**Accessories dominate the costs of producing seed**

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[general comment: these are all at some level costs of sex -- at face value, a selfing or apomictic species would not need to produce any surplus ovules, plus would not need showy flowers -- accessory costs would be strictly fruit and seed-coat structures for successfully-provisioned seeds]

# Abstract

Despite the obvious importance of quantifying energy allocation to reproduction, relatively few complete estimates of reproductive investment (RE) exist across multiple species in a community. RE includes energy directly invested in seeds, energy invested in required non-seed tissues (termed success costs; including petals, pedicels, seed pods, and dispersal tissues), and energy invested in plant parts that fail to develop into seeds. To quantify the size of these pools and how they shifted across co-occurring species, we collected detailed RE measurements for a year from 14 perennial species in a recurrent-fire coastal heath community in eastern Australia. Total accessory costs, the proportion of RE not directly invested in provisioning the seed, were enormous, varying from 92% to 99.8% across the study species. While discarded tissue costs accounted for the largest proportion of RE for most species, success costs were not negligible. From this follows that studies using seed or fruit production as measures of reproductive investment vastly underestimate RE. In addition, among individuals within and across species, RE and seed production were only weakly correlated likely due to stochastic processes that affect seed set. A quite accurate and easy to measure estimate of RE was obtained from a composite variable “bud count\*flower mass”.

Merging the predictions of the seed size-number trade-off and the trade-off between investment in pollen attraction versus seed provisioning tissues (from the parental optimist-pessimist literature), we predicted coordinated shifts in floral construction costs, seedset and seed size, reflecting alternate strategies to maximize fitness. As predicted, large-seeded species had low seed set (were parental optimists) and had relatively low pollen-attraction costs (relative to seed provisioning costs) while small-seeded species displayed the alternate suite of traits. This coordination occurs, because larger-seeded species produce relatively fewer seeds, and are therefore predicted to be more selective about the genotypes of embryos they provision, leading to lower seedset. This selectivity requires a greater excess of ovules, in turn selecting for a reduction in per-ovule pollen-attraction costs. Incorporating tissue construction costs in the seed size-number trade-off extends our understanding of the relatives sizes of floral and fruiting structures observed across angiosperms.

# Introduction

Plants allocate a sizeable proportion of their photosynthetic energy to reproduction (Obeso 2004; Hirayama *et al.* 2008; Thomas 2011; Wenk & Falster 2015), into both seeds as well as the many other tissues associated with reproduction, termed accessory costs. Accessory costs include energy required to form a successful seed (e.g. flower petals, seed pod, and dispersal tissues) and energy lost via aborted and discarded buds, flowers and fruit. Previous studies show that for perennial species anywhere from 15% – 99% of total reproductive investment may go into accessory costs (Haig & Westoby 1988; Ashman 1994; Henery & Westoby 2001; Lord & Westoby 2006; Chen, Felker & Sun 2010). Since fruit set and seed set are generally below 50% in perennial species (Stephenson 1981; Wiens 1984; Sutherland 1986; Knight *et al.* 2005; Rosenheim *et al.* 2014), the cost of aborted and discarded tissues may be a substantial proportion of total accessory costs. Yet, despite being a significant energy sink in ecosystems, little is known about the allocation of energy among different reproductive tissues across the plant kingdom and how this links with plant reproductive strategies.

While plant species demonstrate an extraordinary diversity of reproductive structures and strategies, reproductive investment can be divided into broad functional categories that are consistent across species (Figure 1a). Defining such categories is a prerequisite to determining if species vary in the size of these reproductive tissue pools and asking if underlying trade-offs in energy allocation explain the observed variation. The total energy investment per seed matured are the *reproductive costs per seed,* which can be divided into the investment in required parts, termed the *success costs* and the energy expenditure on flowers, fruit, and seeds that never form mature propagules, so-called *discarded tissue costs*. Both are calculated on a *per seed matured* basis. *Success costs* can be further divided into structures that form before pollination (*pollen-attraction costs*; i.e. the flower, including petals, calyx, pedicel) versus structures developed post-pollination (e.g. seed pod, seed), hereafter termed *provisioning costs*. The provisioning component is comprised of the seed itself (*seed costs,* i.e. seed size) versus the dispersal and packaging tissues. The *discarded tissue costs* can likewise be divided into energy invested prior to versus after pollination, here termed *discarded pollen-attraction costs* and *discarded provisioning costs. Accessory costs*, all tissues besides the seed itself,are the sum of *discarded tissue costs, pollen-attraction costs, and packaging and dispersal costs,* high-lighted in red in Figure 1*.* Throughout the manuscript the “costs” indicates investment per seed matured, while “investment” refers to total dry weight invested in a structure.

There are multiple reasons to expect that both success costs and discarded tissue costs will be substantially larger than the weight of the seed itself. Investment in the success cost components is undeniably beneficial for the successful formation and dispersal of a seed. Without showy petals insects would not be attracted to the stamens and stigma, without sepals the developing bud would not be protected, without a seed coat a seed would not be protected during dispersal, and without an attractive fruit, many seeds would not be dispersed. High discarded tissue costs (due to low seedset both pre- and post-pollination) occur in perennial plants for a diversity of reasons, some the result of conditions beyond the plant’s control and others by evolutionary design to increase fitness. They include pollen-limitation, pollen-ovule incompatibility, parental embryo abortion, resource limitation and also as a bet-hedging strategy to capitalize on stochastic variation in pollen availability, pollen quality, and resource availability to mature fertilized ovules (Bierzychudek 1981; Stephenson 1981; Sutherland 1986; Burd 1994, 2008; Ramsey 1997; Obeso 2004; Ashman *et al.* 2004; Knight *et al.* 2005; Holland & Chamberlain 2007; Rosenheim, Schreiber & Williams 2015).

