D_i/D_{0.5})^n} \quad [1]$$

When combined, the drugs show a relatively complex interplay, which can be visualized by 2D slices through the response matrix (Fig. 1). Some slices show nonmonotonic behavior where survival is highest at intermediate doses.

To evaluate synergy and antagonism, we computed the Bliss approximation, given by the product of the single-drug response

## Significance

**We present a mechanism-free formula that predicts effects of multiple drugs at all doses based on measurements of drug pairs at a few doses. The formula bypasses the combinatorial explosion problem by greatly reducing the number of measurements needed to design optimal cocktails for cancer and infection.**

Author contributions: U.A. designed research; A.Z., I.K., E.D., and A.E.M. performed research; A.Z. performed experiments; I.K. contributed new reagents/analytic tools; I.K. designed the model and analyzed data; and A.Z., I.K., and U.A. wrote the paper.

The authors declare no conflict of interest.

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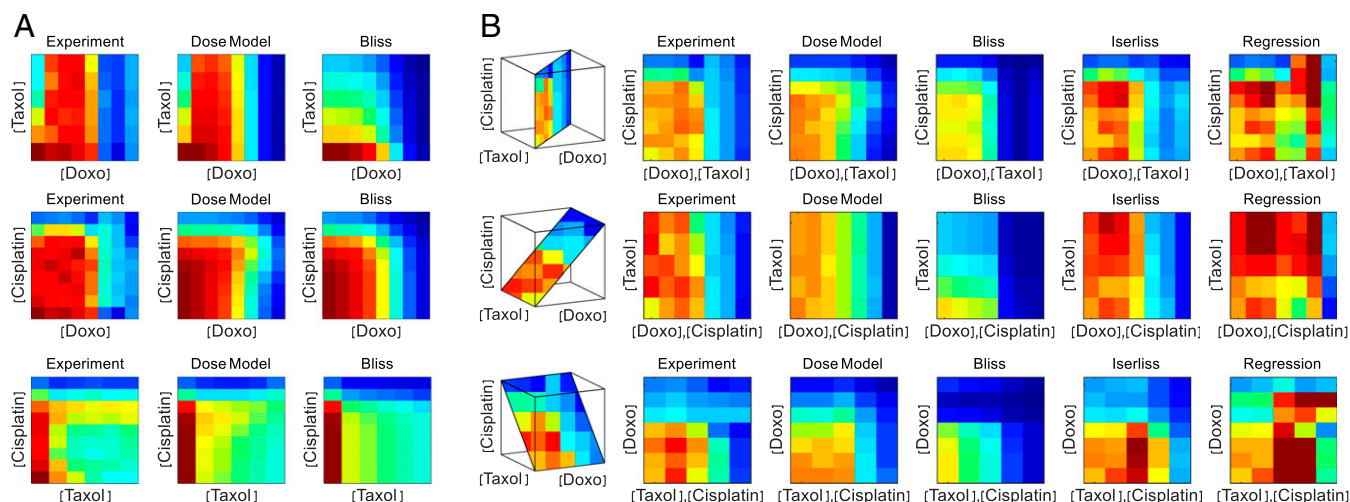
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See Commentary on page 10231.

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**Fig. 1.** Response matrix of three chemotherapy drugs at eight doses shows nonmonotonic behavior that is well captured by the dose model but not by other models. (A) Survival of A549 lung cancer cells when treated with the three pairs of drugs (taxol–doxorubicin, cisplatin–doxorubicin, cisplatin–taxol) at eight doses each: (Left) the measured response, (Middle) the predicted response using the present dose model, and (Right) the predicted response by Bliss independence. (B) Slices of the three-drug dose–response matrix. The first column is the measured response, followed by the prediction of the three drugs' interactions using different models. Note that the Isserlis and regression models apply only to triplets and above, not to pairs.

curves  $g_{123}(D_1, D_2, D_3) = g_1(D_1)g_2(D_2)g_3(D_3)$ . The Bliss approximation differs significantly from the measured response matrix (Figs. 1 and 2A). The drug combinations show reduced effect compared with Bliss, which means that they show antagonism (Fig. 2A). Antagonism is partly due to cell cycle effects where taxol tends to prevent entry of cells into the S phase in which the other two drugs are most effective (40–42).

