



HW2

Speaker : Alan

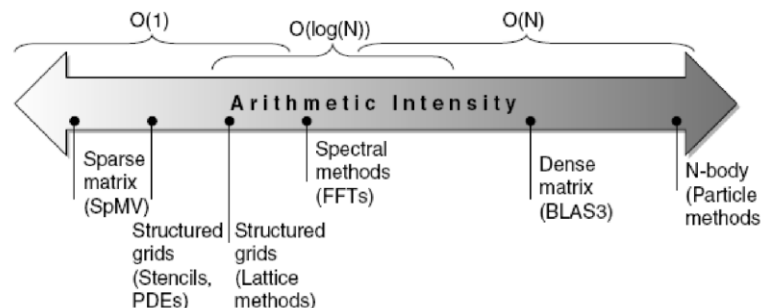
Advisor : Prof. An-Yeu Wu

Date : 2022/09/20



Roofline Visual Performance Model

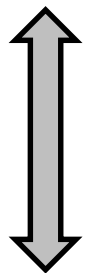
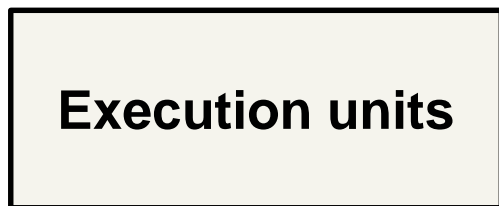
- ❖ A simple performance model : Execution vs. Data Transfer
- ❖ Three key factors
 - ❖ System Spec (Hardware Level)
 - Computation : peak floating point performance
 - Floating-point ops /sec
 - Memory: peak memory bandwidth
 - Bytes per sec
 - ❖ Program characteristics (Algorithm Level)
 - Arithmetic intensity : Floating-Point Ops/ byte
 - Ratio of floating-point operations in a program to the number of data types accessed by a program from main memory





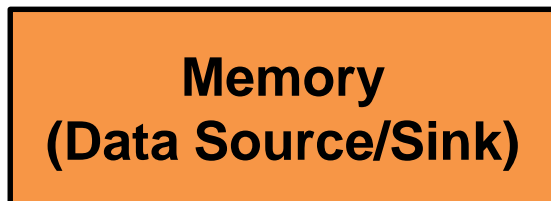
Simplistic view

Max. Performance P_{peak}



Data Path :
Bandwidth

b_s



❖ How fast can tasks be processed?

❖ The Bottleneck:

❖ The execution of Work:

➤ P_{peak} [flops : flop/s]

❖ The data path

➤ $I * b_s$ [flop/byte * byte/s]