Across species variation in the relative size of the reproductive tissue energy pools (Figure 1a) should indicate different reproductive energy allocation strategies underpinned by trade-offs. Plants will differ in how they divide their finite pool of reproductive energy into different tissue types, displaying variation in relative investment in pollen-attraction versus provisioning costs as well as variation in the number of ovules formed and the number of seeds matured. Two established reproductive strategy trade-offs have already investigated relationships between some reproductive energy pools and reproductive parts counts and here we expand upon their hypotheses. The first is the well-supported seed size-seed number trade-off central to the plant functional trait literature and the second is the seed set-pollen-attraction cost trade-off described in the parental optimist-parental pessimist literature.

**Seed size – seed number trade-off:** Previous studies have shown that, plants, relative to their size, have a fixed energy budget to invest in seeds, leading to the seed size - seed number trade-off. Plants can divide this pool of energy into many small seeds or fewer larger seeds, such that a log-log plot of seed size versus scaled seed count should have a slope of -1 (Smith & Fretwell 1974; Henery & Westoby 2001; Sadras 2007). Very small and very large seeds represent endpoints of a continuous life history strategy (Rees & Westoby 1997; Leishman 2001; Turnbull et al. 2004; Moles & Westoby 2006), with small-seeded species displaying superior colonization ability, while larger-seeded species have a greater likelihood of establishing and better competitive outcomes. In turn, since large-seeded species produce fewer seeds, they display a suite of traits to ensure that a greater proportion of their seeds successfully establish (Moles & Westoby 2006).

While well-supported by empirical data, the seed size-seed number trade-off does not consider energy invested in accessory tissues, leading us to hypothesize two related trade-offs. First, we suggest plants, relative to their size, should invest a fixed amount of energy maturing ovules to the point of pollination, depicted as a trade-off between pollen-attraction costs and the number of ovules that are displayed to pollinators (Figure 1b). Species with higher pollen-attraction costs will be able to produce fewer ovules. Second, we hypothesize that plants, again relative to their size, should display a trade-off between total reproductive costs and seed count (Figure 1b). This trade-off is similar to the seed size-seed count trade-off, but includes all of a plants reproductive energy expenditures to construct a seed, not just the seed weight itself. Both trade-offs are predicted to have a slope = -1, but the pollen-attraction costs – ovules at point of pollination trade-off should have a higher intercept, since seed set is <1. These are two independent trade-offs, each simply showing there exists a fixed pool of energy to spend. Species variation in seedset, the ratio of seed count to ovule count, provides the link between these two trade-offs – and is itself one of the axes in the trade-off described below.

**The pollen attraction-seed provisioning versus seed set trade-off:** Haig & Westoby (1988) developed a conceptual model for the relative allocation of energy to different reproductive tissues, dividing the total energy investment per seed between the costs of attracting pollen versus the cost of provisioning pollinated ovules. Their simple model makes several predictions, including that plants 1) produce excess ovules and flowers to optimize seed production across a population and across time, 2) face a trade-off between pollen attraction and embryo provisioning, and 3) allocate just enough to pollen-attracting tissues to ensure pollination of the number of ovules they are able to provision *on average*. This initial model has since been extended to use the proportion of energy invested in pollen attraction versus seed provisioning tissues to predict seed set across species (Rosenheim *et al.* 2014, 2016; Burd 2016). The models, supported by empirical data, indicate that species with relatively low pollen-attraction costs (in their studies, defined as successful and discarded costs) should produce a greater excess of ovules, relative to what they are able to provision, manifested as lower seedset.

This axis of variation accords with the parental optimist-parental pessimist strategy continuum (Mock & Forbes 1995; Burd 2008; Rosenheim *et al.* 2014). A parental optimist is defined as a species that overproduces ovules, relatively few of which mature in an average year due to limited resource supply. Such a species is forever “optimistic” that it will have higher-than-average provisioning resources and overproduces ovules should environmental conditions be unusually favourable. Since an optimist discards so many ovules – both pollinated and unpollinated – it must reduce the cost of producing a single pollinator-ready ovule. The alternative, a species with proportionally higher pollen-attraction costs should display parental pessimism: an underproduction of ovules, with embryo number limiting seed production in many years, often as a result of pollen limitation.

Since parental optimists have lower seedset (seed to ovule ratio), logically they need to ensure that the seeds they mature are likely to germinate and establish. One mechanism to increase seed and seedling success is to invest more resources in embryo provisioning, manifested as higher packaging and dispersal costs and higher seed mass. High per seed resource investment in turn requires that the plant provision embryos that are vigorous genotypes, in part accomplished by being selective about which pollen grains to use and which zygotes to provision, termed selective abortion. This has been shown to be an important mechanism to increase plant fitness (Willson & Burley 1983; Sutherland 1986; Kozlowski & Stearns 1989; Guittian 1993; Melser & Klinkhamer 2001; Harder & Barrett 2006). A parent plant can exert stronger zygote selection if there is a large pool of excess embryos, exactly the strategy displayed by a parental optimist. In summary, we expect the ratio of ovules to seeds, defined here as *choosiness* (the inverse of *seedset*), to be highest in parental optimists, those species with relatively lower pollen-attraction costs (Figure 1c). (Note, that *choosiness* as defined here, encompasses a number of processes that occur between ovule maturation and the onset of zygote provisioning, including pollen-limitation, pollen-ovule incompatibility, and selective embryo abortion. It is illogical that pollen-limitation or pollen-ovule incompatibility – on a proportional basis – would be higher in plants with a relatively higher ovule count, such that selective embryo abortion is the most likely explanation for low seedset among parental optimists.)

The trade-offs described embody different reproductive tissue measures, but both represent the same reproductive strategy continuum. At one end of the spectrum are species that produce relatively few, large seeds, and have low seedset due to resource limitation. They display greater selectively in which zygotes to provision, since they are investing more energy in each offspring and maturing fewer seeds. These species invest proportionally more in seed provisioning and relatively less in pollen attraction per ovule. Parental pessimists have the same energy to invest in both ovules and seeds, but produce relatively fewer, more costly ovules and relatively more, less costly seeds. Two previous studies have indeed observed that big-seeded species have lower seedset, also attributed to greater choosiness (Lord & Westoby 2012).