We next compared the data to the Isserlis formula  $g_{123} = g_{12}g_3 + g_{13}g_2 + g_{23}g_1 - 2g_1g_2g_3$ . We find that the Isserlis model does better than Bliss but still explains only 60% of the variance,  $R^2 = 0.6$  (Fig. 2B). One reason for this relative lack of fit is experimental noise: The Isserlis model depends sensitively on errors in the three input pairs  $g_{12}$ ,  $g_{13}$ , and  $g_{23}$  and the three single-effect data points  $g_1$ ,  $g_2$ , and  $g_3$ .

We also performed regression similar to that used in machine learning approaches (36, 37, 43), which results in the formula  $g_{123} = g_{12}g_{13}g_{23}/g_1g_2g_3$  (Methods). This regression formula shows poor performance (Fig. 2C). We conclude that an improved formula is needed to describe the present three-drug response matrix.

**A Simple Dose Model for Drug Combinations.** We present a simple model for drug combinations. This is a model for three or more drugs, based on measurements of the response of single drugs and drugs pairs at a few dose combinations.

The model extends the Bliss formula; it is based on the product of the effects of all drugs in the mixture, not at their true doses but rather at effective doses that differ from the true doses due to interactions with the other drugs in the mixture. This interaction is modeled by introducing interaction terms between drug pairs (14). In the model, the effective dose of each drug,  $D_{ieff}$ , is its true dose  $D_i$  times a product of the Michaelis–Menten-like terms for all of the other drugs

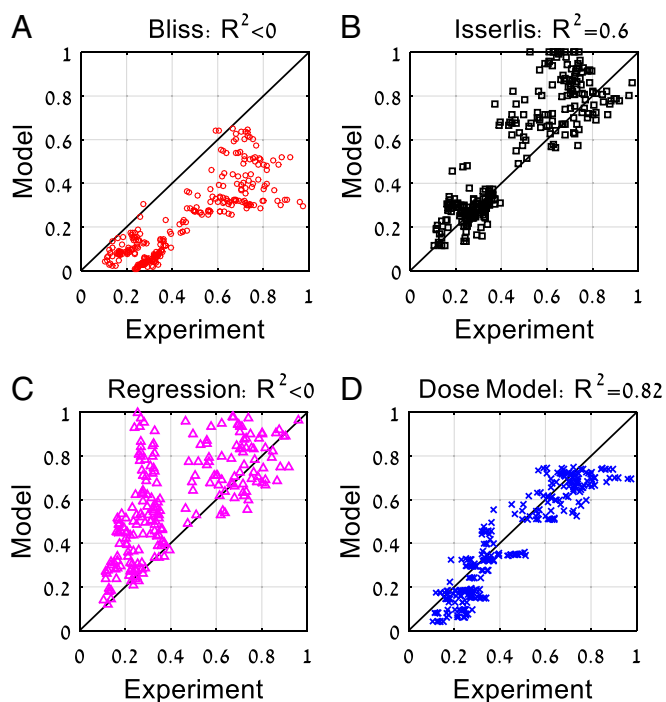
$$g_{1...n} = g_1(D_{1eff}) \cdot g_2(D_{2eff}) \cdots g_n(D_{neff})$$

$$D_{ieff} = D_i \prod_{j \neq i} \left( 1 + a_{ij} \frac{D_{jeff}/D_{0j}}{1 + D_{jeff}/D_{0j}} \right)^{-1} \quad [2]$$

The functions  $g_i$  are Hill functions appropriate to each single drug (Eq. 1) with steepness  $n_i$  and halfway point  $D_{0i}$ . They are evaluated from the single-drug response curve. The  $a_{ij}$  interaction parameters are

computed from two-drug data (Methods). This model assumes that the effects of drugs on each other's effective doses are multiplicative, and that one can neglect third-order and higher interactions (44).

To test this model, we begin by considering two-drug response surfaces (3, 45, 46). Thus, we consider Eq. 2 with only two drugs.

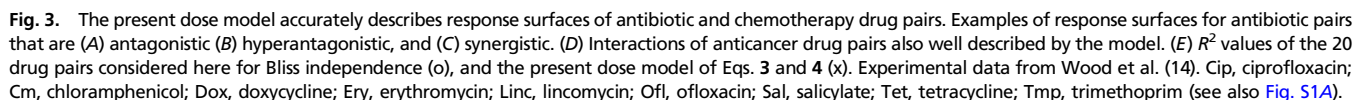


**Fig. 2.** Response of three cancer drug mixtures at multiple doses is best captured by the present dose model. Experimental measurements of the mixture of the three anticancer drugs taxol, doxorubicin, and cisplatin at all dose combinations compared with (A) Bliss independence, (B) Isserlis predictions, (C) regression model, and (D) present dose model predictions.  $R^2 = 1 - \sum (\text{Model} - \text{Experiment})^2 / \text{var}(\text{Experiment})$  can yield negative values when the mean model prediction is different from the mean experimental measurement, indicating a very poor fit.