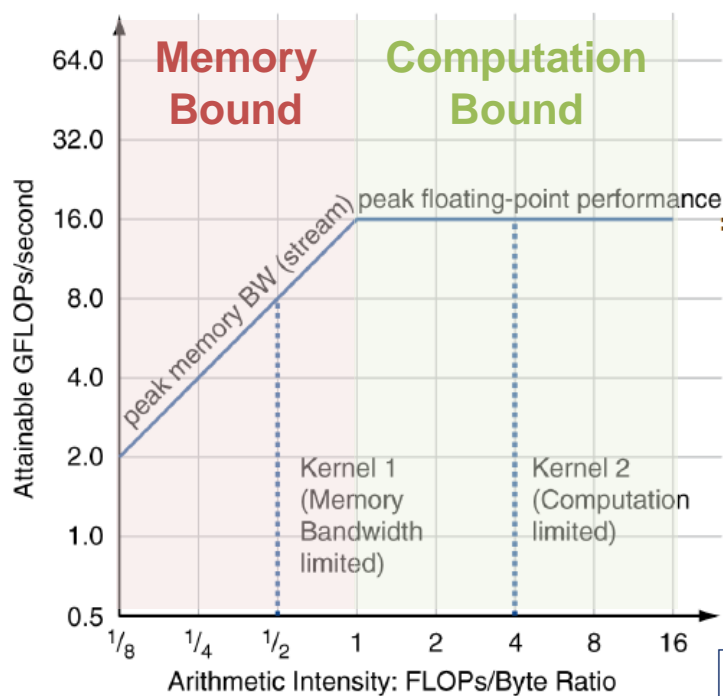
➤ I : Arithmetic Intensity

❖ Roofline Model Equation

$$P = \min(P_{peak}, I * b_s)$$



Roofline Diagram



Memory Bandwidth Limited

Floating-Point Ops/sec

= Peak Bytes/sec x Floating-Point Ops/ byte

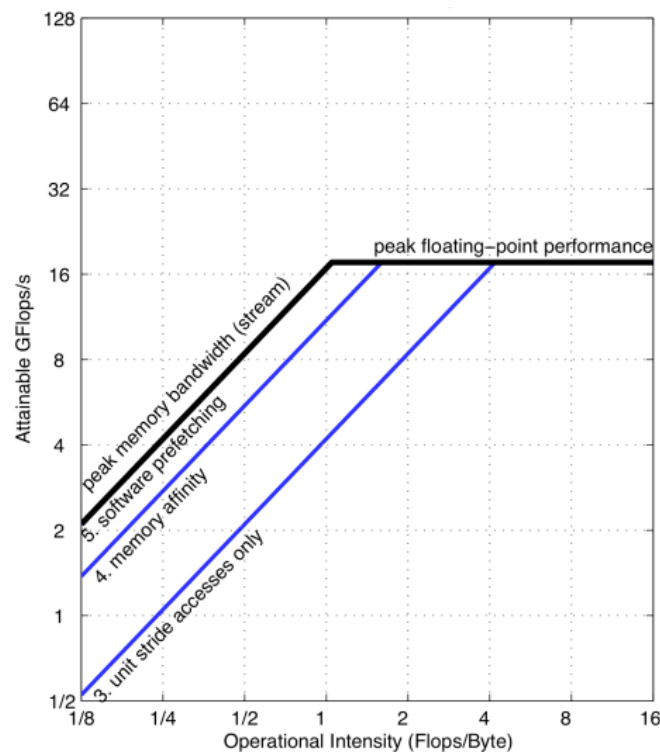
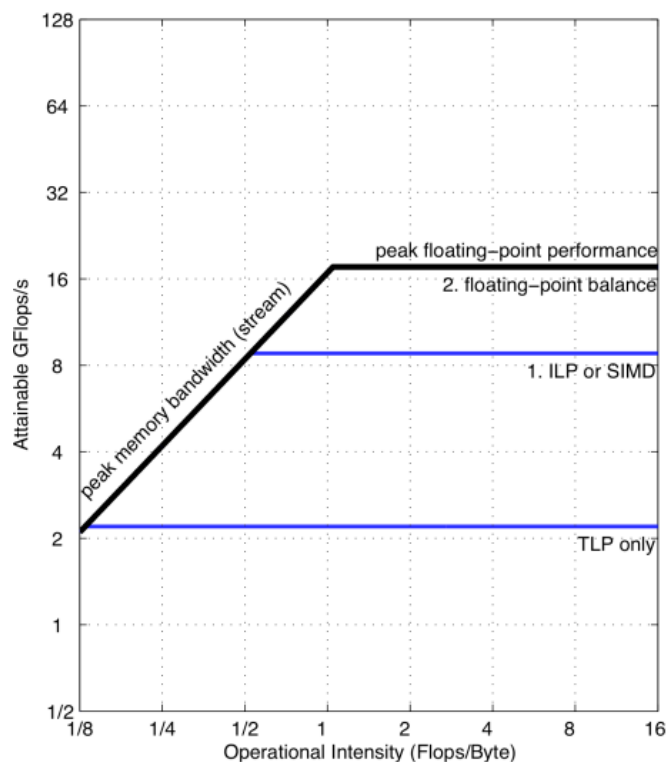
Computation Limited

Peak Floating-Point Ops/sec

(assuming 16GB/sec peak bandwidth)