Based on these trade-offs we predict that the proportion of reproductive energy going to the different outcomes in Figure 1a will shift with seed size: 1) With increase seed size, species will spend a decreasing proportion of their success costs on pollen-attraction costs, as they are expected to produce a large number of inexpensive ovules (Figure 1d). 2) In large-seeded species total pre-provisioning investment will be predominately into discarded tissues, as most of the ovules produced will be shed or aborted before the onset of provisioning (Figure 1e). 3) Once large-seeded species begin provisioning a zygote they are more likely to successfully create a viable seed, such that the proportion of total provisioning investment allocated to successful tissues versus discarded tissues should be higher in large-seeded species (Figure 1e).

In summary, we ask the following questions:

1. How much do individual plants invest in different reproductive tissues and does the proportional investment differ among species?
2. Do the hypothesized pollen attraction costs-ovules available for pollination and success costs-seed count trade-offs exist?
3. Is there a trade-off between choosiness and pollen-attraction costs?
4. Does the proportion of energy allocated to different reproductive tissue types shift with seed size?
5. Within a species, do total accessory costs or particular accessory cost components shift with plant size, age, or reproductive investment?

The dataset we use to address these questions is, to our knowledge, the most complete dataset that simultaneously measured plant size, vegetative investment, reproductive investment, seed investment, seed count, and seed mass across multiple species at different size and ages in a native community. In a recurrent-fire coastal heath community, we studied fourteen species differing in seed size, lifespan, and maximum height. Individuals were sampled at different ages across a fire-created chronosequence, from 3 months to 30 years. We assessed total reproductive investment every 3 weeks for a year, to determine total investment both in tissues that developed into mature seeds and in tissues that were aborted during the developmental trajectory. This detailed accounting allows us to investigate correlates of reproductive tissue pool investment across and within species.

Finally, given the complexity of measuring all the components of reproductive investment, we assess how well different surrogate measures potentially predict total reproductive investment? For this purpose we consider variables including total seed weight, total fruit weight, and total investment to the point of pollination.

# Methods

## Study system

The study was carried out in Kuring’gai National Park, just to the northeast of Sydney, Australia. The sandstone ridges throughout the park host a coast heath community, whose dynamics have been governed by fire for at least 6000 years (Kodela & Dodson 1988). Fire regimes under traditional aboriginal management are unknown, but current New South Wales National Parks and Wildlife Service (NSW NPWS) management practises seek to achieve an average interval between 7-30 years to maintain the current floristic diversity (NSW Office of the Environment 2006). The community includes perennial species that re-sprout following fire and also obligate seeders, species that are killed by fire and re-establish from seed. The obligate seeders included in this study germinate within a year of the fire and often after the next rain. Since the fire history of the park is well documented, the age of obligate seeders at a site can be estimated. In total, we selected 14 obligate-seeder, woody perennials that are common in the community, with asymptotic heights ranging from 0.5 m – 5 m. They were *Banksia ericifolia* (Proteaceae), *Boronia ledifolia* (Rutaceae), *Conospermum ericifolium* (Proteaceae), *Epacris microphylla* (Ericaceae), *Grevillea buxifolia* (Proteaceae), *Grevillea speciosa* (Proteaceae), *Hakea teretifolia* (Proteaceae), *Hemigenia purpurea* (Lamiaceae), *Leucopogon esquamatus* (Ericaceae), *Persoonia lanceolata* (Proteaceae), *Petrophile pulchella* (Proteaceae), *Phyllota phylicoides* (Fabaceae), *Pimelea linifolia* (Thymelaeaceae), *Pultenaea tuberculata* (Fabaceae). The family Myrtaceae is well represented in the community, but absent from the study, as all locally common species in this family re-sprout following fire. All sites were chosen to have minimal *Eucalyptus* cover, such that *Banksia ericifolia*, *Hakea teretifolia*, and *Allocasuarina distyla* (not included in our study because it is dioecious) would be the dominant canopy species late in succession, at heights of 3-5 m.

## Field measurements

The study was conducted over a single year, with the initial plant measurements and subsequent harvest conducted during the late autumn and early winter, the period of minimal vegetative growth in this plant community, and repeat visits made throughout the year to record reproductive activity. Individuals were sampled at different ages across a fire-created chronosequence, from 3 months to 30 years. Site ages were estimated from fire records maintained by NSW NPWS. At the conclusion of the study, the approximate ages of the individuals on the six sites were: 1.4, 2.4, 5, 7, 9 and 31 years. Plants were tagged during May-June 2012 and harvested during May-June 2013, with a given individual tagged and harvested within 2 weeks of the same calendar date. Only one species, *Persoonia lanceolata*, displayed any shoot extension during these months. These months are similarly a period of minimal reproductive activity – only *Banksia ericifolia*, *Grevillea speciosa,* and (occasionally) *Hemigenia purpurea* flowered during this period – although a number of species had immature fruit from the previous year (*Persoonia lanceolata*) or small buds that would open in the subsequent year (*Boronia ledifolia*, *Conospermum ericifolium*, *Epacris microphylla*, *Grevillea buxifolia*, *Leucopogon esquamatus*).

Seven healthy individuals of each species were selected at each site (and thus age). At the beginning of the study year, the basal diameter was recorded approximately 10 mm above the base to avoid the basal swelling. At the end of the study year, the diameter was remeasured at the same location. The plants were then harvested at ground level and oven dried at 60ºC for at least 1 week. Leaves and stems were separated and weighed.

Flowering parts on all individuals were recorded during repeat censuses, every four weeks during cooler months and every three weeks during spring and summer. At each census, all flowering parts were counted, including buds (by size class), flowers, young fruit, and mature fruit. For some species the size of immature and mature fruit and cones was also measured, as the final size of the structures was quite variable. The exact flowering parts considered varied considerably by species due to their diverse floral structures. Flowcharts detailing what flower parts were included for each species are provided in the Supplementary Material. The Supplementary Material also includes a table that indicates how each flowering part was counted and/or measured for each species. Each of the flower parts was independently collected from multiple untagged individuals in the community to determine its dry weight.