For drug pairs, there exists an additional wealth of published data to test the model. The model fits well all interactions of 20 antibiotic pairs and two pairs of anticancer drugs measured in

$$D_{1eff} = \frac{D_1}{\left(1 + a_{12} \frac{D_{2eff}/D_{02}}{1 + D_{2eff}/D_{02}}\right)}; D_{2eff} = \frac{D_2}{\left(1 + a_{21} \frac{D_{1eff}/D_{01}}{1 + D_{1eff}/D_{01}}\right)}. \quad [4]$$

The finding that a single interaction parameter captures many of the pairs provides a picture of a hierarchy between the drugs: Drug 1 changes the effective dose of drug 2 but not vice versa (1→2). A hierarchy is obtained because we find that these relations are transitive: If drug 1 affects drug 2 (1→2) and drug 2 affects drug 3 (2→3), then drug 1 will affect drug 3 (1→3) but not vice versa. The hierarchy between antibiotics is shown in Fig. 4.



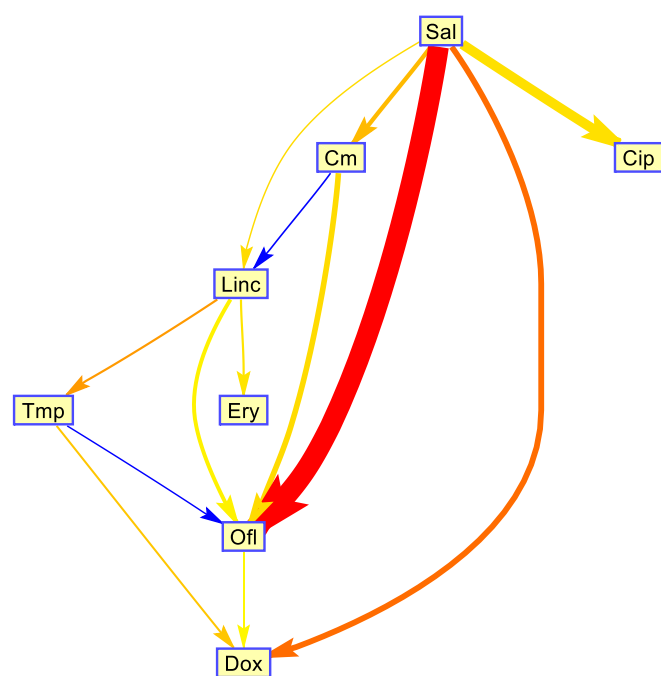


For example, salicylate is high on the hierarchy because it activates a multidrug efflux system that transports other drugs out of the bacterial cell (48) (Fig. S3).

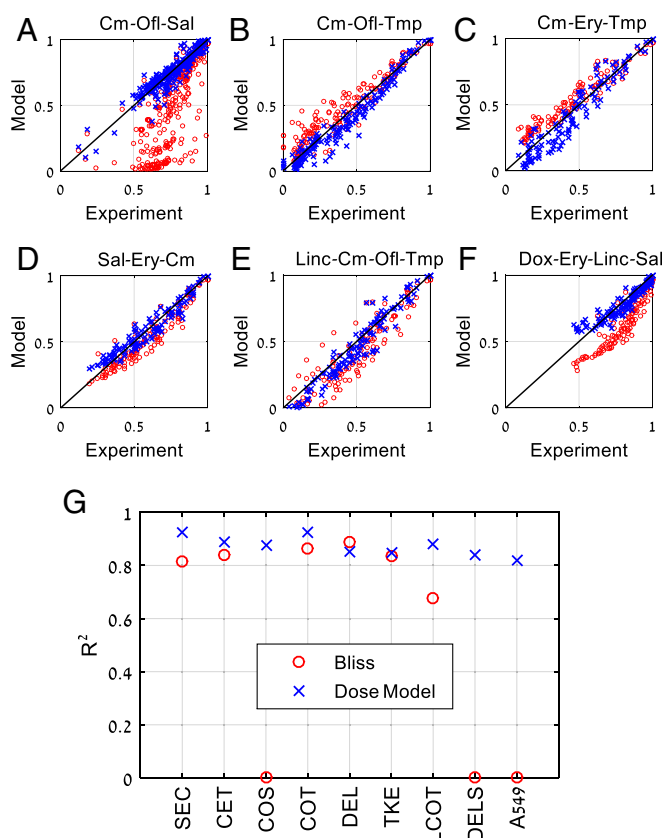
**The Dose Model Describes Combinations of Three and Four Antibiotics Using Only Pair Data.** We now turn to the anticancer drug triplet measured here. We used the  $a_{ij}$  interaction parameters for the three pairs in the triplet. We find that the dose model for three drugs (Eq. 2) describes the full three-drug interaction matrix very well ( $R^2 = 0.82$ ; Figs. 1 and 2).