Roofline Analysis



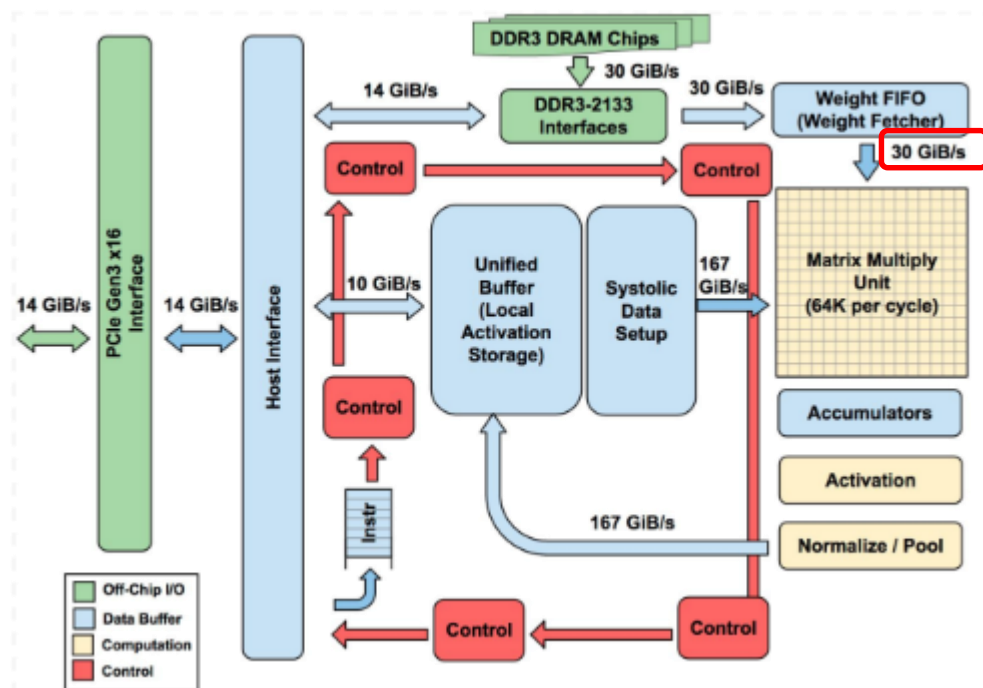
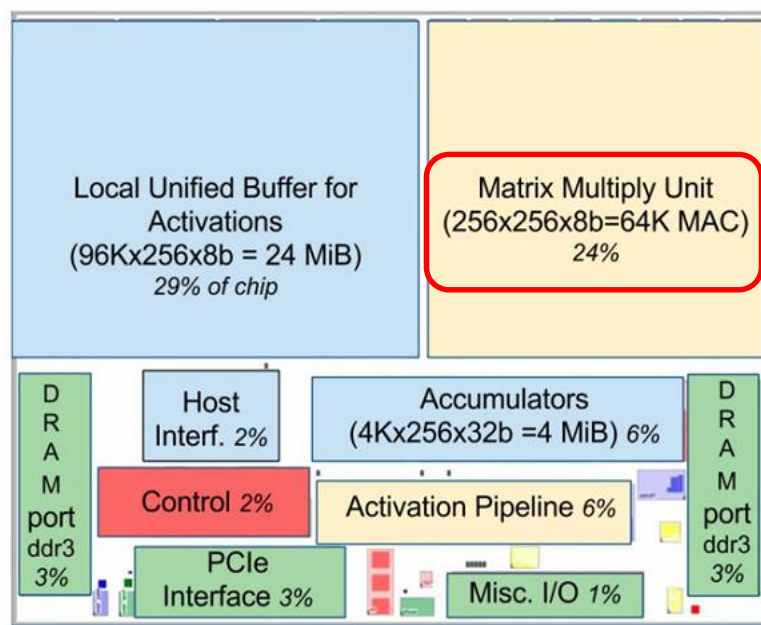
- ❖ The Roofline model gives an upper bound to performance.
- ❖ Need some techniques to achieve the ceiling

*TLP : Thread-Level Parallelism
ILP : Instruction-Level Parallelism



HW2 – Roofline Model

❖ TPU Example



Peak Performance :