## Calculating reproductive investment and cost components

Total reproductive effort (RE) is the sum of investment in all the different flowering parts during the year, tabulated on a dry mass basis. For each species, reproductive parts were designated as either forming up to the point of pollination (pollen-attraction; i.e. the flower) or post-pollination and were summed into one of the two respective investment pools. For floral parts that were present at the time of pollination and continued to develop into either the seed or packaging and dispersal tissues post-pollination, the fraction of the final mass present at the time of pollination was designated part of the pollen-attraction investment and the remaining fraction as part of the packaging and dispersal investment. All calculations were made on an individual basis, although the weights of many plant parts are based on species level measurements. These calculations yielded total pollen-attraction tissue investment and total provisioning tissue investment. Total pollen-attraction costs and total provisioning costs are calculated by dividing the respective investment values by seed count.

To calculate the three success costs components, pollen-attraction costs, packaging and dispersal costs, and seed weight, the unit weight of reproductive parts required for the successful creation and provisioning of a single propagule were summed together. For pollen-attraction tissues, unit weight was determined by dividing the mass of the part at the time of pollination by the number of ovules it supported. All calculations make the assumption that each species produces a fix number of ovules per flower, but individual-level calculations are made for cones or inflorescence stalks which support variable numbers of flowers and hence ovules. For packaging and dispersal tissues, the unit weight was calculated by dividing the mass of the part at seed maturity by the number of seeds it supported. For seed weight, we chose to designate the endosperm and embryo as the primary reproductive unit, for it provides a consistent comparison of tissue weights across species. It is hereafter referred to as *seed size*. In contrast, the propagule includes the seed coat and additional dispersal tissues in some species, but not others. See the Supplementary Material for a depiction of the parts for each species and the number of ovules in each part.

Discarded pollen-attraction tissue costs were then determined by the following formula:

Total pollen-attraction costs – Successful pollen-attraction costs

Discarded provisioning tissue costs were then determined by the following formula, where successful provisioning costs is the sum of seed size and successful packaging and dispersal costs:

Total provisioning costs – Successful provisioning costs

Reproductive count values used in the manuscript are defined as follows: *Ovule count* indicates the count of all ovules initiated by the plant. *Reach flowering count* indicates the count of ovules that developed to maturity and were presented to pollinators. *Post-pollen count* indicates the count of ovules that experienced at least some provisioning and is divided into *seed count*, the count of mature seeds formed, and *post-pollen aborted count,* the count of zygotes that aborted after provisioning had commenced. All counts are for a one-year time period.

## Statistical methods

All statistical analyses were completed using the SMATR package in R (version ###).

# Results

## Accessory costs and accessory cost components

Of the 599 plants included in this study, 223 individuals produced at least one seed during the year. Across these individuals, on average 97.5% of reproductive investment went to accessory tissues rather than to seeds, decreasing to 91.5% if the entire propagule weight was treated as direct investment in offspring instead of just the embryo and endosperm components. Hereafter, all results report results for the embryo and endosperm component, designating them as seed size. Across species, accessory costs ranged from a low of 95.8% for *Epacris microphylla* to a high of 99.8% for *Hakea teretifolia* (Table 1).

Total reproductive costs can be divided into discarded tissue costs (the weight of all aborted and discarded parts, including mature flowers that fail to set seed) versus reproductive success costs (seed weight plus the total per ovule cost of required floral parts, both before pollination and during seed provisioning). Only the two cone-bearing species, *Banksia ericifolia* and *Petrophile pulchella*, had success costs that were higher than discarded tissue costs (Table 1). Three species, *Hakea teretifolia*, *Phyllota phylicoides*, and *Pultenaea tuberculata* spent more than 90% of their reproductive investment on discarded tissues (Table 1). For most species, these discarded tissues were predominantly pre-provisioning, with aborted seeds and fruit a minor component of discarded tissue costs (Table 1). Note that fruit that abort after pollination but before the onset of visible provisioning are recorded as shed flowers, such that pollen-attraction costs (pre-provisioning) includes the costs associated with ovules that are aborted both due to lack of pollination and due to early maternal selection.

Total success costs are divided into mass of parts formed up to the point of pollination (pollen-attraction costs) versus the mass of the seed, packaging, and dispersal structures (provisioning costs). The relative costs of these components shifted markedly across species (Table 1). Four species, *Epacris microphylla, Hemigenia purpurea, Pimelea linifolia, and Pultenaea tuberculata* had pollen-attraction costs that were greater than 50% of total success costs, while 5 species had pollen-attraction costs that were less than 10% of total success costs (Table 1). The percentage of success costs invested in provisioning tissues (including the seed itself) ranged from a low of 18% (for *Epacris microphylla*) to a high of 99% (*Banksia ericifolia*) (Table 1). The maximum percentages of reproductive investment any species invested directly in seeds were 4.2% for *Epacris microphylla* and 4.1% for *Hemigenia purpurea*.

## Observed trade-offs

Plants produce many inexpensive ovules or proportionally fewer more expensive ovules, such that the relationship between ovule count at the time of pollination, scaled to the plant’s leaf area, versus pollen-attraction costs is highly significant and has a slope not significantly different from -1 (Figure 2a; r2=0.88, slope = -1.12, with confidence interval [-0.90 – -1.41]). Similarly, plant produce a greater number of more expensive seeds or proportionally fewer less costly seeds, such that the relationship between seed count, scaled to the plant’s leaf area, and reproductive costs also has a slope of -1 (Figure 2a; r2=0.93, slope = -0.99, with confidence interval [-0.84 – -1.17]).