We further compared the model for triplets and quadruplets of antibiotics published previously (32). The dataset includes six triplets and two quadruplets at a total of 1,384 dose combinations. The drug pairs that make up these combinations have synergy and antagonism, and several of the triplet and quadruplets are markedly non-bliss-like, so that prediction is challenging. We find that the model of Eq. 2, with  $a_{ij}$  parameters fitted from drug pair data, works very well ( $R^2 \in [0.85, 0.93]$ ) for all of these combinations (Fig. 5 and Fig. S1B).

For example, consider the antibacterial triplet chloramphenicol, ofloxacin, and salicylate. Salicylate is highest in the hierarchy and antagonistic to the other two antibiotics (48, 49). In the model, this antagonism is represented by the parameters  $a_{23} = 7.2 \pm 0.4$  and  $a_{13} = 2.8 \pm 0.3$ . The remaining pair has mild antagonism ( $a_{21} = 0.5 \pm 0.02$ ). The triplet shows very strong antagonism predicted accurately by the model [ $R^2 = 0.88$ ; compare with Bliss  $R^2 \approx 0$  (Fig. 5A)].



**Fig. 4.** A hierarchy between antibiotics. For most of the drug pairs, one of the two interaction parameters  $a_{12}$  or  $a_{21}$  can be set to zero without significant loss of fit quality, resulting in a single parameter for the interaction. In these cases, we can say that drug 1 changes the effective dose of drug 2 but not vice versa (1→2). We find that these relations are transitive: If drug 1 affects drug 2 (1→2) and drug 2 affects drug 3 (2→3), then drug 1 will affect drug 3 (1→3) but not vice versa. The direction of the interaction is transitive, but the absolute strength of the interaction is not always transitive. To quantify the strength of the hierarchy we use the goodness of fit (RMSE) difference in the case of  $a_{12} = 0$  and  $a_{21} = 0$ . This quantity is indicated by the arrow thickness. The strength of the interaction is indicated by the color of the arrow (red, strong antagonistic; blue, strong synergistic). We plotted only interaction with nonnegligible hierarchy ( $\Delta\text{RMSE} > 0.005\%$ ). Note that 8 out of the 28 possible interactions were not present in the published dataset.

