# Supervised learning

Inteligencia Artificial en los Sistemas de Control Autónomo Máster en Ciencia y Tecnología desde el Espacio

Departamento de Automática





## **Objectives**

- 1. Define Machine Learning (ML)
- 2. Delimite ML scope3. Introduce the main ML tasks
- 4. Recognize problems as ML tasks

# Bibliography

- Bishop, Christopher M. Pattern Recognition and Machine Learning. 2nd edition. Springer-Verlag. 2011
- Müller, Andreas C., Guido, Sarah. Introduction to Machine Learning with Python. O'Reilly. 2016

# Table of Contents



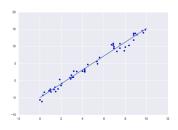
# Linear regression (I)

Lineal regression assumes a linear relationship among variables

- This limitation can be easely overcome
- Surprisingly good results in high dimensional spaces

# Lineal regression

$$y = a_0 + a_1 x_1 + a_2 x_2 + \dots + a_n x_n$$



## Linear regression (II)

#### Several methods to fit coefficients

- Ordinary Least Squares (OLS)
- Generalized Least Squares (GSL)
- Weighted Least Squares (WLS)
- Generalized Least Squares with AR Covariance Structure (GLSAR)

#### Regularization: Term that penalizes complexity

- LI (Lasso regression)
- L2 (Ridge regression)
- ElasticNet: L1 and L2

٠,				
		10	c	Ċ
- 4	Lc	เอ	0	u

 $\textstyle \lambda \sum_j^{\mathfrak{n}} \beta_j^2$ 

# Ridge

$$\lambda \sum_{j=1}^{n} |\beta_{j}|$$

#### ElasticNet

$$\alpha \sum_{j}^{\tt n} \beta_{j}^2 + (1-\alpha) \sum_{j}^{\tt n} |\beta_{j}|$$



# ARIMA (I)

#### AR: Autoregressive model

- Current observation depends on the last p observations
- Long term memory

#### MA: Moving Average model

- Current observation linearly depends on the last q innovations
- Short term memory

#### ARMA model = AR + MA

• ARMA(p, q): Two hyperparameters, p and q

# AR(p)

$$X_t = c + \sum_{i=1}^p \phi_i X_{t-1} + \epsilon_t$$

## MA(q)

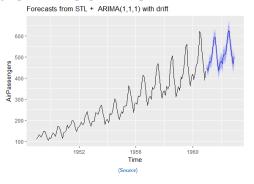
$$X_t = \mu + \epsilon_t + \theta_1 \epsilon_{t-1} + ... + \theta_q \epsilon_{t-q}$$



## ARIMA (II)

#### ARIMA = AR + i + MA (AR integrated MA)

- ARIMA(p, d, q)
- Three integer parameters: p, q and d (in practice, low order models)



autoarima: search over p, q and d