There also exists a trade-off between choosiness (ovule to seed ratio, the inverse of seedset) and pollen-attraction costs, scaled to the plant’s leaf area (Figure 2b; r2=0.26, rising to r2=0.77 when *Epacris microphylla* with oddly high leaf area relative to all other metrics is removed; slope = -1.25, with confidence interval [-0.91 – -1.71]). Plants which expend less of their energy budget to produce a single mature ovule, abort and discard a greater proportion of the ovules displayed to pollinators.

## Changes in relative energy investment with seed size

The strong trade-offs between the cost to produce a specific reproductive tissue and the number of units produced by the plant is manifested as shifts in the proportion of reproductive energy invested in different reproductive tissue pools across the seed size spectrum. Larger-seeded species expend a greater proportion of their *success costs* on provisioning tissues versus pollen-attraction tissues in comparison to smaller-seeded species (Figure 2c; r2= 0.80, p<0.0001). As seed size increases, there is also a trend toward increasing expenditure on discarded pollen-attraction tissues in comparison to successful pollen-attraction tissues (Figure 2d; r2= 0.60, p=0.0012), reflecting the increased choosiness (decreased seed set) in larger-seeded species (r2 =0 .59 for the seed set-seed size regression; p = 0.0013). Increased seed size was only marginally related to a shift in the proportion of provisioning energy invested in successful versus discarded tissues, with larger-seeded species showing a slight increase in proportional investment in successful tissues (Figure 2e; r2= 0.24, p=0.0741).

These shifts are also reflected in the relative slopes of the regression between seed size and provisioning costs and between seed size and pollen-attraction costs: provisioning costs show a steeper than isometric increase with seed size, while pollen-attraction costs show a less than isometric increase with seed size (Figure 2f; Table 2). The per seed matured costs of most other reproductive tissue pools show slightly steeper than isometric increases with increasing seed size, indicating the costs are relatively higher for larger-seeded species (Table 2).

## Shifts in accessory costs with plant size, age, or reproductive effort

None of these species demonstrated a decrease in per seed accessory costs with increasing plant size or RE, and only 1 species showed a decrease in per seed accessory costs with age. With only 1/42 tests significant (Supplementary Material), this likely represents little more than chance. There are also two regressions, where accessory costs increased with plant size or age (Supplementary Material).

## Correlates with total reproductive investment

Of the 599 plants included in this study, 357 individuals produced buds and 223 individuals produced mature seeds. Even among the individuals that produced seeds, propagule investment was only rather loosely correlated with total reproductive investment, both within and across species (Tables 3, Figure 3, and Supplementary Material). All but one species showed a significant correlation between the two metrics, but only three species displayed an r2 above 0.80 and only eight of the species had an r2 above 0.70. Furthermore, the slopes and intercepts of the relationship differed across species with the result that the correlation between reproductive investment and propagule investment across individuals of all species had an r2 of just 0.52 (Figure 3a, Table 3) and only four of the species had slopes and intercepts identical to the all-individuals regression (Supplementary Material).

To assess what approximation of reproductive investment was the best alternative to measuring total reproductive investment, we regressed additional investment categories against total reproductive investment. Measures that included only investment in tissues associated with the production of mature seeds, were inferior predictors of total reproductive investment compared to measures that included investment in discarded tissues (Table 3). In particular, note that the correlation between investment in all discarded tissues versus all reproductive tissues was 0.97, while the correlation between investment in all successful tissues (success costs\*seed count) versus all reproductive tissues was just 0.73. Investment in discarded tissues is a better predictor for two reasons. First, because discarded tissues accounted for 73% of total reproductive investment; and second, because energy investment into buds and flowers was more predictable, while further filtering processes occur before buds become mature seeds. A composite metric, the count of buds initiated \* average flower mass, when regressed against total reproductive investment, had an r2 of 0.92, making it nearly as strong a predictor of total reproductive investment as discarded tissue investment. This composite metric has the merits that it would be relatively easy to measure on large numbers of plants and that it effectively combines both the within and across species variation (Figure 3b, Table 3, Supplementary Material). Twelve of the species had the same slope for the relationship and eleven of the species had the same intercept for the relationship as the all-individuals regression (Supplementary Material).

# Discussion

There were three key outcomes from this study. First, these long-lived perennial plants expended an astounding proportion of reproductive energy on accessory costs. Investment in seed dry mass represented a quite modest proportion of total reproductive investment (RE) for the 14 perennial species included in this study, with just 0.2-4% of RE going to seeds versus other reproductive tissues (Table 1). Even the individual with the lowest accessory costs invested just 9.5% of its RE into the seed itself. Second, there existed trade-offs between ovule count and pollen-attraction costs and between seed count and total reproductive costs, indicating these exists a fixed pool of energy to invest and species differ in the relative cost of a part versus the number of parts they can produce. We also observed a trade-off between choosiness, defined as the inverse of seedset, and pollen-attraction costs: species that expend less energy to produce an ovule produce a greater excess of ovules. These are species at the *parental* *optimist* end of the optimist-pessimist spectrum, which have proportionally costlier provisioning tissues relative to pollen attraction tissues (Rosenheim *et al.* 2014). Combining these lines of thought, we can show that the *parental optimists* were, as predicted, the large-seeded species: part of the big seed-size, low seedset strategy is to invest proportionally less in flower construction to the point of pollination and proportionally more in provisioning tissues. The third major result from these data was that for perennial species with low seedset, total reproductive investment was best predicted by energy expenditure in buds and flowers, not by investment in seeds or fruit.

## Accessory costs are large

All species in this study allocated an enormous proportion of RE to accessory costs, both the required costs, designated *success costs*, and discarded tissues (Figure 1a, Table 1). Many estimates of plant energy investment in reproduction do not account for total accessory costs, leading to potentially misleading results (reviewed in Obeso 2002; Lord & Westoby 2006; Rosenheim et al. 2014; Wenk & Falster 2015). For example, studies seeking to estimate the cost of reproduction, may reach erroneous conclusions if they record only shifts in seed production year upon year, ignoring investment in accessory tissues (Obeso 2002). Reproductive allocation, the proportion of energy spent on reproduction, instead of on growing and replacing vegetative tissue (Ashman 1994; Bazzaz, Ackerly & Reekie 2000; Wenk & Falster 2015), will also be substantially underestimated, leading to overestimates of the proportion of energy (and absolute amount of energy) available for vegetative growth. The current study indicates accurate calculations of RE must tabulate all pools of accessory tissues. Indeed, across the species studied, both discarded tissue costs and success cost components (see Figure 1a for definitions) contributed to the high accessory costs (Table 1).