$$64 * 1024 * 2 * 700 * 10^6 = 91.7504 \text{ Tops}$$

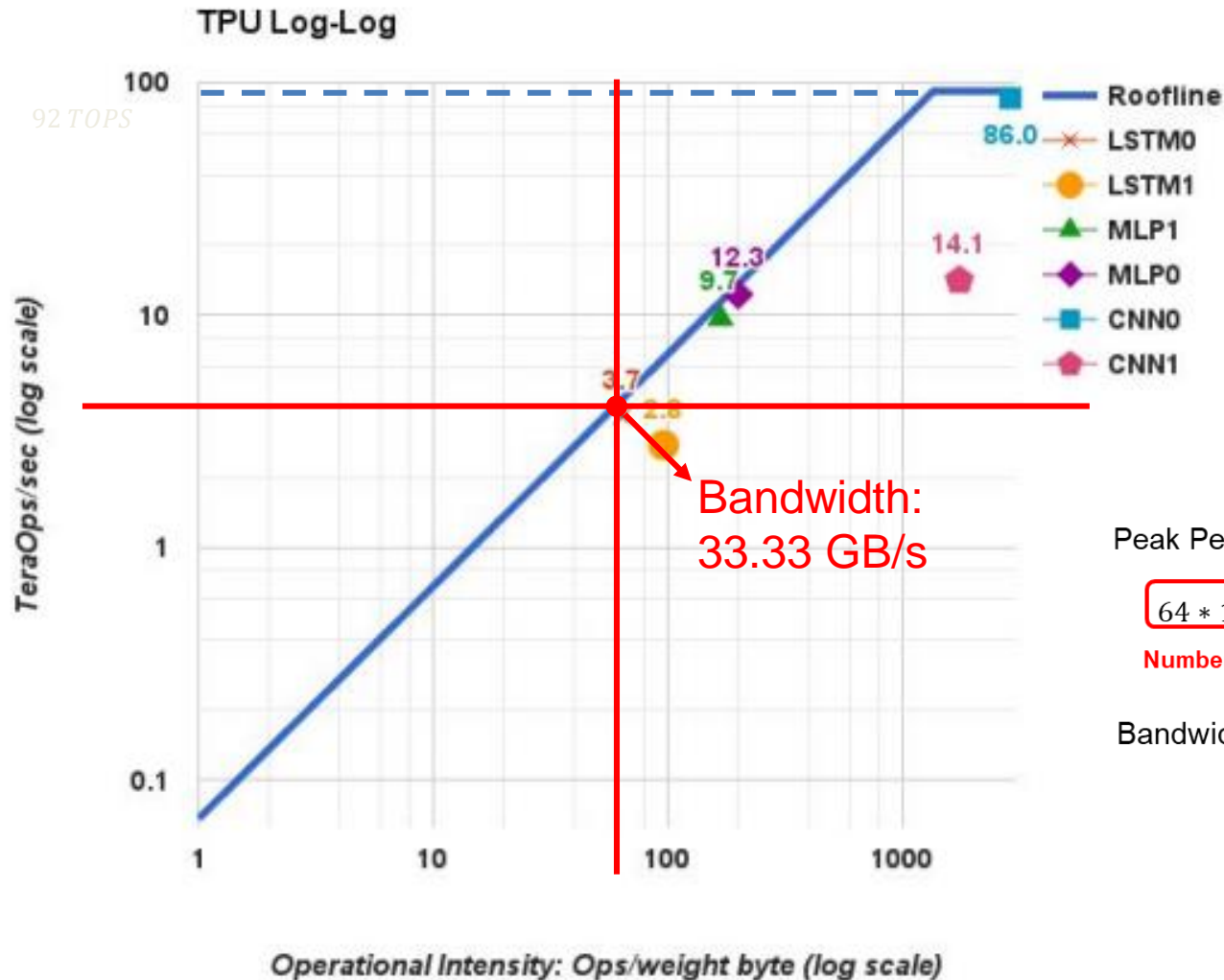
Number of PE MAC Frequency

Bandwidth:

$$30 * \frac{2^{30}}{10^9} = 32.2 \text{ GB/s}$$



HW2 – Roofline Model



Peak Performance :

