

# Supervised learning

Aprendizaje Automático para la Robótica  
Máster Universitario en Ingeniería Industrial

Departamento de Automática

## Objectives

1. Extend supervised learning algorithms
2. Apply supervised learning to real-world problems

## Bibliography

- Géron, Aurélien. Hands-On Machine Learning with Scikit-Learn, Keras & TensorFlow. O'Reilly. 2020
- Müller, Andreas C., Guido, Sarah. Introduction to Machine Learning with Python. O'Reilly. 2016

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# k-Nearest Neighbors

## kNN classification (I)

Diagrama 1-NN y 3-NN.

# k-Nearest Neighbors

## kNN classification (II)

Diagrama frontera para varios valores de K

# k-Nearest Neighbors

## kNN regression

TODO

# k-Nearest Neighbors

## Scikit-learn

### TODO

`sklearn.cluster.AgglomerativeClustering`

#### Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

#### Attributes:

- `n_clusters`: int
- `labels_`: ndarray (n\_samples)

Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

# k-Nearest Neighbors

## Summary

Hyperparameters	Advantages	Disadvantages



# Linear models

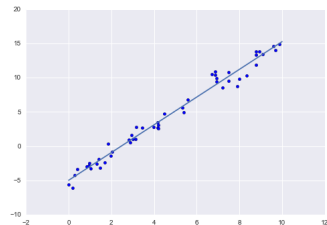
## Linear regression (I)

Linear regression assumes a linear relationship among variables

- This limitation can be easily overcome
- Surprisingly good results in high dimensional spaces

### Linear regression

$$y = a_0 + a_1x_1 + a_2x_2 + \cdots + a_nx_n$$



## Linear models (II)

Several methods to fit coefficients

- Ordinary Least Squares (OLS)
- Generalized Least Squares (GSL)
- Weighted Least Squares (WLS)
- Generalized Least Squares with AR Covariance Structure (GLSAR)

**Regularization:** Term that penalizes complexity

- $L_1$  (Lasso regression)
- $L_2$  (Ridge regression)
- ElasticNet:  $L_1$  and  $L_2$

Lasso

$$\lambda \sum_j \beta_j^2$$

Ridge

$$\lambda \sum_j |\beta_j|$$

ElasticNet

$$\alpha \sum_j \beta_j^2 + (1 - \alpha) \sum_j |\beta_j|$$

# Linear models

## Scikit-learn

### TODO

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#### Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

#### Attributes:

- `n_clusters`: int
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Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

# Linear models

## Summary

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Hyperparameters

Advantages

Disadvantages

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# Naive Bayes Classifiers

TODO

# Naive Bayes Classifiers

## Scikit-learn

```
sklearn.cluster.AgglomerativeClustering
```

Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

Attributes:

- `n_clusters`: int
- `labels_`: ndarray (n\_samples)

Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

# Naive Bayes Classifiers

## Summary

Hyperparameters	Advantages	Disadvantages

# Decission Trees

TODO



# Decision Trees

## Scikit-learn

```
sklearn.cluster.AgglomerativeClustering
```

### Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

### Attributes:

- `n_clusters`: int
- `labels_`: ndarray (n\_samples)

Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

# Decision Trees

## Summary

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Hyperparameters	Advantages	Disadvantages
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# Ensembles of Decision Trees

TODO

# Ensembles of Decision Trees

## Ensembles of Decision Trees : Scikit-learn

```
sklearn.cluster.AgglomerativeClustering
```

Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

Attributes:

- `n_clusters`: int
- `labels_`: ndarray (n\_samples)

Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

# Ensembles of Decision Trees

## Summary

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Hyperparameters	Advantages	Disadvantages
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# Support Vector Machines

TODO

# Support Vector Machines

## Kernelized Support Vector Machines

TODO

# Scikit-Learn



# Support Vector Machines

## Scikit-learn

`sklearn.cluster.AgglomerativeClustering`

Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

Attributes:

- `n_clusters`: int
- `labels_`: ndarray (n\_samples)

Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

# Support Vector Machines

## Summary

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Hyperparameters

Advantages

Disadvantages

---

A

B

TODO

## A

## B: Scikit-learn

```
sklearn.cluster.AgglomerativeClustering
```

## Constructor arguments:

- `linkage`: 'ward', 'complete', 'average', 'single'

## Attributes:

- `n_clusters`: int
- `labels_`: ndarray (n\_samples)

Methods: `fit()`, `fit_predict()`

(Scikit-Learn reference)

## A

## B: Summary

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Hyperparameters

Advantages

Disadvantages

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# Algorithms

## ARIMA (I)

### AR: Autoregressive model

- Current observation depends on the last  $p$  observations
- Long term memory

AR( $p$ )

$$X_t = c + \sum_{i=1}^p \phi_i X_{t-i} + \epsilon_t$$

### MA: Moving Average model

- Current observation linearly depends on the last  $q$  innovations
- Short term memory

MA( $q$ )

$$X_t = \mu + \epsilon_t + \theta_1 \epsilon_{t-1} + \dots + \theta_q \epsilon_{t-q}$$

ARMA model = AR + MA

- ARMA( $p, q$ ): Two hyperparameters,  $p$  and  $q$

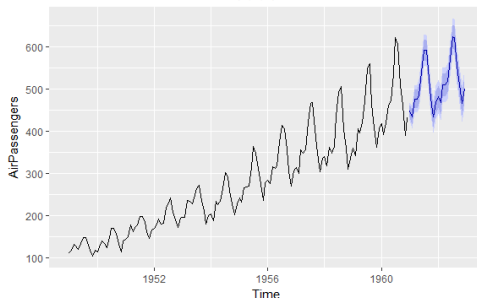
# Algorithms

## ARIMA (II)

ARIMA = AR + i + MA (AR integrated MA)

- ARIMA(p, d, q)
- Three integer parameters: p, q and d (in practice, low order models)

Forecasts from STL + ARIMA(1,1,1) with drift



(Source)

**autoarima:** search over p, q and d