The success-associated costs, are those required for the formation of a seed, and include pollen attraction costs and seed provisioning costs, the latter divided into packaging and dispersal costs versus the seed itself (Figure 1a, Table 1). The study species have diverse floral and fruiting structures, such that disparate tissues comprise success cost expenditures in different species. For three species (*Epacris microphylla, Hemigenia purpurea,* and *Pimelea linifolia*), the costs of producing pollen-attraction tissues (on flowers that develop into mature seeds) was 21-27% of total RE, while for other species it was substantially less (Table 1). The two cone-producing species, *Banksia ericifolia* and *Petrophile pulchella,* had the costliest packaging and dispersal tissues, spending 71.0% and 60.5% of total RE, respectively. Other species also had high packaging and dispersal expenditure due to structures including fleshy fruit (*Persoonia lanceolata*), woody seedpods (*Grevillea* species), and thick seedcoats (*Leucopogon esquamatus*). These are tissues that must be produced to mature each seed and their exact structures have presumably evolved to optimize seed production and survival.

Discarded tissues, those tissues associated with ovules that abort instead of developing into a mature seed, are the complement to success investment and for 12 of the 14 study species, discarded tissues accounted for more than 60% of total reproductive investment (Table 1). Only in *Banksia ericifolia* and *Petrophile pulchella,* the two species with very high energy investment in woody cones,was a smaller proportion of RE attributable to discarded tissues. The majority of discarded tissue costs was due to buds and flowers that were aborted before seed provisioning became substantial (Table 1). Indeed, a large energy investment in discarded tissues is true for all species that display low seed or fruit sets (Stephenson 1981; Sutherland 1986; Ramirez & Berry 1997; Knight *et al.* 2005), with a strong negative correlation between species average seedset and the proportion of reproductive energy going to discarded tissues in this study (r2=0.56, p = 0.0031 when excluding the species producing the largest cones, *Banksia ericifolia*). High discarded costs should not be considered a pointless cost to plants: plants should have evolved to produce the number of ovules that leads to the number of zygotes they are able to provision. Having a surplus of ovules may help with attracting pollinators or allow the plant to be selective about which zygotes to mature. Indeed, explanations for the abortion of a large number of mature ovules near the time of pollination include environmental stochasticity, pollen-limitation, poor pollen-tube growth, pollen incompatibility, selective abortion, and resource limitation (Ashman *et al.* 2004; Knight *et al.* 2005; Ruane, Rotzin & Congleton 2014). Additional zygotes will be lost during the provisioning period due to factors including insect attack and poor environmental conditions.

In the following section we explore whether the relative investment in different accessory cost pools shifted predictably based on three trade-offs.

## Count-cost and choosiness-investment strategy trade-offs observed

In the introduction we identified three predicted trade-offs. The first two trade-offs describe how a fixed pool of energy, relative to plant size, can be divided into many small units or proportionally fewer large units. Abundant theoretical and empirical evidence underpins the seed size-seed number trade-off and here we extend the theory to include two trade-offs that account for the significant accessory costs required for seed production. The first is the ovule count-pollen-attraction costs trade-off, suggesting that plants have a fixed pool of energy to allocate to construct flowers to the point of pollination and may divide this energy into fewer, showier flowers or more, less costly flowers. Endless floral forms exist among plant species and across angiosperms families, plants have also adjusted their per-ovule floral construction costs by increasing the count of ovules in each flower. The second trade-off is between seed count and total reproductive costs: plants, relative to their size, have a fixed pool of energy for reproduction and can invest it in more seeds that cost less to reproduce or fewer seeds with greater per-seed construction costs, including all accessory costs. This is closely related to the well-established seed size-seed count trade-off and taken together demonstrate that large-seeded species are those species with high overall per seed reproductive costs and low seed counts (Smith & Fretwell 1974; Rees & Westoby 1997; Moles & Westoby 2006).

The third trade-off is between choosiness (inverse of seedset) and the relative cost of producing a single ovule to the point of pollination: species for whom producing an ovule is less costly have lower seedset. Species with low seed set are also termed parental optimists: they produce excess pollinated ovules, relative to the seeds they can provision in an average year, because they are always optimistic that the year will be better than average. Due to the large number of ovules they produce, they are selected to reduce their pollen-attraction costs (Haig & Westoby 1988; Schreiber *et al.* 2015; Rosenheim *et al.* 2015). Since these species have lower seed output, they are under stronger selection to produce seeds that will successfully establish (Lord & Westoby 2006). Simply being larger is part of their strategy (Moles & Westoby 2006), but ensuring their seeds have vigorous genotypes is another strategy dimension and one achieved through greater choosiness of the most vigorous embryos shortly after pollination (Willson & Burley 1983; Sutherland 1986; Guittian 1993). Having excess ovules pollinated means parental optimists can be more selective in terms of pollen receipt (Zimmerman & Pyke 1988) and which zygotes to provision (Willson & Burley 1983; Sutherland 1986; Guittian 1993).

Linking together the expected outcomes of these trade-offs, we predict that large seeded species are parental optimists, displaying low seedset (high choosiness) because they produce an overabundance of inexpensive ovules, but then are highly selective about which ovules to provision, because they have high seed masses and relatively high provisioning costs. This led up to hypothesize specific shifts in relative energy allocation with seed size, two of which were strongly borne out by the data. In particular, with increasing seed size, there was an increase in the proportion of energy allocated to successful pollen-attraction tissues versus successful provisioning tissues, reflecting the parental optimist-parental pessimist spectrum. Second, because larger-seeded species discard an increasing proportion of their ovules, discarded pollen-attraction tissues become an increasing proportion of all pollen-attraction tissues with increasing seed size. This pattern was also strongly observed in the data. The third prediction was that parental optimists, once they opted to provision a zygote, would be more likely to continue provisioning it through to a mature seed, because of the strong embryo selection near the time of pollination and the high provisioning costs. There was only a weak trend in this direction, in part reflecting the overall high success rate of embryos once post-pollination provisioning commenced.