$$64 * 1024 * 2 * 700 * 10^6 = 91.7504 \text{ Tops}$$

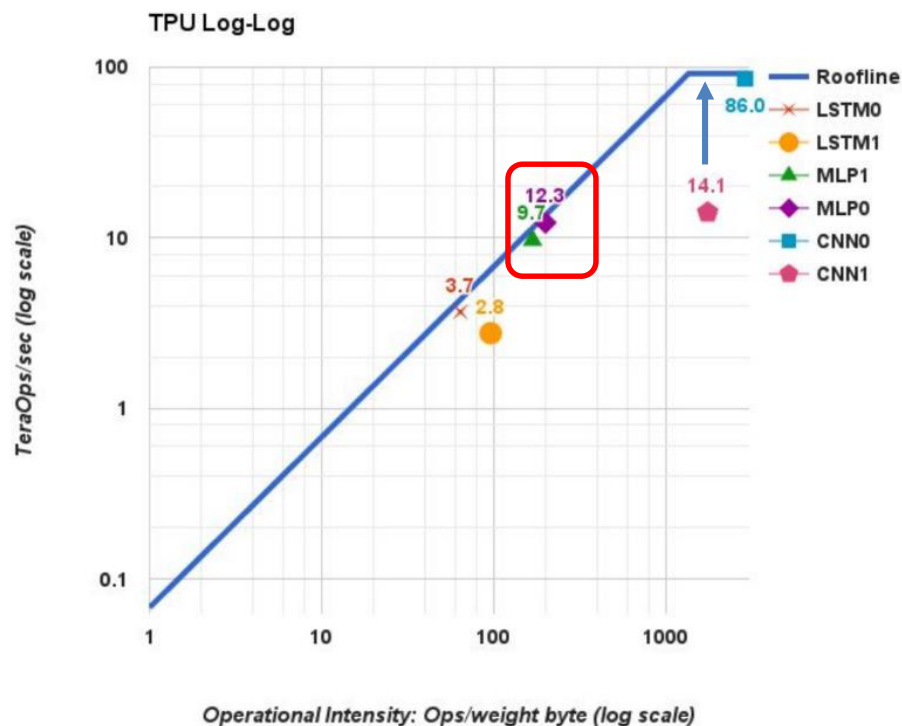
Number of PE MAC Frequency

Bandwidth:

$$30 * \frac{2^{30}}{10^9} = 32.2 \text{ GB/s}$$



Roofline Model : TPU



Application	CNN0	CNN1
Array active cycles	78.2%	46.2%
Useful MACs in 64K matrix (% peak)	78.2%	22.5%
Unused MACs	0.0%	23.7%
Weight stall cycles	0.0%	28.1%
Weight shift cycles	0.0%	7.0%
Non-matrix cycles	21.8%	18.7%
RAW stalls	3.5%	22.8%
Input data stalls	3.4%	0.6%
TeraOps/sec (92 Peak)	86.0	14.1

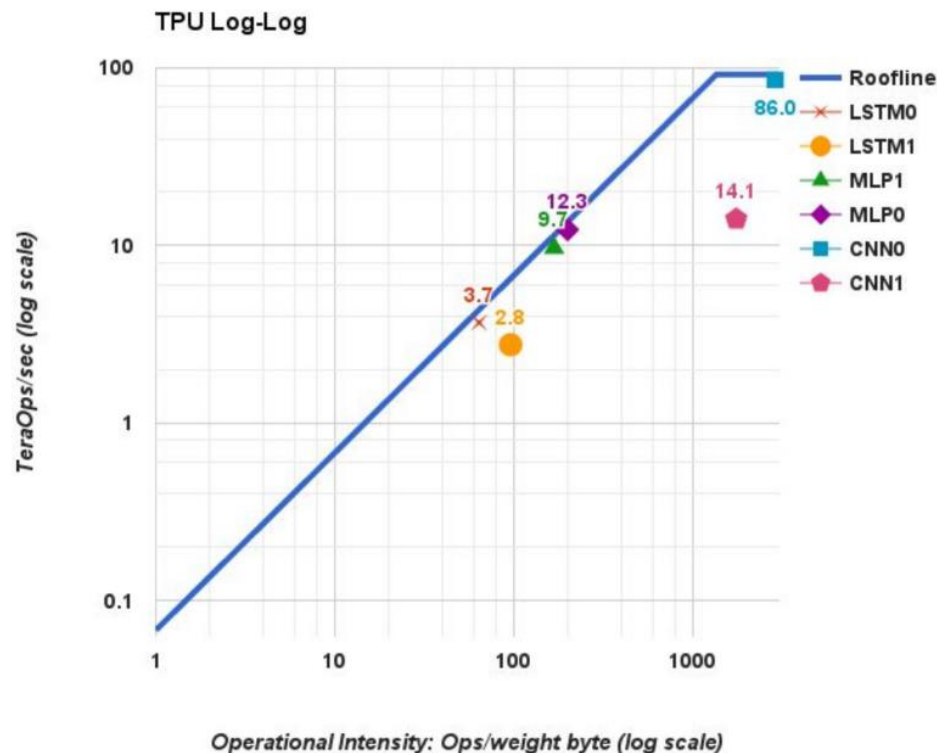
Low Utilization

- ❖ Fully connected layer is less operation-intensive than convolution layer.
- ❖ CNN1 has some layers with shallow feature depths.
 - ❖ Utilization is not high
 - The actual efficiency is far away from ceiling