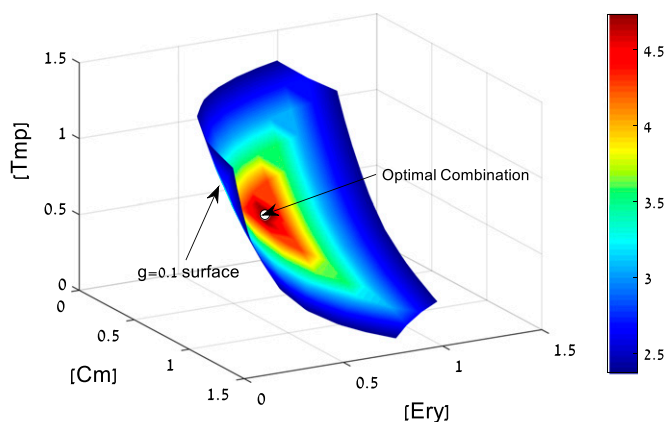


**Fig. 5.** Combinations of three or four drugs are well described by the present dose model (x). Bliss independence (o) results are displayed for comparison. The three-drug combination Cm-Ofi-Sal shows strong antagonism (B) The three-drug combination Cm-Ofi-Tmp show synergism. (C) The three-drug combination Cm-Ery-Tmp shows synergism. (D) The three-drug combination Sal-Ery-Cm shows mild antagonism (E) The four-drug combination Linc-Cm-Ofi-Tmp shows complex interactions captured by the model. (F) The four-drug combination Dox-Ery-Linc-Sal shows antagonism. (G)  $R^2$  values for three- and four-drug combinations: Bliss model (o) and the present dose model (x). Antibiotic data are from Wood et al. (32); results for the present experiments on three anticancer drugs on A549 cells (Figs. 1 and 2) are also presented. Cm/C, chloramphenicol; Dox/D, doxycycline; Ery/E, erythromycin; Linc/L, lincomycin; Ofi/O, ofloxacin; Sal/S, salicylate; Tmp/T, trimethoprim. Isserlis model for quadruplets is  $g_{1234} = g_{12}g_{34} + g_{13}g_{24} + g_{14}g_{23} - 2g_1g_2g_3g_4$  (see also Fig. S1B).

A second example that includes both synergy and antagonism is the triplet chloramphenicol, ofloxacin, and trimethoprim (Fig. 5B). Here ofloxacin and trimethoprim are synergistic ( $a_{23} = -0.8 \pm 0.05$ ) as are chloramphenicol and trimethoprim ( $a_{31} = -0.57 \pm 0.08$ ), whereas chloramphenicol and ofloxacin are antagonistic ( $a_{21} = 0.99 \pm 0.07$ ). Thus, a priori, it is difficult to predict the synergy/antagonism of the triplet. The model predicts overall synergy, and fits the experiment very well ( $R^2 = 0.93$  compared with Bliss  $R^2 = 0.86$ ).

**The Dose Model May Be Used to Optimize Drug Combinations for Minimal Side Effects.** The dose model described here can be used to navigate the space of multidrug doses to find combinations of interest. As a schematic example, we consider the problem of finding a drug combination with a given efficacy that has minimal side effects. This example is meant to demonstrate a general approach, which can be made more realistic with accurate models for side effects or other features that need to be optimized.

To illustrate this, we consider a triplet of antibiotics—chloramphenicol, erythromycin, and trimethoprim. The model allows calculating all dose combinations with a given effect, say a 10-fold growth reduction of the bacteria,  $g = 0.1$ . The dose combinations that give  $g = 0.1$  form a surface in the 3D space of doses (Fig. 6).



**Fig. 6.** Search for a mixture with high efficacy at low doses. We seek a combination of three antibiotics with a given large effect ( $g = 0.1$ ). The doses that satisfy this condition form a surface in the 3D dose space for chloramphenicol (Cm), erythromycin (Ery), and trimethoprim (Tmp). On this surface, we seek the combination with minimal side effects. Assuming that side effects increase with drug doses, we can seek to minimize, for example, the maximal dose in the combination  $M = \max(D_i/D_{0i})$ . The colors indicate the decrease in  $M$  relative to the lowest  $D_i/D_{0i}$  of the individual drugs. The optimal drug combination indicated by an arrow on the  $g = 0.1$  surface has a fourfold-lower  $M$  than the best individual drug (see also Fig. S4).

On this surface, we seek the combination with minimal side effects. Assuming that side effects increase with drug doses, we can seek to minimize, for example, the sum of normalized doses  $S = \sum D_i/D_{0i}$  (Fig. S4). Another possibility is to minimize the maximal dose in the combination  $M = \max(D_i/D_{0i})$ . In both cases, an optimal drug combination is found that uses lower doses than the best individual drug (indicated by an arrow on the  $g = 0.1$  surface in Fig. 6). The combination that minimizes summed doses has a twofold lower total dose than the best individual drug (Fig. S4). The combination that minimizes maximal dose has a fourfold lower dose than the best individual drug (Fig. 6).

## Discussion

We presented a model for the effects of multidrug mixtures for anticancer drugs and antibiotics. The model does not require knowledge of the mechanism of drug action, and is based on relatively few measurements on drug pairs. The model accurately describes published data on antibiotic triplets and quadruplets, as well as experimental data presented here on dose-response of combinations of three cancer drugs.

The model has two interaction parameters for each pair,  $a_{12}$  and  $a_{21}$ . These parameters describe how the effective dose of a drug is affected by the presence of the other drug. The parameters can be accurately estimated based on about 10 dose combinations for each pair. The use of several dose combination measurements to estimate the parameters helps reduce the effects of experimental noise, partly explaining why the present model is more accurate than previous mechanism-free models such as the Isserlis model and regression-based models (Fig. S5).

The fitted interaction parameters reveal a hierarchy between the drugs. Some drugs impact the effective dose of the other drug but not vice versa. This relationship is transitive and can offer clues about the mechanisms of synergy and antagonism.