Scaling of reproductive costs with seed size  
Previous studies have found an isometric increase in total reproductive costs and accessory costs with increasing seed size (Henery & Westoby 2001; Moles *et al.* 2003; Lord & Westoby 2006, 2012; Chen *et al.* 2010), suggesting that despite the enormous diversity of floral forms and the known adaptive function of many floral parts (Harder & Barrett 2006; Harder & Johnson 2009), all seeds sizes are equally costs to produce, in affirmation of theories on optimal energy allocation (Rosenheim *et al.* 2010; Mironchenko & Kozłowski 2014). In this study, total reproductive costs and accessory costs both showed a steeper than isometric increase with seed size (Table 2), indicating proportion of reproductive energy invested in accessory tissues is higher in larger-seeded species. This suggests there are additional benefits to being large-seeded that have not been explored in this study, such as higher seedling germination and success.

The changes in the proportion of energy going to successful pollen-attraction versus successful provisioning tissues with seed size (Figure 2c), did lead a less than isometric increase in pollen-attraction costs with seed size and greater than isometric increase in provisioning costs with seed size, as has been previously observed (Lord & Westoby 2006, 2012). This is in part because larger seeds tend to have biotic dispersal agents, and animal-dispersed species allocate a greater proportion of their reproductive energy to packaging and dispersal materials (Hughes *et al.* 1994; Moles *et al.* 2005; Eriksson 2008).

## Shifts in accessory costs with plant size and age

An additional motivation for this study was to determine if accessory costs shifted with plant age, size or RE. The theoretical literature suggests that for plants to increase their allocation to reproduction (versus growth) as they grow and age, plants must realize some compounding benefit (Myers & Doyle 1983; Sibly, Calow & Nichols 1985; Reekie & Bazzaz 1987a; Kozlowski 1992). Increasing mortality with age and concurrent decreases in future reproductive value, is one mechanism that can increase reproductive allocation (RA) in older plants. Decreasing accessory costs, and hence more efficient seed production, with increasing RA is another obvious compounding benefit. If, for instance, accessory costs declined with RE, plants should be selected to have fewer, larger reproductive episodes (Kelly 1994; Kelly & Sork 2002) or delay reproduction until they are larger and can invest more energy in reproduction (Cole 1954; Wenk & Falster 2015). This pattern was not observed in this dataset. Across individuals within a species, total accessory costs and accessory cost components did not shift consistently with plant size, age, or total reproductive investment (Supplementary Material). The consistent lack of shift in per seed accessory costs (or seedset, data not shown) with RE (or bud count, data not shown) is notable. There is a large literature on expected and observed trends in pollination and seedset with the size of the floral display, with quite disparate patterns, but we had not anticipated a flat relationship for 13 of 14 species (Supplementary Material). In conclusion, for many species, the sample sizes of the current data set are large and we sampled across their entire age range, such that if a shift in accessory costs (or accessory cost components) existed with plant size, age, or RE it should have been detected in this data.

## Estimating reproductive effort

Realistic estimates of RE are essential for many research questions: plant functional growth models require estimates of the proportion of photosynthetic energy that is allocated to growth versus reproduction (Fisher *et al.* 2010; Falster *et al.* 2011; Scheiter, Langan & Higgins 2013), while demographic models may need estimates of seed production for a given RE (Garcia & Ehrlen 2002; Miller *et al.* 2012). The current study – and others – have shown that plants are allocating energy to many different reproductive tissues, with a notably small proportion going to seeds. However, the detailed measurements required to account for all reproductive energy expenditure are not practical for many research projects and pointing researchers to the best rapidly-obtainable estimates of total RE would be beneficial to many.

Total RE scaled isometrically with seed size, indicating that total RE, *on a species level*, could be broadly estimated by knowing seed size (r2 = 0.56 (*p = 0.0021*), increasing to r2 = 0.69 (*p = 0.0004*) if *Epacris microphylla*, with very small seeds,is omitted). Total plant weight was similarly strongly correlated with seed size *on a species level* (r2 = 0.62, *p = 0.0008*). These relationships show that species that are larger-seeded also have a larger adult size and therefore had more energy going to reproduction. However, seed size cannot provide an estimate of RE for individual plants in a population

At the individual level, embryo and endosperm investment, propagule investment, and fruit investment were relatively poor predictors of RE (Table 3), with r2=0.66, r2=0.53 and r2=0.68, respectively, for regressions across individuals of all species. Even within species, knowing seed investment provided only a mediocre total RE, with only 8 of the 14 species having an r2>0.70 and one species not even displaying a significant correlation across individuals (Supplementary Material). In contrast, all investment in discarded tissues, primarily representing investment in aborted flowers and buds, and our artificial composite measure, “total bud count \* average flower mass at the time of pollination”, provided excellent estimates of total RE (r2=0.96 and r2=0.92 respectively for regressions across all individuals; Table 3). While total discarded tissue investment is not a “quick measure”, requiring repeat visits to the field and tedious accounting, the composite measure would work well for species where most of their buds are visible at a single point in time. Doing a single bud count and determining flower weight for the species would be a manageable prospect. These results conversely demonstrate that if your research question requires seed investment or seed count as an output, estimates of RE will not accurately predict seed production. Instead, and in contrast to many herbaceous species (Shipley & Dion 1992), this is a measure that must be measured at the individual level for perennial species with relatively low seedset.