Problem 1 (20 points)

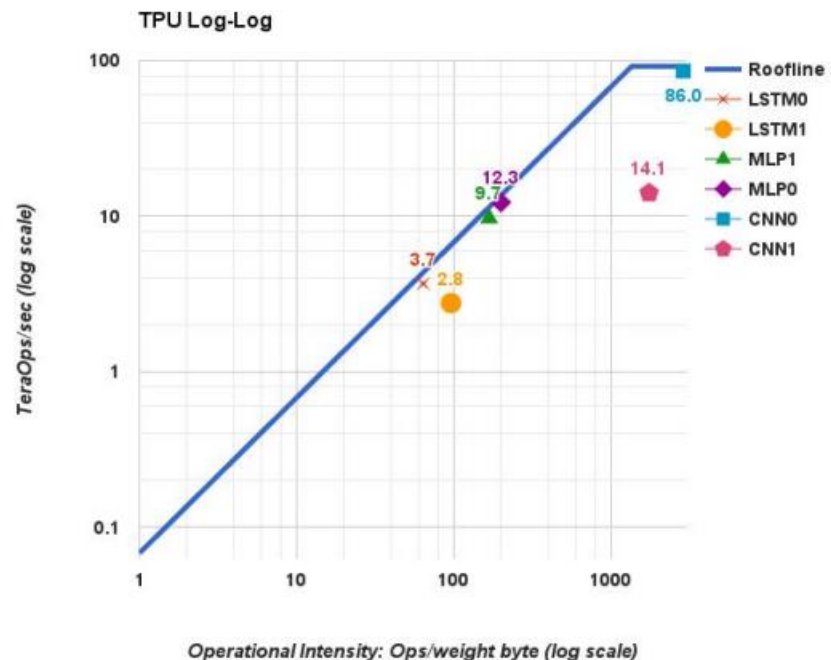
- ❖ Recap the concept of arithmetic intensity (AI)
- ❖ Compare and discuss the arithmetic intensity of LSTM, MLP, and CNN





Problem 2 (20 points)

- ❖ Goal
 - ❖ Understand the meaning of the roofline model
 - ❖ Adjust the roofline according to different specification
- ❖ Plot the roofline curve if the TPU has upgraded its PE array
 - ❖ From 256x256 to 320x320





Problem 3 (60 points)

- ❖ Goal
 - ❖ Understand the meaning of the roofline model
 - ❖ Adjust the roofline according to different specification
- ❖ Plot the roofline model if we change the hardware
 - ❖ CPU (Haswell), GPU (Nvidia K80), and TPU

Model	Die										Benchmarked Servers				
	mm ²	nm	MHz	TDP	Measured		TOPS/s		GB/s	On-Chip Memory	Dies	DRAM Size	TDP	Measured	
					Idle	Busy	8b	FP						Idle	Busy
Haswell E5-2699 v3	662	22	2300	145W	41W	145W	2.6	1.3	51	51 MiB	2	256 GiB	504W	159W	455W
NVIDIA K80 (2 dies/card)	561	28	560	150W	25W	98W	--	2.8	160	8 MiB	8	256 GiB (host) + 12 GiB x 8	1838W	357W	991W
TPU	NA*	28	700	75W	28W	40W	92	--	34	28 MiB	4	256 GiB (host) + 8 GiB x 4	861W	290W	384W



Requirements

- ❖ The report should be merged as a single **pdf file** and **uploaded to NTU COOL**.
 - ❖ Example of filename: AVLSI_HW2_d09943011.pdf
 - ❖ Note that you have to replace d09943011 with your student ID number
- ❖ Deadline: 2022/09/26 23:59
 - ❖ Late submission will only get half score (deadline: 2022/09/30 23:59)