For example, a drug high in the hierarchy is likely to set off general drug resistance systems, as in the case of salicylate, which activates the *mar* system in bacteria (Fig. S3).

The present approach can overcome the combinatorial explosion problem in which the number of experiments rises exponentially with the number of drugs and doses, because it requires few measurements. Instead of  $D^N$  measurements for  $N$  drugs and  $D$  doses, we can use the single-drug dose-response curves plus a sampling of the pair dose combinations to fit the interaction parameters  $a_{ij}$ . In total, this model requires only a quadratic number of measurements,  $N \cdot D + cN(N-1)/2$ , where  $c$  is  $\sim 10$ . This means that for  $N = 6$  drugs and  $D = 8$  doses, we need only 198 measurements instead of  $D^N \approx 3 \cdot 10^5$ . For  $N = 10$  drugs and  $D = 8$  doses, we need only 530 measurements instead of  $\sim 10^9$ . This approach therefore potentially allows navigating the space of high-order drug combinations to search for mixtures with high efficacy at low dose.

## Methods

**Regression Model.** Machine learning approaches often use regression models. A commonly used regression formula employs the variables  $x_i = 0$  or 1 that denote the absence or presence of drug  $i$  in the mixture. The effect of the mixture  $g$  is described in the model as  $\log(g) = \sum b_i x_i + \sum c_{ij} x_i x_j$ . The parameters  $b_i$  and  $c_{ij}$  are fit from single and pair data. For triplets, the equivalent formula is  $g_{123} = g_{12}g_{13}g_{23}/g_1g_2g_3$ . For quadruplets,  $g_{1234} = g_{12}g_{13}g_{14}g_{23}g_{24}g_{34}/(g_1g_2g_3g_4)^2$ .

**Estimation of Model Parameters.** We determine the values and confidence intervals of the model parameters ( $n_i$ ,  $D_{0i}$ , and  $a_{ij}$ ) using the MATLAB function "fit." We use the single-drug dose-response curve to estimate the values and uncertainty of  $n_i$  and  $D_{0i}$  for each drug. The interaction parameters  $a_{ij}$  are determined by the two-drug response matrix. In the process of fitting  $a_{ij}$ , we allow  $n_i$  and  $D_{0i}$  to change within their uncertainty estimated from the single-drug measurements.

**Computation of Effective Doses in the Model.** In the general case  $a_{ij} \neq 0$ , we determine the effective dose by numerically solving Eq. 2 using the MATLAB function "fmincon." When there exists a hierarchy between the drugs in the combination and  $\{a_{ij} = 0 | a_{ji} = 0\}$ , there is an analytic solution to Eq. 2 that one can use instead of a numerical solution

$$D_{1\text{eff}} = D_1; D_{i\text{eff}} = D_i \prod_{j>i} \left( 1 + a_{ij} \frac{D_{j\text{eff}}/D_{0j}}{1 + D_{j\text{eff}}/D_{0j}} \right)^{-1}.$$

**Cell Lines and Culture Conditions.** Measurements were performed by BioDuro (email bioduroinfo@bioduro.com). A549 (non-small cell lung cancer) cells were grown in 384-well plates (#3707; Corning) plated at  $10^4$  cells per well. Plates were incubated at 37°C and 5% (vol/vol) CO<sub>2</sub> for 24 h in membrane-filtered growth media composed of RPMI (Roswell Park Memorial Institute) 1640 with L-glutamine (#11875093; Invitrogen) supplemented with 10% FCS [certified FBS, FBS (#SH30084.03; HyClone)], and 0.05% Penicillin-Streptomycin (#15140-122; Invitrogen). After 24 h, the drugs (taxol, doxorubicin, and cisplatin) were added (2.5  $\mu\text{L}$  per well) to final concentrations of 20  $\mu\text{M}$ , 10  $\mu\text{M}$ , 3.3  $\mu\text{M}$ , 1.1  $\mu\text{M}$ , 370 nM, 123 nM, 41 nM, and 13.7 nM and two controls: 0.1% DMSO and 2.5  $\mu\text{L}$  of regular media (untreated). Cells were incubated with drugs for 48 h, followed by a cell survival assay [3-(4,5-dimethylthiazol-2-yl)-2,5-diphenyltetrazolium bromide].

**Cell Survival Assay.** The viability assay was done using an MTT-based in vitro toxicology assay (#C0009; Beyotime). Cells were incubated with reconstituted MTT for 4 h, and absorbance was measured at 570 nm.

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