The explanation for the poor correlation between seed investment and RE is clear: most of these species have relatively low seedset (Table 1) and moreover, seed set is quite variable across individuals at a single site (Figure 3). Therefore, although the number of initiated buds is well-predicted by plant size (for most species) and is in turn tightly correlated with total reproductive investment (for all species), the unpredictability of seedset and overall low seedset means that investment in seeds, at the individual level, cannot be predicted by any easy-to-measure metrics. Many stochastic processes, from pollinator activity to pollen compatibility to resource availability lie between bud production and seed production (Herrera *et al.* 1998; Wesselingh 2007; Gómez 2008). These processes lead to both individual and inter-annual variation in seed production (Copland & Whelan 1989; Mitchell 1997; Herrera *et al.* 1998).

## Considerations

To reach meaningful conclusions about trade-offs between reproductive costs, counts, and seedset, accurate measurements of total reproductive investment is essential. Our accounting scheme is very good, but of course imperfect. The largest source of error is that we have not measured nectar production, despite knowing that several of the species produce abundant nectar, particularly *Banksia ericifolia*, *Hakea teretifolia* andboth *Grevillea* species (Pyke 1983; Pyke, O’Connor & Recher 1993; Lloyd, Ayre & Whelan 2002). Very rough back of the envelope calculations, based on studies of closely related species in nearby communities, indicate nectar production increases total reproductive investment by ~20% for *Grevillea speciosa*, 10% for *Hakea teretifolia*, and well under 5% for the other two species, increasing pollen-attraction costs relative to provisioning costs.

These seemingly large energy expenditures, segue to our next consideration: Is dry weight the best measure of energy expenditure, especially in a community growing on soils known to be very low in P (Beadle 1968)? Previous studies indicate that nutrient concentrations may better estimate energy allocation choices (Reekie & Bazzaz 1987b; Ashman 1994; Rosenheim *et al.* 2014), but also that all currencies yield similar results. It is however, possible that in a P-limited community, it is less “costly” to produce copious quantities of nectar, for carbon is not limiting. This is a direction for future investigations. A final consideration, is how to choose which tissues to include as “reproductive tissues”, since some green reproductive tissues are known to photosynthesize (Cohen 1976; Reekie & Bazzaz 1987a; Wesselingh 2007). Since the net photosynthetic benefit of green reproductive tissues was unknown in this study and likely varied enormously across species, tissues and time, we adopted the parsimonious approach of considering all plant parts produced solely for the benefit of reproduction as components of reproductive investment.

Not addressed by this dataset, are other known factors that undoubtedly also contribute to low seedset in this system, including pollen-limitation (Burd 2008, 2016) and environmental stochasticity. Insufficient pollen receipt may certainly be contributing to the patterns observed in this community, but given recent theoretical treatments that suggest pollen-limitation should be more severe among parental-pessimists (Rosenheim *et al.* 2014, 2016), it is unlikely the observed trend of lower seedset among the parental-optimists is primarily attributable to pollen-limitation. Environmental stochasticity, both in terms of pollen receipt and resources to provision embryos, also select for overproduction of embryos in parental optimists (Haig & Westoby 1988; Rosenheim *et al.* 2014). Indeed the tendency towards over- (or under-) production of ovules among parental optimists (or pessimists) will be exacerbated by environmental stochasticity, because plants will invest more heavily in the cheaper of the tissue categories (Rosenheim *et al.* 2010, 2014). Indeed, it is from the environmental stochasticity in resource supply that “parental optimists” have their name: They over-produce ovules because they are optimistic about resource supply and the number of ovules they will be able to mature and therefore have additional ovules that can be matured when sufficient resources are available (Mock & Forbes 1995; Burd *et al.* 2009; Schreiber *et al.* 2015; Rosenheim *et al.* 2015).

The coastal heath community in eastern Australia has been well studied, both as a focal point for data collection on trait ecology and because of a general interest in the family Proteaceae, a dominant in this and many nearby communities. Indeed, 7 of the 14 species in this study are in Proteaceae, a family known to have particularly low fruit set (Hermanutz *et al.* 1998) (###) and to produce large woody fruits designed to allow seeds to withstand the frequent fires and then germinate following fire. Five species of *Grevillea* studied in communities nearby had fruit set between 1.5-9.6% (Hermanutz *et al.* 1998), similar to the seedset of the two species growing at our study site (Table 1). *Grevillea* species tend not to be self-incompatible, with the low fruit set attributed to pollen limitation and flower and fruit predation. *Banksia ericifolia*, *Hakea teretifolia*, and *Petrophile pulchella* all have fire-resistant fruits, and *Banksia* *ericifolia* and *Hakea* *teretifolia* have the largest seeds and greatest packaging and dispersal investment among the species in this study. Although none of the species included in the study are explicitly masting species, the two cone-producing species, *Banksia* *ericifolia* and *Petrophile pulchella*, do not form seeds each year (pers. obs.). This is shown at the population level by the large number of reproductively mature individuals that do not produce any seeds – or sometimes even any buds – in a given year. As has been shown in other species of *Banksia* (Copland & Whelan 1989), the inter-annual variability in seed production for these species may be due to resource limitation in the year following seed production.

## Conclusions

In summary, the correlations observed in our study indicate that seed size, ovule production versus seed production, and the magnitude of specific RE pools are coordinated across species. While a plant’s accessory costs may be startlingly large at first glance, one must assume their allocation of energy to different tissues represents an evolved strategy to maximize fitness. Identifying trade-offs between specific energy allocation choices – and then determining that energy allocation within this community matches the predicted patterns – provides a framework for understanding coordinated responses for seed size, seedset, and allocation to pollen-attraction versus seed provisioning tissues. Just as species have long been shown to follow a seed size-seed number trade-off, so do all species have the same amount of energy (relative to their leaf area) to invest in ovules, leading to a trade-off between the cost pollen-attraction tissues and ovule count. Large-seeded, low seedset species have proportionally less costly pollen-attraction tissues and produce a proportionally larger excess of ovules relative to, on average, the seeds they are able to provision.

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